

# Package ‘GBJ’

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**Type** Package

**Title** Generalized Berk-Jones Test for Set-Based Inference in Genetic Association Studies

**Version** 0.5.3

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**Description** Offers the Generalized Berk-Jones (GBJ) test for set-based inference in genetic association studies. The GBJ is designed as an alternative to tests such as Berk-Jones (BJ), Higher Criticism (HC), Generalized Higher Criticism (GHC), Minimum p-value (minP), and Sequence Kernel Association Test (SKAT). All of these other methods (except for SKAT) are also implemented in this package, and we additionally provide an omnibus test (OMNI) which integrates information from each of the tests. The GBJ has been shown to outperform other tests in genetic association studies when signals are correlated and moderately sparse. Please see the vignette for a quickstart guide or the paper at <doi:10.1080/01621459.2019.1660170> for full details.

**Depends** R (>= 2.10)

**Imports** Rcpp (>= 0.12.7), mvtnorm, SKAT, stats,

**LinkingTo** Rcpp, BH

**License** GPL-3

**RoxygenNote** 7.0.2

**Suggests** knitr, rmarkdown, bindata, rje, testthat

**VignetteBuilder** knitr

**NeedsCompilation** yes

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BJ	<i>BJ.R</i>
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### Description

Calculate the Berk-Jones test statistic and p-value.

### Usage

```
BJ(test_stats, cor_mat = NULL, pairwise_cors = NULL)
```

### Arguments

test_stats	Vector of test statistics for each factor in the set (i.e. marginal test statistic for each SNP in a gene).
cor_mat	d*d matrix of the correlations between all the test statistics in the set, where d is the total number of test statistics in the set. You only need to specify EITHER cor_mat OR pairwise_cors.
pairwise_cors	A vector of all d(d-1)/2 pairwise correlations between the test statistics. You only need to specify EITHER cor_mat OR pairwise_cors.

### Value

A list with the elements:

BJ	The observed Berk-Jones test statistic.
BJ_pvalue	The p-value of this observed value, given the size of the set and correlation structure.

**Examples**

```
# Should return statistic = 1.243353 and p_value = 0.256618
set.seed(100)
Z_vec <- rnorm(5) + rep(1,5)
cor_Z <- matrix(data=0.2, nrow=5, ncol=5)
diag(cor_Z) <- 1
BJ(test_stats=Z_vec, cor_mat=cor_Z)
```

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calc\_score\_stats      *calc\_score\_stats.R*

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**Description**

Starting with individual-level data on  $p$  factors, generate score test statistics for each factor for input into GBJ/GHC/HC/BJ/minP. Also get the correlations between these test statistics. Designed to be used with linear or logistic or log-linear regression null models.

**Usage**

```
calc_score_stats(null_model, factor_matrix, link_function, P_mat = NULL)
```

**Arguments**

null_model	An R regression model fitted using <code>glm()</code> . Do not use <code>lm()</code> , even for linear regression!
factor_matrix	An $n \times p$ matrix with each factor as one column. There should be no missing data.
link_function	Either "linear" or "logit" or "log"
P_mat	The projection matrix used in calculation may be passed in to speed up the calculation. See paper for details. Default is null.

**Value**

A list with the elements:

test_stats	The $p$ score test statistics.
cor_mat	The $p \times p$ matrix giving the pairwise correlation of every two test statistics.

**Examples**

```
set.seed(0)
Y <- rbinom(n=100, size=1, prob=0.5)
null_mod <- glm(Y~1, family=binomial(link="logit"))
factor_mat <- matrix(data=rnorm(n=100*5), nrow=100)
calc_score_stats(null_mod, factor_mat, "logit")
```

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estimate_ss_cor	<i>estimate_ss_cor.R</i>
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### Description

Estimate the correlations between GWAS summary statistics using reference panel eigenvectors and reference panel genotypes.

### Usage

```
estimate_ss_cor(ref_pcs, ref_genotypes, link_function)
```

### Arguments

ref_pcs	An n*m matrix containing PCs calculated from the reference panel. Here n is the number of subjects in the reference panel and m is roughly the number of PCs used in the original analysis which produced the summary statistics.
ref_genotypes	An n*d matrix holding the genotypes from the reference panel, where the d columns correspond to the d SNPs for which we have summary statistics. No missing data allowed.
link_function	Either "linear" or "logit" or "log".

### Value

A list with the elements:

cor_mat	The d*d matrix giving the pairwise correlation of every two test statistics.
---------	--

### Examples

```
ref_pcs <- matrix(data=runif(n=1000, min=-0.2, max=0.2), ncol=5)
ref_genotypes <- matrix(data=rbinom(n=2000, size=2, prob=0.3), ncol=10)
estimate_ss_cor(ref_pcs=ref_pcs, ref_genotypes=ref_genotypes, link_function="linear")
```

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FGFR2	<i>Genotypes at FGFR2 SNPs for subjects from 'GBR' population in the 1000 Genomes Project.</i>
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### Description

A dataset containing the genotypes (number of minor alleles) for each of 91 subjects from the 'GBR' population in the 1000 Genomes Projects. There are 64 SNPs documented here, all residing in the FGFR2 gene.

### Usage

```
data(FGFR2)
```

**Format**

A matrix with 91 rows (one for each subject) and 64 columns (one for each SNP)

**Source**

<http://www.internationalgenome.org/data>

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GBJ

*GBJ.R*

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**Description**

Calculate the Generalized Berk-Jones test statistic and p-value.

**Usage**

```
GBJ(test_stats, cor_mat = NULL, pairwise_cors = NULL)
```

**Arguments**

<code>test_stats</code>	Vector of test statistics for each factor in the set (i.e. marginal test statistic for each SNP in a gene).
<code>cor_mat</code>	$d \times d$ matrix of the correlations between all the test statistics in the set, where $d$ is the total number of test statistics in the set. You only need to specify EITHER <code>cor_mat</code> OR <code>pairwise_cors</code> .
<code>pairwise_cors</code>	A vector of all $d(d-1)/2$ pairwise correlations between the test statistics. You only need to specify EITHER <code>cor_mat</code> OR <code>pairwise_cors</code> .

**Value**

A list with the elements:

<code>GBJ</code>	The observed Generalized Higher Criticism test statistic.
<code>GBJ_pvalue</code>	The p-value of this observed value, given the size of the set and correlation structure.
<code>err_code</code>	Sometimes if your p-value is very small ( $< 10^{-12}$ usually), R/C++ do not have enough precision in their standard routines to calculate the number accurately. In these cases (and very rarely others) we switch to standard Berk-Jones instead (more stable numerically) and let you know with a message here.

**Examples**

```
# Should return statistic = 0.9248399 and p_value = 0.2670707
set.seed(100)
Z_vec <- rnorm(5) + rep(1,5)
cor_Z <- matrix(data=0.2, nrow=5, ncol=5)
diag(cor_Z) <- 1
GBJ(test_stats=Z_vec, cor_mat=cor_Z)
```

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GBJ_pvalue	<i>GBJ_pvalue.R</i>
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### Description

Calculate the p-value for the Generalized Berk-Jones (GBJ) statistic.

### Usage

```
GBJ_pvalue(observed_gbj, d, pairwise_cors, times_to_try = 5)
```

### Arguments

observed_gbj	The observed value of the GBJ statistic.
d	The number of test statistics in the set.
pairwise_cors	A vector of all $d(d-1)/2$ pairwise correlations between the test statistics, where d is total number of test statistics in the set.
times_to_try	Sometimes the numerical root-finder is finnick, so we have to give it extra chances to try and calculate the p-value if first time is failure. Recommend setting this parameter to 5.

### Value

The p-value of the GBJ test.

### Examples

```
GBJ_pvalue(observed_gbj=2, d=5, pairwise_cors=rep(0.2,10))
```

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gbr_pcs	<i>Simulated Principal Components for 'GBR' population in the 1000 Genomes Project.</i>
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### Description

A dataset containing 5 simulated Principal Components (PCs) for each of 91 subjects from the 'GBR' population in the 1000 Genomes Projects. These would normally be used as covariates in a regression model to control for population stratification.

### Usage

```
data(gbr_pcs)
```

### Format

A matrix with 91 rows (one for each subject) and 5 columns (one for each PC)

---

GHC

*GHC.R*

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### Description

Calculate the Generalized Higher Criticism test statistic and p-value.

### Usage

```
GHC(test_stats, cor_mat = NULL, pairwise_cors = NULL)
```

### Arguments

<code>test_stats</code>	Vector of test statistics for each factor in the set (i.e. marginal test statistic for each SNP in a gene).
<code>cor_mat</code>	$d \times d$ matrix of the correlations between all the test statistics in the set, where $d$ is the total number of test statistics in the set. You only need to specify EITHER <code>cor_mat</code> OR <code>pairwise_cors</code> .
<code>pairwise_cors</code>	A vector of all $d(d-1)/2$ pairwise correlations between the test statistics. You only need to specify EITHER <code>cor_mat</code> OR <code>pairwise_cors</code> .

### Value

A list with the elements:

<code>GHC</code>	The observed Generalized Higher Criticism test statistic.
<code>GHC_pvalue</code>	The p-value of this observed value, given the size of the set and correlation structure.
<code>err_code</code>	Sometimes if your p-value is very small ( $< 10^{-12}$ usually), R/C++ do not have enough precision in their standard routines to calculate the number accurately. In these cases (and very rarely others) we switch to standard Higher Criticism instead (more stable numerically) and let you know with a message here.

### Examples

```
set.seed(100)
Z_vec <- rnorm(5)
cor_Z <- matrix(data=0.2, nrow=5, ncol=5)
diag(cor_Z) <- 1
GHC(test_stats=Z_vec, cor_mat=cor_Z)
```

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HC	<i>HC.R</i>
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### Description

Calculate the Higher Criticism test statistic and p-value.

### Usage

```
HC(test_stats, cor_mat = NULL, pairwise_cors = NULL)
```

### Arguments

<code>test_stats</code>	Vector of test statistics for each factor in the set (i.e. marginal test statistic for each SNP in a gene).
<code>cor_mat</code>	$d \times d$ matrix of the correlations between all the test statistics in the set, where $d$ is the total number of test statistics in the set. You only need to specify EITHER <code>cor_mat</code> OR <code>pairwise_cors</code> .
<code>pairwise_cors</code>	A vector of all $d(d-1)/2$ pairwise correlations between the test statistics. You only need to specify EITHER <code>cor_mat</code> OR <code>pairwise_cors</code> .

### Value

A list with the elements:

<code>HC</code>	The observed Higher Criticism test statistic.
<code>HC_pvalue</code>	The p-value of this observed value, given the size of the set and correlation structure.

### Examples

```
# Should return statistic = 2.067475 and p_value = 0.2755146
set.seed(100)
Z_vec <- rnorm(5) + rep(1,5)
cor_Z <- matrix(data=0.2, nrow=5, ncol=5)
diag(cor_Z) <- 1
HC(test_stats=Z_vec, cor_mat=cor_Z)
```



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`minP`*minP.R*

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### Description

Given a vector of individual test statistics and their pairwise correlations, calculate the MinimumP (see Conneely and Boehnke, 2007) second-level test statistic and its p-value.

### Usage

```
minP(test_stats, cor_mat = NULL, pairwise_cors = NULL)
```

### Arguments

<code>test_stats</code>	Vector of test statistics for each factor in the set (i.e. marginal test statistic for each SNP in a gene)
<code>cor_mat</code>	$d \times d$ matrix of the correlations between all the test statistics in the set, where $d$ is the total number of test statistics in the set. You only need to specify EITHER <code>cor_mat</code> OR <code>pairwise_cors</code> .
<code>pairwise_cors</code>	A vector of all $d(d-1)/2$ pairwise correlations between the test statistics. You only need to specify EITHER <code>cor_mat</code> OR <code>pairwise_cors</code> .

### Value

A list with the elements:

<code>minP</code>	The observed MinimumP test statistic.
<code>minP_pvalue</code>	The p-value of this observed value, given the size of the set and correlation structure.

### Examples

```
# Should return statistic = 0.05918928 and p_value = 0.2525972.
set.seed(100)
Z_vec <- rnorm(5) + rep(1,5)
cor_Z <- matrix(data=0.2, nrow=5, ncol=5)
diag(cor_Z) <- 1
minP(test_stats=Z_vec, cor_mat=cor_Z)
```

---

OMNI\_individual      *omni\_individual.R*

---

### Description

Computes the omnibus test statistic combining GBJ, GHC, minP, and SKAT. This version of the function assumes you have the individual factor data (i.e. genotypes) for each subject. If you only have summary statistics, use `omni_ss()`. You WILL NOT be able to use this function unless you have also loaded the SKAT package (`install.packages("SKAT"); library(SKAT)`).

### Usage

```
OMNI_individual(null_model, factor_matrix, link_function, num_boots = 100)
```

### Arguments

<code>null_model</code>	An R regression model fitted using <code>glm()</code> . Do not use <code>lm()</code> , even for linear regression!
<code>factor_matrix</code>	An $n \times d$ matrix with each factor (i.e. each SNP) as one column. There should be no missing data.
<code>link_function</code>	Either "linear" or "logit" or "log".
<code>num_boots</code>	Number of bootstrap repetitions to find correlation matrix of set-based statistics.

### Value

A list with the elements:

<code>OMNI</code>	The observed omnibus test statistic.
<code>OMNI_pvalue</code>	The p-value of the OMNI test
<code>err_code</code>	Sometimes if your p-value is very small ( $< 1 \times 10^{-10}$ ), R may run into numerical issues. This message will alert you if such a situation occurs.

### Examples

```
factor_matrix <- matrix(data=rbinom(n=1000, size=2, prob=0.3), ncol=5)
Y <- rnorm(n=200)
null_mod <- glm(Y ~ 1)
OMNI_individual(null_model=null_mod, factor_matrix=factor_matrix,
link_function='linear', num_boots=5)
```

---

OMNI_ss	<i>omni_ss.R</i>
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### Description

Computes the omnibus test statistic combining GBJ, GHC, minP, and SKAT. This version of the function assumes you are using GWAS summary statistics. If you individual-level genotype data, use `omni_individual()`.

### Usage

```
OMNI_ss(test_stats, cor_mat, num_boots = 100)
```

### Arguments

<code>test_stats</code>	Vector of test statistics for each factor in the set (i.e. marginal test statistic for each SNP in a gene)
<code>cor_mat</code>	$d \times d$ matrix of the correlations between all the test statistics in the set, where $d$ is the total number of test statistics in the set.
<code>num_boots</code>	Number of bootstrap repetitions to find correlation matrix of set-based statistics.

### Value

A list with the elements:

<code>OMNI</code>	The observed omnibus test statistic.
<code>OMNI_pvalue</code>	The p-value of the OMNI test
<code>err_code</code>	Sometimes if your p-value is very small ( $< 1 \times 10^{-10}$ ), R may run into numerical issues. This message will alert you if such a situation occurs.

### Examples

```
cor_mat <- matrix(data=0.3, nrow=5, ncol=5)
diag(cor_mat) <- 1
test_stats <- as.numeric(mvtnorm::rmvnorm(n=1, sigma=cor_mat))
OMNI_ss(test_stats=test_stats, cor_mat=cor_mat, num_boots=5)
```

---

score\_stats\_only      *score\_stats\_only.R*

---

### Description

Starting with individual-level data on  $p$  factors, generate score test statistics for each factor for input into GBJ/GHC/HC/BJ/minP. DOES NOT get the correlations (assumed known).

### Usage

```
score_stats_only(null_model, factor_matrix, link_function, P_mat = NULL)
```

### Arguments

`null_model`      An R regression model fitted using `glm()`. Do not use `lm()`, even for linear regression!

`factor_matrix`    An  $n \times d$  matrix with each factor as one column. There should be no missing data.

`link_function`    Either "linear" or "logit" or "log".

`P_mat`            The projection matrix used in calculation may be passed in to speed up the calculation. See paper for details. Default is null.

### Value

The  $d$  score test statistics.

### Examples

```
Y <- rbinom(n=100, size=1, prob=0.5)
null_mod <- glm(Y~1, family=binomial(link="logit"))
factor_matrix <- matrix(data=rnorm(n=100*5), nrow=100)
score_stats_only(null_mod, factor_matrix, "logit")
```

---

surv                      *surv.R*

---

### Description

Survival (1 minus the CDF) function of standard normal random variable.

### Usage

```
surv(x)
```

### Arguments

`x`                      Vector of quantiles

**Value**

Probability that a standard normal random variable is greater than  $x$ .

**Examples**

```
surv(0) # Should return 0.5
```

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