

# Package ‘yuima’

September 29, 2014

**Type** Package

**Title** The YUIMA Project package for SDEs

**Version** 1.0.36

**Date** 2014-09-29

**Depends** methods, zoo, stats4, utils, expm, cubature, mvtnorm

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**Description** Simulation and Inference for Stochastic Differential Equations

**License** GPL-2

**URL** <http://R-Forge.R-project.org/projects/yuima/>

**NeedsCompilation** yes

**Repository** CRAN

**Date/Publication** 2014-09-29 15:19:08

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adaBayes	<i>Adaptive Bayes estimator for the parameters in sde model</i>
----------	---

---

**Description**

Adaptive Bayes estimator for the parameters in a specific type of sde.

**Usage**

```
adaBayes(yuima, start, prior,
         lower, upper, method = "nomcmc")
```

**Arguments**

yuima	a 'yuima' object.
start	initial suggestion for parameter values
prior	a list of prior distributions for the parameters [function].
lower	...
upper	...
method	nomcmc requires package cubature

**Details**

Calculate the values of the parameters  $\theta_1$  and  $\theta_2$ . When the quasi-likelihood is too large for the given data, the integral in the Bayes estimator may diverge. For such a case, offset values for the parameters can be specified not to diverge.

**Value**

vector            a vector of the parameter estimate

**Note**

This routine is not stable and accurate. Dr.Kamatani is now working for improvements.

**Author(s)**

The YUIMA Project Team

**Examples**

```
set.seed(123)

ymodel <- setModel(drift="(-1)*theta2*x", diffusion="sqrt(theta1^2+1)",
                  time.variable="t", state.variable="x", solve.variable="x")
n <- 500
h <- 1/((n)^(2/3))
ysamp <- setSampling(Terminal=(n)^(1/3), n=n)
yuima <- setYuima(model=ymodel, sampling=ysamp)
param.true <- list(theta2=0.3, theta1=0.5)
yuima <- simulate(yuima, xinit=1, true.parameter=param.true)

prior.theta1 <- function(theta2)
  1*(theta2 > 0 & theta2 < 1)

prior.theta2 <- function(theta1)
  1*(theta1 > 0 & theta1 < 1)

prior <- list(theta2=list(measure.type="code",df="dunif(z,0,1)"),
             theta1=list(measure.type="code",df="dunif(z,0,1)"))

param.init <- list(theta2=0.35,theta1=0.52)
```

```

lower = c(0,0)
upper=c(1,1)

bayes1 <- adaBayes(yuima, start=param.init, prior=prior, method="nomcmc")
bayes1@coef

mle1 <- qmle(yuima, start=param.init, lower=list(theta1=0,theta2=0),
            upper=list(theta1=1,theta2=1), method="L-BFGS-B")
mle1@coef

```

---

asymptotic_term	<i>asymptotic expansion of the expected value of the functional</i>
-----------------	---

---

### Description

calculate the first and second term of asymptotic expansion of the functional mean.

### Usage

```
asymptotic_term(yuima, block=100, rho, g, expand.var="e")
```

### Arguments

yuima	an yuima object containing model and functional.
block	the number of trapezoids for integrals.
rho	specify discounting factor in mean integral.
g	arbitrary measurable function for mean integral.
expand.var	default expand.var="e".

### Details

Calculate the first and second term of asymptotic expansion of the expected value of the functional associated with a sde. The returned value  $d0 + \text{epsilon} * d1$  is approximation of the expected value.

### Value

terms	list of 1st and 2nd asymptotic terms, terms\$d0 and terms\$d1.
-------	--

### Note

we need to fix this routine.

### Author(s)

YUIMA Project Team

## Examples

```

# to the Black-Scholes economy:
#  $dX_t^e = X_t^e * dt + e * X_t^e * dW_t$ 
diff.matrix <- "x*e"
model <- setModel(drift = "x", diffusion = diff.matrix)
# call option is evaluated by averating
#  $\max\{ (1/T) * \int_0^T X_t^e dt, 0\}$ , the first argument is the functional of interest:
Terminal <- 1
xinit <- c(1)
f <- list( c(expression(x/Terminal)), c(expression(0)))
F <- 0
division <- 1000
e <- .3
yuima <- setYuima(model = model, sampling = setSampling(Terminal=Terminal, n=division))
yuima <- setFunctional( yuima, f=f,F=F, xinit=xinit,e=e)

# asymptotic expansion
rho <- expression(0)
F0 <- F0(yuima)
get_ge <- function(x,epsilon,K,F0){
  tmp <- (F0 - K) + (epsilon * x)
  tmp[(epsilon * x) < (K-F0)] <- 0
  return( tmp )
}
g <- function(x) get_ge(x,epsilon=e,K=1,F0=F0)
set.seed(123)
asymp <- asymptotic_term(yuima, block=10, rho,g)
asymp
sum(asymp$d0 + e * asymp$d1)

### An example of multivariate case: Heston model
## a <- 1;C <- 1;d <- 10;R<-.1
## diff.matrix <- matrix( c("x1*sqrt(x2)*e", "e*R*sqrt(x2)",0,"sqrt(x2*(1-R^2))*e"), 2,2)
## model <- setModel(drift = c("a*x1", "C*(10-x2)"),
## diffusion = diff.matrix,solve.variable=c("x1", "x2"),state.variable=c("x1", "x2"))
## call option is evaluated by averating
##  $\max\{ (1/T) * \int_0^T X_t^e dt, 0\}$ , the first argument is the functional of interest:
##
## Terminal <- 1
## xinit <- c(1,1)
##
## f <- list( c(expression(0), expression(0)),
## c(expression(0), expression(0)) , c(expression(0), expression(0)) )
## F <- expression(x1,x2)
##
## division <- 1000
## e <- .3
##
## yuima <- setYuima(model = model, sampling = setSampling(Terminal=Terminal, n=division))
## yuima <- setFunctional( yuima, f=f,F=F, xinit=xinit,e=e)
##

```

```
## rho <- expression(x1)
## F0 <- F0(yuima)
## get_ge <- function(x){
##   return( max(x[1],0))
## }
## g <- function(x) get_ge(x)
## set.seed(123)
## asymp <- asymptotic_term(yuima, block=10, rho,g)
## sum(asymp$d0 + e * asymp$d1)
```

---

bns.test	<i>Barndorff-Nielsen and Shephard's Test for the Presence of Jumps Using Bipower Variation</i>
----------	--

---

### Description

Tests the presence of jumps using the statistic proposed in Barndorff-Nielsen and Shephard (2004,2006) for each components.

### Usage

```
bns.test(yuima, r = rep(1, 4), type = "standard", adj = TRUE)
```

### Arguments

yuima	an object of <a href="#">yuima-class</a> or <a href="#">yuima.data-class</a> .
r	a vector of non-negative numbers or a list of vectors of non-negative numbers. Theoretically, it is necessary that $\text{sum}(r)=4$ and $\text{max}(r)<2$ .
type	type of the test statistic to use. standard is default.
adj	logical; if TRUE, the maximum adjustment suggested in Barndorff-Nielsen and Shephard (2004) is applied to the test statistic when type is equal to either "log" or "ratio".

### Details

For the  $i$ -th component, the test statistic is equal to the  $i$ -th component of  $\sqrt{n} * (\text{mpv}(yuima, 2) - \text{mpv}(yuima, c(1, 1))) /$  when type="standard",  $\sqrt{n} * \log(\text{mpv}(yuima, 2) / \text{mpv}(yuima, c(1, 1))) / \sqrt{\text{vartheta} * \text{mpv}(yuima, r) / \text{mpv}(yuima, c(1, 1))}$  when type="log" and  $\sqrt{n} * (1 - \text{mpv}(yuima, c(1, 1)) / \text{mpv}(yuima, 2)) / \sqrt{\text{vartheta} * \text{mpv}(yuima, r) / \text{mpv}(yuima, c(1, 1))}$  when type="ratio". Here,  $n$  is equal to the length of the  $i$ -th component of the zoo.data of yuima minus 1 and  $\text{vartheta}$  is  $\pi^2/4 + \pi - 5$ . When adj=TRUE,  $\text{mpv}(yuima, r)[i] / \text{mpv}(yuima, c(1, 1))^2[i]$  is replaced with 1 if it is less than 1.

**Value**

A list with the same length as the `zoo.data` of `yuima`. Each component of the list has class “`htest`” and contains the following components:

<code>statistic</code>	the value of the test statistic of the corresponding component of the <code>zoo.data</code> of <code>yuima</code> .
<code>p.value</code>	an approximate p-value for the test of the corresponding component.
<code>method</code>	the character string “Barndorff-Nielsen and Shephard jump test”.
<code>data.name</code>	the character string “ <code>xi</code> ”, where <code>i</code> is the number of the component.

**Note**

Theoretically, this test may be invalid if sampling is irregular.

**Author(s)**

The YUIMA Project Team

**References**

Barndorff-Nielsen, O. E. and Shephard, N. (2004) Power and bipower variation with stochastic volatility and jumps, *Journal of Financial Econometrics*, **2**, no. 1, 1–37.

Barndorff-Nielsen, O. E. and Shephard, N. (2006) Econometrics of testing for jumps in financial economics using bipower variation, *Journal of Financial Econometrics*, **4**, no. 1, 1–30.

Huang, X. and Tauchen, G. (2005) The relative contribution of jumps to total price variance, *Journal of Financial Econometrics*, **3**, no. 4, 456–499.

**See Also**

[mpv](#)

**Examples**

```
set.seed(123)

# One-dimensional case
## Model:  $dX_t = t \cdot dW_t + t \cdot dz_t$ ,
## where  $z_t$  is a compound Poisson process with intensity 5 and jump sizes distribution  $N(0, 0.1)$ .

model <- setModel(drift=0, diffusion="t", jump.coeff="t", measure.type="CP",
                 measure=list(intensity=5, df=list("dnorm(z, 0, sqrt(0.1))")),
                 time.variable="t")

yuima.samp <- setSampling(Terminal = 1, n = 390)
yuima <- setYuima(model = model, sampling = yuima.samp)
yuima <- simulate(yuima)
plot(yuima) # The path seems to involve some jumps
```

```

bns.test(yuima) # standard type

bns.test(yuima,type="log") # log type

bns.test(yuima,type="ratio") # ratio type

# Multi-dimensional case
## Model: dXkt=t*dWk_t (k=1,2,3) (no jump case).

diff.matrix <- diag(3)
diag(diff.matrix) <- c("t","t","t")
model <- setModel(drift=c(0,0,0),diffusion=diff.matrix,time.variable="t",
                 solve.variable=c("x1","x2","x3"))

yuima.samp <- setSampling(Terminal = 1, n = 390)
yuima <- setYuima(model = model, sampling = yuima.samp)
yuima <- simulate(yuima)
plot(yuima)

bns.test(yuima)

```

---

carma.info-class

*Class for information about CARMA(p,q) model*


---

## Description

The `carma.info-class` is a class of the **yuima** package.

## Details

The `carma.info-class` object cannot be directly specified by the user but it is constructed when the `yuima.carma-class` object is constructed via `setCarma`.

## Slots

`p`: Number of autoregressive coefficients.

`q`: Number of moving average coefficients.

`loc.par`: Label of location coefficient.

`scale.par`: Label of scale coefficient.

`ar.par`: Label of autoregressive coefficients.

`ma.par`: Label of moving average coefficients.

`lin.par`: Label of linear coefficients.

`Carma.var`: Label of the observed process.

`Latent.var`: Label of the unobserved process.

`XinExpr`: Logical variable. If `XinExpr=FALSE`, the starting condition of `Latent.var` is zero otherwise each component of `Latent.var` has a parameter as a starting point.



**Author(s)**

The YUIMA Project Team

---

CarmaNoise

*Estimation for the underlying Levy in a carma model*

---

**Description**

Retrieve the increment of the underlying Levy for the carma(p,q) process using the approach developed in Brockwell et al.(2011)

**Usage**

```
CarmaNoise(yuima, param, data=NULL, NoNeg.Noise=FALSE)
```

**Arguments**

yuima	a yuima object or an object of <a href="#">yuima.carma-class</a> .
param	list of parameters for the carma.
data	an object of class <a href="#">yuima.data-class</a> contains the observations available at uniformly spaced time. If data=NULL, the default, the 'CarmaNoise' uses the data in an object of <a href="#">yuima.data-class</a> .
NoNeg.Noise	Estimate a non-negative Levy-Driven Carma process. By default NoNeg.Noise=FALSE.

**Value**

incr.Levy	a numeric object contains the estimated increments.
-----------	---

**Note**

The function `qmle` uses the function `CarmaNoise` for estimation of underlying Levy in the carma model.

**Author(s)**

The YUIMA Project Team

**References**

Brockwell, P., Davis, A. R. and Yang. Y. (2011) Estimation for Non-Negative Levy-Driven CARMA Process, *Journal of Business And Economic Statistics*, **29** - 2, 250-259.

**Examples**

```

## Not run:
#Ex.1: Carma(p=3, q=0) process driven by a brownian motion.

mod0<-setCarma(p=3,q=0)

# We fix the autoregressive and moving average parameters
# to ensure the existence of a second order stationary solution for the process.

true.parm0 <-list(a1=4,a2=4.75,a3=1.5,b0=1)

# We simulate a trajectory of the Carma model.

numb.sim<-1000
samp0<-setSampling(Terminal=100,n=numb.sim)
set.seed(100)
incr.W<-matrix(rnorm(n=numb.sim,mean=0,sd=sqrt(100/numb.sim)),1,numb.sim)

sim0<-simulate(mod0,
               true.parameter=true.parm0,
               sampling=samp0, increment.W=incr.W)

#Applying the CarmaNoise

system.time(
  inc.Levy0<-CarmaNoise(sim0,true.parm0)
)

# We compare the original with the estimated noise increments

par(mfrow=c(1,2))
plot(t(incr.W)[1:998],type="l", ylab="",xlab="time")
title(main="True Brownian Motion",font.main="1")
plot(inc.Levy0,type="l", main="Filtered Brownian Motion",font.main="1",ylab="",xlab="time")

# Ex.2: carma(2,1) driven by a compound poisson
# where jump size is normally distributed and
# the lambda is equal to 1.

mod1<-setCarma(p=2,
               q=1,
               measure=list(intensity="Lamb",df=list("dnorm(z, 0, 1)")),
               measure.type="CP")

true.parm1 <-list(a1=1.39631, a2=0.05029,
                 b0=1,b1=2,
                 Lamb=1)

# We generate a sample path.

samp1<-setSampling(Terminal=100,n=200)
set.seed(123)

```

```

sim1<-simulate(mod1,
               true.parameter=true.parm1,
               sampling=samp1)

# We estimate the parameter using qmle.
carmaopt1 <- qmle(sim1, start=true.parm1)
summary(carmaopt1)
# Internally qmle uses CarmaNoise. The result is in
plot(carmaopt1)

# Ex.3: Carma(p=2,q=1) with scale and location parameters
# driven by a Compound Poisson
# with jump size normally distributed.
mod2<-setCarma(p=2,
               q=1,
               loc.par="mu",
               scale.par="sig",
               measure=list(intensity="Lamb",df=list("dnorm(z, 0, 1)")),
               measure.type="CP")

true.parm2 <-list(a1=1.39631,
                 a2=0.05029,
                 b0=1,
                 b1=2,
                 Lamb=1,
                 mu=0.5,
                 sig=0.23)
# We simulate the sample path
set.seed(123)
sim2<-simulate(mod2,
               true.parameter=true.parm2,
               sampling=samp1)

# We estimate the Carma and we plot the underlying noise.

carmaopt2 <- qmle(sim2, start=true.parm2)
summary(carmaopt2)

# Increments estimated by CarmaNoise
plot(carmaopt2)

## End(Not run)

```

## Description

This function estimates the covariance between two Ito processes when they are observed at discrete times possibly nonsynchronously. It can apply to irregularly sampled one-dimensional data as a special case.

**Usage**

```
cce(x, method="HY", theta, kn, g=function(x)min(x,1-x), refreshing = TRUE,
    cwise = TRUE, delta = 0, adj = TRUE, K, c.two, J = 1, c.multi, kernel, H,
    c.RK, eta = 3/5, m = 2, ftregion = 0, opt.method = "BFGS", vol.init = NA,
    covol.init = NA, nvar.init = NA, ncov.init = NA, ..., mn, alpha = 0.4,
    frequency = 300, avg = TRUE, threshold, utime, psd = FALSE)
```

**Arguments**

x	an object of <a href="#">yuima-class</a> or <a href="#">yuima.data-class</a> .
method	the method to be used. See ‘Details’.
theta	a numeric vector or matrix. If it is a matrix, each of its components indicates the tuning parameter which determines the pre-averaging window lengths $kn$ to be used for estimating the corresponding component. If it is a numeric vector, it is converted to a matrix as $(C+t(C))/2$ , where $C=matrix(theta,d,d)$ and $d=dim(x)$ . The default value is 0.15 for the method "PHY" or "PTHY" following Christensen et al. (2011), while it is 1 for the method "MRC" following Christensen et al. (2010).
kn	an integer-valued vector or matrix indicating the pre-averaging window length(s). For the methods "PHY" or "PTHY", see ‘Details’ for the default value. For the method "MRC", the default value is $ceiling(theta*n^{(1+delta)})$ , where $n$ is the number of the refresh times associated with the data minus 1.
g	a function indicating the weight function to be used. The default value is the Bartlett window: $function(x)min(x,1-x)$ .
refreshing	logical. If TRUE, the data is pre-synchronized by the next-tick interpolation in the refresh times.
cwise	logical. If TRUE, the estimator is calculated componentwise.
delta	a non-negative number indicating the order of the pre-averaging window length(s) $kn$ .
adj	logical. If TRUE, a finite-sample adjustment is performed. For the method "MRC", see Christensen et al. (2010) for details. For the method "TSCV", see Zhang (2011) and Zhang et al. (2005) for details.
K	a positive integer indicating the large time-scale parameter. The default value is $ceiling(c.two*n^{(2/3)})$ , where $n$ is the number of the refresh times associated with the data minus 1.
c.two	a positive number indicating the tuning parameter which determines the scale of the large time-scale parameter $K$ . The default value is the average of the numeric vector each of whose components is the roughly estimated optimal value in the sense of the minimizer of the theoretical asymptotic variance of the estimator of the corresponding diagonal component. The theoretical asymptotic variance is considered in the standard case and given in Zhang et al. (2005).
J	a positive integer indicating the small time-scale parameter.
c.multi	a numeric vector or matrix. If it is a matrix, each of its components indicates the tuning parameter which determines (the scale of) the number of the time scales to be used for estimating the corresponding component. If it is a numeric vector,

it is converted to a matrix as  $(C+t(C))/2$ , where  $C=\text{matrix}(c.\text{multi},d,d)$  and  $d=\text{dim}(x)$ . The default value is the numeric vector each of whose components is the roughly estimated optimal value in the sense of minimizing the theoretical asymptotic variance of the estimator of the corresponding diagonal component. The theoretical asymptotic variance is considered in the standard case and given in Bibinger et al. (2012).

kernel	a function indicating the kernel function to be used. The default value is the Parzan kernel, which is recommended in Barndorff-Nielsen et al. (2009, 2011).
H	a positive number indicating the bandwidth parameter. The default value is $c.RK \times n^{\eta}$ , where $n$ is the number of the refresh times associated with the data minus 1.
c.RK	a positive number indicating the tuning parameter which determines the scale of the bandwidth parameter $H$ . The default value is the average of the numeric vector each of whose components is the roughly estimated optimal value in the sense of minimizing the theoretical asymptotic variance of the estimator of the corresponding diagonal component. The theoretical asymptotic variance is considered in the standard case and given in Barndorff-Nielsen et al. (2009, 2011).
eta	a positive number indicating the tuning parameter which determines the order of the bandwidth parameter $H$ .
m	a positive integer indicating the number of the end points to be jittered.
ftregion	a non-negative number indicating the length of the flat-top region. <code>ftregion=0</code> (the default) means that a non-flat-top realized kernel studied in Barndorff-Nielsen et al. (2011) is used. <code>ftregion=1/H</code> means that a flat-top realized kernel studied in Barndorff-Nielsen et al. (2008) is used. See Varneskov (2011) for other values.
opt.method	passed to the argument <code>method</code> of <code>constrOptim</code> .
vol.init	a numeric vector each of whose components indicates the initial value to be used to estimate the integrated volatility of the corresponding component, which is passed to the optimizer. Components involving NA are filled with the rough estimated true values.
covol.init	a numeric matrix each of whose columns indicates the initial value to be used to estimate the integrated covariance of the corresponding component, which is passed to the optimizer. Components involving NA are filled with the rough estimated true values.
nvar.init	a numeric vector each of whose components indicates the initial value to be used to estimate the variance of noise of the corresponding component, which is passed to the optimizer. Components involving NA are filled with the rough estimated true values.
ncov.init	a numeric matrix each of whose columns indicates the initial value to be used to estimate the covariance of noise of the corresponding component, which is passed to the optimizer. Components involving NA are filled with the rough estimated true values.
...	other named arguments to be passed to <code>constrOptim</code> .
mn	a positive integer indicating the number of terms to be used for calculating the SIML estimator. The default value is $\text{ceiling}(n^{\alpha})$ , where $n$ is the number of the refresh times associated with the data minus 1.

alpha	a positive number indicating the order of mn.
frequency	a positive integer indicating the frequency (seconds) of the calendar time sampling to be used.
avg	logical. If TRUE, the averaged subsampling estimator is calculated. Otherwise the simple sparsely subsampled estimator is calculated.
threshold	a numeric vector or list indicating the threshold parameter(s). Each of its components indicates the threshold parameter or process to be used for estimating the corresponding component. If it is a numeric vector, the elements in threshold are recycled if there are two few elements in threshold. The default value is determined following Koike (2013a) (for the method "THY") and Koike (2013b) (for the method "PTHY").
utime	a positive number indicating what seconds the unit time means. The default value is 23400 (this means 6.5 hours) if the time indices of the (first component) of x is numeric, otherwise 1.
psd	logical. If TRUE, the estimated covariance matrix C is converted to $(C\%*\%C)^{(1/2)}$ for ensuring the positive semi-definiteness.

## Details

This function is a method for objects of [yuima.data-class](#) and [yuima-class](#). It extracts the data slot when applied to a an object of [yuima-class](#).

Typical usages are

```

cce(x,psd=FALSE)
cce(x,method="PHY",theta,kn,g,refreshing=TRUE,cwise=TRUE,psd=FALSE)
cce(x,method="MRC",theta,kn,g,delta=0,avg=TRUE,psd=FALSE)
cce(x,method="TSCV",K,c.two,J=1,adj=TRUE,utime,psd=FALSE)
cce(x,method="GME",c.multi,utime,psd=FALSE)
cce(x,method="RK",kernel,H,c.RK,eta=3/5,m=2,ftregion=0,utime,psd=FALSE)
cce(x,method="QMLE",opt.method="BFGS",vol.init=NULL,covol.init=NULL,
  nvar.init=NULL,ncov.init=NULL,...,utime,psd=FALSE)
cce(x,method="SIML",mn,alpha=0.4,psd=FALSE)
cce(x,method="THY",threshold,psd=FALSE)
cce(x,method="PTHY",theta,kn,g,threshold,refreshing=TRUE,cwise=TRUE,psd=FALSE)
cce(x,method="SRC",frequency=300,avg=TRUE,utime,psd=FALSE)
cce(x,method="SBPC",frequency=300,avg=TRUE,utime,psd=FALSE)

```

The default method is method "HY", which is an implementation of the Hayashi-Yoshida estimator proposed in Hayashi and Yoshida (2005).

Method "PHY" is an implementation of the Pre-averaged Hayashi-Yoshida estimator proposed in Christensen et al. (2010).

Method "MRC" is an implementation of the Modulated Realized Covariance based on refresh time sampling proposed in Christensen et al. (2010).

Method "TSCV" is an implementation of the previous tick Two Scales realized CoVariance based on

refresh time sampling proposed in Zhang (2011).

Method "GME" is an implementation of the Generalized Multiscale Estimator proposed in Bibinger (2011).

Method "RK" is an implementation of the multivariate Realized Kernel based on refresh time sampling proposed in Barndorff-Nielsen et al. (2011).

Method "QMLE" is an implementation of the nonparametric Quasi Maximum Likelihood Estimator proposed in Ait-Sahalia et al. (2010).

Method "SIML" is an implementation of the Separating Information Maximum Likelihood estimator proposed in Kunitomo and Sato (2008) with the basis of refresh time sampling.

Method "THY" is an implementation of the Truncated Hayashi-Yoshida estimator proposed in Mancini and Gobbi (2012).

Method "PTHY" is an implementation of the Pre-averaged Truncated Hayashi-Yoshida estimator, which is a thresholding version of the pre-averaged Hayashi-Yoshida estimator.

Method "SRC" is an implementation of the calendar time Subsampled Realized Covariance.

Method "SBPC" is an implementation of the calendar time Subsampled realized BiPower Covariance.

The rough estimation procedures for selecting the default values of the tuning parameters are based on those in Barndorff-Nielsen et al. (2009).

For the methods "PHY" or "PTHY", the default value of  $kn$  changes depending on the values of refreshing and *cwise*. If both refreshing and *cwise* are TRUE (the default), the default value of  $kn$  is given by the matrix  $\text{ceiling}(\text{theta} * N)$ , where  $N$  is a matrix whose diagonal components are identical with the vector  $\text{length}(x) - 1$  and whose  $(i, j)$ -th component is identical with the number of the refresh times associated with  $i$ -th and  $j$ -th components of  $x$  minus 1. If refreshing is TRUE while *cwise* is FALSE, the default value of  $kn$  is given by  $\text{ceiling}(\text{mean}(\text{theta}) * \text{sqrt}(n))$ , where  $n$  is the number of the refresh times associated with the data minus 1. If refreshing is FALSE while *cwise* is TRUE, the default value of  $kn$  is given by the matrix  $\text{ceiling}(\text{theta} * N_0)$ , where  $N_0$  is a matrix whose diagonal components are identical with the vector  $\text{length}(x) - 1$  and whose  $(i, j)$ -th component is identical with  $(\text{length}(x)[i] - 1) + (\text{length}(x)[j] - 1)$ . If both refreshing and *cwise* are FALSE, the default value of  $kn$  is given by  $\text{ceiling}(\text{mean}(\text{theta}) * \text{sqrt}(\text{sum}(\text{length}(x) - 1)))$  (following Christensen et al. (2011)).

## Value

A list with components:

covmat	the estimated covariance matrix
cormat	the estimated correlation matrix

**Note**

The example shows the central limit theorem for the nonsynchronous covariance estimator. Estimation of the asymptotic variance with p-values and the second-order correction will be provided in a future version of the package.

**Author(s)**

The YUIMA Project Team

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## See Also

[setModel](#)

## Examples

```
## Set a model
diff.coef.1 <- function(t, x1 = 0, x2 = 0) sqrt(1+t)
diff.coef.2 <- function(t, x1 = 0, x2 = 0) sqrt(1+t^2)
cor.rho <- function(t, x1 = 0, x2 = 0) sqrt(1/2)
diff.coef.matrix <- matrix(c("diff.coef.1(t,x1,x2)",
"diff.coef.2(t,x1,x2) * cor.rho(t,x1,x2)",
"", "diff.coef.2(t,x1,x2) * sqrt(1-cor.rho(t,x1,x2)^2)"), 2, 2)
cor.mod <- setModel(drift = c("", ""),
diffusion = diff.coef.matrix,solve.variable = c("x1", "x2"))

set.seed(111)

## We use a function poisson.random.sampling to get observation by Poisson sampling.
yuima.samp <- setSampling(Terminal = 1, n = 1200)
yuima <- setYuima(model = cor.mod, sampling = yuima.samp)
yuima <- simulate(yuima)
psample<- poisson.random.sampling(yuima, rate = c(0.2,0.3), n = 1000)

## cce takes the psample and returns an estimate of the quadratic covariation.
cce(psample)$covmat[1, 2]
##cce(psample)[1, 2]

## True value of the quadratic covariation.
cc.theta <- function(T, sigma1, sigma2, rho) {
  tmp <- function(t) return(sigma1(t) * sigma2(t) * rho(t))
  integrate(tmp, 0, T)
}

theta <- cc.theta(T = 1, diff.coef.1, diff.coef.2, cor.rho)$value
cat(sprintf("theta =%.5f\n", theta))

names(psample@zoo.data)
```

```

# Example. A stochastic differential equation with nonlinear feedback.

## Set a model
drift.coef.1 <- function(x1,x2) x2
drift.coef.2 <- function(x1,x2) -x1
drift.coef.vector <- c("drift.coef.1","drift.coef.2")
diff.coef.1 <- function(t,x1,x2) sqrt(abs(x1))*sqrt(1+t)
diff.coef.2 <- function(t,x1,x2) sqrt(abs(x2))
cor.rho <- function(t,x1,x2) 1/(1+x1^2)
diff.coef.matrix <- matrix(c("diff.coef.1(t,x1,x2)",
"diff.coef.2(t,x1,x2) * cor.rho(t,x1,x2)", "",
"diff.coef.2(t,x1,x2) * sqrt(1-cor.rho(t,x1,x2)^2)"), 2, 2)
cor.mod <- setModel(drift = drift.coef.vector,
diffusion = diff.coef.matrix,solve.variable = c("x1", "x2"))

## Generate a path of the process
set.seed(111)
yuima.samp <- setSampling(Terminal = 1, n = 10000)
yuima <- setYuima(model = cor.mod, sampling = yuima.samp)
yuima <- simulate(yuima, xinit=c(2,3))
plot(yuima)

## The "true" value of the quadratic covariation.
cce(yuima)

## We use the function poisson.random.sampling to generate nonsynchronous
## observations by Poisson sampling.
psample<- poisson.random.sampling(yuima, rate = c(0.2,0.3), n = 3000)

## cce takes the psample to return an estimated value of the quadratic covariation.
## The off-diagonal elements are the value of the Hayashi-Yoshida estimator.
cce(psample)

```

## Description

Volatility structural change point estimator

**Usage**

```
CPoint(yuima, param1, param2, print=FALSE, symmetrized=FALSE, plot=FALSE)
qmleL(yuima, t, ...)
qmleR(yuima, t, ...)
```

**Arguments**

yuima	a yuima object.
param1	parameter values before the change point t
param2	parameter values after the change point t
plot	plot test statistics? Default is FALSE.
print	print some debug output. Default is FALSE.
t	time value. See Details.
symmetrized	if TRUE uses the symmetrized version of the quasi maximum-likelihood approximation.
...	passed to <a href="#">qmle</a> method. See Examples.

**Details**

CPoint estimates the change point using quasi-maximum likelihood approach.

Function qmleL estimates the parameters in the diffusion matrix using observations up to time t.

Function qmleR estimates the parameters in the diffusion matrix using observations from time t to the end.

Arguments in both qmleL and qmleR follow the same rules as in [qmle](#).

**Value**

ans a list with change point instant, and paramters before and after the change point.

**Author(s)**

The YUIMA Project Team

**Examples**

```
## Not run:
diff.matrix <- matrix(c("theta1.1*x1", "0*x2", "0*x1", "theta1.2*x2"), 2, 2)

drift.c <- c("1-x1", "3-x2")
drift.matrix <- matrix(drift.c, 2, 1)

ymodel <- setModel(drift=drift.matrix, diffusion=diff.matrix, time.variable="t",
state.variable=c("x1", "x2"), solve.variable=c("x1", "x2"))
n <- 1000

set.seed(123)
```

```

t1 <- list(theta1.1=.1, theta1.2=0.2)
t2 <- list(theta1.1=.6, theta1.2=.6)

tau <- 0.4
ysamp1 <- setSampling(n=tau*n, Initial=0, delta=0.01)
yuima1 <- setYuima(model=ymodel, sampling=ysamp1)
yuima1 <- simulate(yuima1, xinit=c(1, 1), true.parameter=t1)

x1 <- yuima1@data@zoo.data[[1]]
x1 <- as.numeric(x1[length(x1)])
x2 <- yuima1@data@zoo.data[[2]]
x2 <- as.numeric(x2[length(x2)])

ysamp2 <- setSampling(Initial=n*tau*0.01, n=n*(1-tau), delta=0.01)
yuima2 <- setYuima(model=ymodel, sampling=ysamp2)

yuima2 <- simulate(yuima2, xinit=c(x1, x2), true.parameter=t2)

yuima <- yuima1
yuima@data@zoo.data[[1]] <- c(yuima1@data@zoo.data[[1]], yuima2@data@zoo.data[[1]][-1])
yuima@data@zoo.data[[2]] <- c(yuima1@data@zoo.data[[2]], yuima2@data@zoo.data[[2]][-1])

plot(yuima)

# estimation of change point for given parameter values
t.est <- CPoint(yuima,param1=t1,param2=t2, plot=TRUE)

low <- list(theta1.1=0, theta1.2=0)

# first state estimate of parameters using small
# portion of data in the tails
tmp1 <- qmleL(yuima,start=list(theta1.1=0.3,theta1.2=0.5),t=1.5,
             lower=low, method="L-BFGS-B")
tmp1
tmp2 <- qmleR(yuima,start=list(theta1.1=0.3,theta1.2=0.5), t=8.5,
             lower=low, method="L-BFGS-B")
tmp2

# first stage changepoint estimator
t.est2 <- CPoint(yuima,param1=coef(tmp1),param2=coef(tmp2))
t.est2$tau

# second stage estimation of parameters given first stage
# change point estimator
tmp11 <- qmleL(yuima,start=as.list(coef(tmp1)), t=t.est2$tau-0.1,
             lower=low, method="L-BFGS-B")
tmp11
tmp21 <- qmleR(yuima,start=as.list(coef(tmp2)), t=t.est2$tau+0.1,

```

```

    lower=low, method="L-BFGS-B")
tmp21

# second stage estimator of the change point
CPoint(yuima,param1=coef(tmp11),param2=coef(tmp21))

## One dimensional example: non linear case
diff.matrix <- matrix("(1+x1^2)^theta1", 1, 1)
drift.c <- c("x1")

ymodel <- setModel(drift=drift.c, diffusion=diff.matrix, time.variable="t",
state.variable=c("x1"), solve.variable=c("x1"))
n <- 500

set.seed(123)

y0 <- 5 # initial value
theta00 <- 1/5
gamma <- 1/4

theta01 <- theta00+n^(-gamma)

t1 <- list(theta1= theta00)
t2 <- list(theta1= theta01)

tau <- 0.4
ysamp1 <- setSampling(n=tau*n, Initial=0, delta=1/n)
yuima1 <- setYuima(model=ymodel, sampling=ysamp1)
yuima1 <- simulate(yuima1, xinit=c(5), true.parameter=t1)
x1 <- yuima1@data@zoo.data[[1]]
x1 <- as.numeric(x1[length(x1)])

ysamp2 <- setSampling(Initial=tau, n=n*(1-tau), delta=1/n)
yuima2 <- setYuima(model=ymodel, sampling=ysamp2)

yuima2 <- simulate(yuima2, xinit=c(x1), true.parameter=t2)

yuima <- yuima1
yuima@data@zoo.data[[1]] <- c(yuima1@data@zoo.data[[1]], yuima2@data@zoo.data[[1]][-1])

plot(yuima)

t.est <- CPoint(yuima,param1=t1,param2=t2)
t.est$tau

low <- list(theta1=0)
upp <- list(theta1=1)

```

```

# first state estimate of parameters using small
# portion of data in the tails
tmp1 <- qmleL(yuima,start=list(theta1=0.5),t=.15,lower=low, upper=upp,method="L-BFGS-B")
tmp1
tmp2 <- qmleR(yuima,start=list(theta1=0.5), t=.85,lower=low, upper=upp,method="L-BFGS-B")
tmp2

# first stage changepoint estimator
t.est2 <- CPoint(yuima,param1=coef(tmp1),param2=coef(tmp2))
t.est2$tau

# second stage estimation of parameters given first stage
# change point estimator
tmp11 <- qmleL(yuima,start=as.list(coef(tmp1)), t=t.est2$tau-0.1,
  lower=low, upper=upp,method="L-BFGS-B")
tmp11

tmp21 <- qmleR(yuima,start=as.list(coef(tmp2)), t=t.est2$tau+0.1,
  lower=low, upper=upp,method="L-BFGS-B")
tmp21

# second stage estimator of the change point
CPoint(yuima,param1=coef(tmp11),param2=coef(tmp21),plot=TRUE)

## End(Not run)

```

---

lasso

*Adaptive LASSO estimation for stochastic differential equations*


---

## Description

Adaptive LASSO estimation for stochastic differential equations.

## Usage

```
lasso(yuima, lambda0, start, delta=1, ...)
```

## Arguments

yuima	a yuima object.
lambda0	a named list with penalty for each parameter.
start	initial values to be passed to the optimizer.
delta	controls the amount of shrinking in the adaptive sequences.
...	passed to <code>optim</code> method. See Examples.

## Details

lasso behaves more likely the standard `qml` function in and argument `method` is one of the methods available in `optim`.

From initial guess of QML estimates, performs adaptive LASSO estimation using the Least Squares Approximation (LSA) as in Wang and Leng (2007, JASA).

## Value

`ans` a list with both QMLE and LASSO estimates.

## Author(s)

The YUIMA Project Team

## Examples

```
##multidimension case
diff.matrix <- matrix(c("theta1.1","theta1.2", "1", "1"), 2, 2)

drift.c <- c("-theta2.1*x1", "-theta2.2*x2", "-theta2.2", "-theta2.1")
drift.matrix <- matrix(drift.c, 2, 2)

ymodel <- setModel(drift=drift.matrix, diffusion=diff.matrix, time.variable="t",
                  state.variable=c("x1", "x2"), solve.variable=c("x1", "x2"))
n <- 100
ysamp <- setSampling(Terminal=(n)^(1/3), n=n)
yuima <- setYuima(model=ymodel, sampling=ysamp)
set.seed(123)

truep <- list(theta1.1=0.6, theta1.2=0,theta2.1=0.5, theta2.2=0)
yuima <- simulate(yuima, xinit=c(1, 1),
                 true.parameter=truep)

est <- lasso(yuima, start=list(theta2.1=0.8, theta2.2=0.2, theta1.1=0.7, theta1.2=0.1),
            lower=list(theta1.1=1e-10,theta1.2=1e-10,theta2.1=.1,theta2.2=1e-10),
            upper=list(theta1.1=4,theta1.2=4,theta2.1=4,theta2.2=4), method="L-BFGS-B")

# TRUE
unlist(truep)

# QMLE
round(est$mle,3)

# LASSO
round(est$lasso,3)
```

---

limiting.gamma	<i>calculate the value of limiting covariance matrices : Gamma</i>
----------------	--

---

**Description**

To confirm assymptotic normality of theta estimators.

**Usage**

```
limiting.gamma(obj, theta, verbose=FALSE)
```

**Arguments**

obj	an yuima or yuima.model object.
theta	true theta
verbose	an option for display a verbose process.

**Details**

Calculate the value of limiting covariance matrices Gamma. The returned values gamma1 and gamma2 are used to confirm assymptotic normality of theta estimators. this program is limited to 1-dimension-sde model for now.

**Value**

gamma1	a theoretical figure for variance of theta1 estimator
gamma2	a theoretical figure for variance of theta2 estimator

**Note**

we need to fix this routine.

**Author(s)**

The YUIMA Project Team

**Examples**

```
set.seed(123)

## Yuima
diff.matrix <- matrix(c("theta1"), 1, 1)
myModel <- setModel(drift=c("(-1)*theta2*x"), diffusion=diff.matrix,
time.variable="t", state.variable="x")
n <- 100
mySampling <- setSampling(Terminal=(n)^(1/3), n=n)
myYuima <- setYuima(model=myModel, sampling=mySampling)
```



```

myYuima <- simulate(myYuima, xinit=1, true.parameter=list(theta1=0.6, theta2=0.3))

## theoretical figure of theta
theta1 <- 3.5
theta2 <- 1.3

theta <- list(theta1, theta2)
lim.gamma <- limiting.gamma(obj=myYuima, theta=theta, verbose=TRUE)

## return theta1 and theta2 with list
lim.gamma$list

## return theta1 and theta2 with vector
lim.gamma$vec

```

---

llag

*Lead Lag Estimator*


---

### Description

Estimate the lead-lag parameters of discretely observed processes by maximizing the shifted Hayashi-Yoshida covariation contrast functions, following Hoffmann et al. (2013).

### Usage

```

llag(x, from=-Inf, to=Inf, division=FALSE, verbose=FALSE, grid, psd=TRUE,
     plot=FALSE, ccor=FALSE)

```

### Arguments

x	an object of <a href="#">yuima-class</a> or <a href="#">yuima.data-class</a> .
verbose	whether llag returns matrices or not.
from	a numeric vector each of whose component(s) indicates the lower end of a finite grid on which the contrast function is evaluated, if grid is missing.
to	a numeric vector each of whose component(s) indicates the upper end of a finite grid on which the contrast function is evaluated, if grid is missing.
division	a numeric vector each of whose component(s) indicates the number of the points of a finite grid on which the contrast function is evaluated, if grid is missing.
grid	a numeric vector or a list of numeric vectors. See ‘Details’.
psd	logical. If TRUE, the estimated cross-correlation functions are converted to the interval [-1,1]. See ‘Details’.
plot	logical. If TRUE, the estimated cross-correlation functions are plotted.
ccor	logical. If TRUE, the estimated cross-correlation functions are returned. This argument is ignored if verbose is FALSE.

## Details

Let  $d$  be the number of the components of the `zoo.data` of the object `x`.

Let  $X_{i_{t_{i_0}}}, X_{i_{t_{i_1}}}, \dots, X_{i_{t_{i_n}(i)}}$  be the observation data of the  $i$ -th component (i.e. the  $i$ -th component of the `zoo.data` of the object `x`).

The shifted Hayashi-Yoshida covariation contrast function  $U_{ij}(\theta)$  of the observations  $X_i$  and  $X_j$  ( $i < j$ ) is defined by the same way as in Hoffmann et al. (2013), which corresponds to their cross-covariance function. The lead-lag parameter  $\theta_{ij}$  is defined as a maximizer of  $|U_{ij}(\theta)|$ .  $U_{ij}(\theta)$  is evaluated on a finite grid  $G_{ij}$  defined below. Thus  $\theta_{ij}$  belongs to this grid. If there exist more than two maximizers, the lowest one is selected.

If `psd` is TRUE, For any  $i, j$  the matrix  $C := (U_{kl}(\theta))_{k,l \in i,j}$  is converted to  $(C \%* \% C)^{(1/2)}$  for ensuring the positive semi-definiteness, and  $U_{ij}(\theta)$  is redefined as the  $(1, 2)$ -component of the converted  $C$ . Here,  $U_{kk}(\theta)$  is set to the realized volatility of  $X_k$ . In this case  $\theta_{ij}$  is given as a maximizer of the cross-correlation functions.

The grid  $G_{ij}$  is defined as follows. First, if `grid` is missing,  $G_{ij}$  is given by

$$a, a + (b - a)/(N - 1), \dots, a + (N - 2)(b - a)/(N - 1), b,$$

where  $a, b$  and  $N$  are the  $(d(i - 1) - (i - 1)i/2 + (j - i))$ -th components of `from`, `to` and `division` respectively. If the corresponding component of `from` (resp. `to`) is `-Inf` (resp. `Inf`),  $a = -(t_{j_n}(j) - t_{i_0})$  (resp.  $b = t_{i_n}(i) - t_{j_0}$ ) is used, while if the corresponding component of `division` is FALSE,  $N = \text{round}(2 \max(n(i), n(j))) + 1$  is used. Missing components are filled with `-Inf` (resp. `Inf`, FALSE). The default value `-Inf` (resp. `Inf`, FALSE) means that all components are `-Inf` (resp. `Inf`, FALSE). Next, if `grid` is a numeric vector,  $G_{ij}$  is given by `grid`. If `grid` is a list of numeric vectors,  $G_{ij}$  is given by the  $(d(i - 1) - (i - 1)i/2 + (j - i))$ -th component of `grid`.

The estimated lead-lag parameters are returned as the skew-symmetric matrix  $(\theta_{ij})_{i,j=1,\dots,d}$ . If `verbose` is TRUE, the covariance matrix  $(U_{ij}(\theta_{ij}))_{i,j=1,\dots,d}$  corresponding to the estimated lead-lag parameters, the corresponding correlation matrix and the computed contrast functions are also returned. If further `ccor` is TRUE, the computed cross-correlation functions are returned as a list with the length  $d(d - 1)/2$ . For  $i < j$ , the  $(d(i - 1) - (i - 1)i/2 + (j - i))$ -th component of the list consists of an object  $U_{ij}(\theta)/\text{sqr}t(U_{ii}(\theta) * U_{jj}(\theta))$  of class `zoo` indexed by  $G_{ij}$ .

If `plot` is TRUE, the computed cross-correlation functions are plotted sequentially.

## Value

If `verbose` is FALSE, a skew-symmetric matrix corresponding to the estimated lead-lag parameters is returned. If `verbose` is TRUE, a list with the following components is returned:

<code>lagcce</code>	a skew-symmetric matrix corresponding to the estimated lead-lag parameters.
<code>covmat</code>	a covariance matrix corresponding to the estimated lead-lag parameters.
<code>cormat</code>	a correlation matrix corresponding to the estimated lead-lag parameters.

If further `ccor` is TRUE, the following component is added to the returned list:

<code>ccor</code>	a list of computed cross-correlation functions.
-------------------	---

## Author(s)

The YUIMA Project Team

## References

Hoffmann, M., Rosenbaum, M. and Yoshida, N. (2013) Estimation of the lead-lag parameter from non-synchronous data, *Bernoulli*, **19**, no. 2, 426–461.

## See Also

[cce](#)

## Examples

```
## Set a model
diff.coef.matrix <- matrix(c("sqrt(x1)", "3/5*sqrt(x2)",
  "1/3*sqrt(x3)", "", "4/5*sqrt(x2)", "2/3*sqrt(x3)",
  "", "", "2/3*sqrt(x3)"), 3, 3)
drift <- c("1-x1", "2*(10-x2)", "3*(4-x3)")
cor.mod <- setModel(drift = drift,
  diffusion = diff.coef.matrix,
  solve.variable = c("x1", "x2", "x3"))

set.seed(111)

## We use a function poisson.random.sampling
# to get observation by Poisson sampling.
yuima.samp <- setSampling(Terminal = 1, n = 1200)
yuima <- setYuima(model = cor.mod, sampling = yuima.samp)
yuima <- simulate(yuima, xinit=c(1,7,5))

# intentionally displace the second time series

data2 <- yuima@data@zoo.data[[2]]
time2 <- time(data2)
theta2 <- 0.05 # the lag of x2 behind x1
stime2 <- time2 + theta2
time(yuima@data@zoo.data[[2]]) <- stime2

data3 <- yuima@data@zoo.data[[3]]
time3 <- time(data3)
theta3 <- 0.12 # the lag of x3 behind x1
stime3 <- time3 + theta3
time(yuima@data@zoo.data[[3]]) <- stime3

#sampled data by Poisson rules
psample<- poisson.random.sampling(yuima,
  rate = c(0.2,0.3,0.4), n = 1000)

# plot
plot(psample)
```

```

#cce
cce(psample)

#lead-lag estimation (with cross-correlation plots)
par(mfcol=c(3,1))
result <- llag(psample,verbose=TRUE,plot=TRUE)

#estimated lead-lag parameter
result$lagcce

```

---

mmfrac

*mmfrac*


---

### Description

Estimates the drift of a fractional Ornstein-Uhlenbeck and, if necessary, also the Hurst and diffusion parameters.

### Usage

```
mmfrac(yuima, ...)
```

### Arguments

yuima	a yuima object.
...	arguments passed to <a href="#">qgv</a> .

### Details

Estimates the drift of s fractional Ornstein-Uhlenbeck and, if necessary, also the Hurst and diffusion parameters.

### Value

an object of class mmfrac

### Author(s)

The YUIMA Project Team

### References

Brouste, A., Iacus, S.M. (2013) Parameter estimation for the discretely observed fractional Ornstein-Uhlenbeck process and the Yuima R package, *Computational Statistics*, pp. 1129–1147.

**See Also**

See also [qgv](#).

**Examples**

```
# Estimating all Hurst parameter, diffusion coefficient and drift coefficient
# in fractional Ornstein-Uhlenbeck

model<-setModel(drift="-x*lambda",hurst=NA,diffusion="theta")
sampling<-setSampling(T=100,n=10000)
yui1<-simulate(model,true.param=list(theta=1,lambda=4),hurst=0.7,sampling=sampling)
mmfrac(yui1)
```

---

model.parameter-class *Class for the parameter description of stochastic differential equations*

---

**Description**

The `model.parameter-class` is a class of the **yuima** package.

**Details**

The `model.parameter-class` object cannot be directly specified by the user but it is constructed when the `yuima.model-class` object is constructed via `setModel`. All the terms which are not in the list of *solution*, *state*, *time*, *jump* variables are considered as parameters. These parameters are identified in the different components of the model (drift, diffusion and jump part). This information is later used to draw inference jointly or separately for the different parameters depending on the model in hands.

**Slots**

**drift:** A vector of names belonging to the drift coefficient.  
**diffusion:** A vector of names of parameters belonging to the diffusion coefficient.  
**jump:** A vector of names of parameters belonging to the jump coefficient.  
**measure:** A vector of names of parameters belonging to the Levy measure.  
**xinit:** A vector of names of parameters belonging to the initial condition.  
**all:** A vector of names of all the parameters found in the components of the model.  
**common:** A vector of names of the parameters in common among drift, diffusion, jump and measure term.

**Author(s)**

The YUIMA Project Team

mpv

*Realized Multipower Variation***Description**

The function returns the realized MultiPower Variation (mpv), defined in Barndorff-Nielsen and Shephard (2004), for each components.

**Usage**

```
mpv(yuima, r = 2, normalize = TRUE)
```

**Arguments**

`yuima` an object of [yuima-class](#) or [yuima.data-class](#).  
`r` a vector of non-negative numbers or a list of vectors of non-negative numbers.  
`normalize` logical. See ‘Details’.

**Details**

Let  $d$  be the number of the components of the `zoo.data` of `yuima`.

Let  $X_{t_0}^i, X_{t_1}^i, \dots, X_{t_n}^i$  be the observation data of the  $i$ -th component (i.e. the  $i$ -th component of the `zoo.data` of `yuima`).

When  $r$  is a  $k$ -dimensional vector of non-negative numbers, `mpv(yuima,r,normalize=TRUE)` is defined as the  $d$ -dimensional vector with  $i$ -th element equal to

$$\mu_{r[1]}^{-1} \cdots \mu_{r[k]}^{-1} n^{\frac{r[1]+\dots+r[k]}{2}-1} \sum_{j=1}^{n-k+1} |\Delta X_{t_j}^i|^{r[1]} |\Delta X_{t_{j+1}}^i|^{r[2]} \cdots |\Delta X_{t_{j+k-1}}^i|^{r[k]},$$

where  $\mu_p$  is the  $p$ -th absolute moment of the standard normal distribution and  $\Delta X_{t_j}^i = X_{t_j}^i - X_{t_{j-1}}^i$ . If `normalize` is `FALSE` the result is not multiplied by  $\mu_{r[1]}^{-1} \cdots \mu_{r[k]}^{-1}$ .

When  $r$  is a list of vectors of non-negative numbers, `mpv(yuima,r,normalize=FALSE)` is defined as the  $d$ -dimensional vector with  $i$ -th element equal to

$$\mu_{r_1^i}^{-1} \cdots \mu_{r_{k_i}^i}^{-1} n^{\frac{r_1^i+\dots+r_{k_i}^i}{2}-1} \sum_{j=1}^{n-k_i+1} |\Delta X_{t_j}^i|^{r_1^i} |\Delta X_{t_{j+1}}^i|^{r_2^i} \cdots |\Delta X_{t_{j+k_i-1}}^i|^{r_{k_i}^i},$$

where  $r_1^i, \dots, r_{k_i}^i$  is the  $i$ -th component of  $r$ . If `normalize` is `FALSE` the result is not multiplied by  $\mu_{r_1^i}^{-1} \cdots \mu_{r_{k_i}^i}^{-1}$ .

**Value**

A numeric vector with the same length as the `zoo.data` of `yuima`

**Author(s)**

The YUIMA Project Team

**References**

Barndorff-Nielsen, O. E. and Shephard, N. (2004) Power and bipower variation with stochastic volatility and jumps, *Journal of Financial Econometrics*, **2**, no. 1, 1–37.

Barndorff-Nielsen, O. E. , Graversen, S. E. , Jacod, J. , Podolskij M. and Shephard, N. (2006) A central limit theorem for realised power and bipower variations of continuous semimartingales, in: Kabanov, Y. , Lipster, R. , Stoyanov J. (Eds.), *From Stochastic Calculus to Mathematical Finance: The Shiryaev Festschrift*, Springer-Verlag, Berlin, pp. 33–68.

**See Also**

[setModel,cce](#)

**Examples**

```
set.seed(123)

# One-dimensional case
## Model:  $dX_t = t \cdot dW_t + t \cdot dz_t$ ,
## where  $z_t$  is a compound Poisson process with intensity 5 and jump sizes distribution  $N(0, 0.1)$ .

model <- setModel(drift=0, diffusion="t", jump.coeff="t", measure.type="CP",
                 measure=list(intensity=5, df=list("dnorm(z, 0, sqrt(0.1))")),
                 time.variable="t")

yuima.samp <- setSampling(Terminal = 1, n = 390)
yuima <- setYuima(model = model, sampling = yuima.samp)
yuima <- simulate(yuima)
plot(yuima)

mpv(yuima) # true value is 1/3
mpv(yuima, 1) # true value is 1/2
mpv(yuima, rep(2/3, 3)) # true value is 1/3

# Multi-dimensional case
## Model:  $dX_k t = t \cdot dW_k t$  ( $k=1, 2, 3$ ).

diff.matrix <- diag(3)
diag(diff.matrix) <- c("t", "t", "t")
model <- setModel(drift=c(0, 0, 0), diffusion=diff.matrix, time.variable="t",
                 solve.variable=c("x1", "x2", "x3"))

yuima.samp <- setSampling(Terminal = 1, n = 390)
yuima <- setYuima(model = model, sampling = yuima.samp)
yuima <- simulate(yuima)
plot(yuima)
```

```
mpv(yuima,list(c(1,1),1,rep(2/3,3))) # true value is c(1/3,1/2,1/3)
```

---

MWK151

*Graybill - Methuselah Walk - PILO - ITRDB CA535*

---

### Description

Graybill - Methuselah Walk - PILO - ITRDB CA535, pine tree width in mm from -608 to 1957.

### Usage

```
data(MWK151)
```

### Details

The full data records of past temperature, precipitation, and climate and environmental change derived from tree ring measurements. Parameter keywords describe what was measured in this data set. Additional summary information can be found in the abstracts of papers listed in the data set citations, however many of the data sets arise from unpublished research contributed to the International Tree Ring Data Bank. Additional information on data processing and analysis for International Tree Ring Data Bank (ITRDB) data sets can be found on the Tree Ring Page <http://www.ncdc.noaa.gov/paleo/treering.html>.

The MWK151 is only a small part of the data relative to one tree and contains measurement of a tree's ring width in mm, from -608 to 1957.

### Source

[http://hurricane.ncdc.noaa.gov/pls/paleox/f?p=519:1:::P1\\_STUDY\\_ID:3376](http://hurricane.ncdc.noaa.gov/pls/paleox/f?p=519:1:::P1_STUDY_ID:3376)

### References

Graybill, D.A., and Shiyatov, S.G., Dendroclimatic evidence from the northern Soviet Union, in *Climate since A.D. 1500*, edited by R.S. Bradley and P.D. Jones, Routledge, London, 393-414, 1992.

### Examples

```
data(MWK151)
```



---

noisy.sampling      *Noisy Observation Generator*

---

**Description**

Generates a new observation data contaminated by noise.

**Usage**

```
noisy.sampling(x, var.adj = 0, rng = "rnorm", mean.adj = 0, ...,
              end.coef = 0, n, order.adj = 0, znoise)
```

**Arguments**

x	an object of <a href="#">yuima-class</a> or <a href="#">yuima.data-class</a> .
var.adj	a matrix or list to be used for adjusting the variance matrix of the exogenous noise.
rng	a function to be used for generating the random numbers for the exogenous noise.
mean.adj	a numeric vector to be used for adjusting the mean vector of the exogenous noise.
...	passed to rng.
end.coef	a numeric vector or list to be used for adjusting the variance of the endogenous noise.
n	a numeric vector to be used for adjusting the scale of the endogenous noise.
order.adj	a positive number to be used for adjusting the order of the noise.
znoise	a list indicating other sources of noise processes. The default value is <code>as.list(double(dim(x)))</code> .

**Details**

TBA

**Value**

an object of [yuima.data-class](#).

**Author(s)**

The YUIMA Project Team

**See Also**

[cce](#)

**Examples**

```

## Set a model (a two-dimensional normal model sampled by a Poisson random sampling)
set.seed(123)

drift <- c(0,0)

sigma1 <- 1
sigma2 <- 1
rho <- 0.7

diffusion <- matrix(c(sigma1,sigma2*rho,0,sigma2*sqrt(1-rho^2)),2,2)

model <- setModel(drift=drift,diffusion=diffusion,
                  state.variable=c("x1","x2"),solve.variable=c("x1","x2"))

yuima.samp <- setSampling(Terminal = 1, n = 2340)
yuima <- setYuima(model = model, sampling = yuima.samp)
yuima <- simulate(yuima)

## Poisson random sampling
psample<- poisson.random.sampling(yuima, rate = c(1/3,1/6), n = 2340)

## Plot the path without noise
plot(psample)

# Set a matrix as the variance of noise
Omega <- 0.01*diffusion

## Contaminate the observation data by centered normal distributed noise
## with the variance matrix equal to 1% of the diffusion
noisy.psample1 <- noisy.sampling(psample,var.adj=Omega)
plot(noisy.psample1)

## Contaminate the observation data by centered uniformly distributed noise
## with the variance matrix equal to 1% of the diffusion
noisy.psample2 <- noisy.sampling(psample,var.adj=Omega,rng="runif",min=-sqrt(3),max=sqrt(3))
plot(noisy.psample2)

## Contaminate the observation data by centered exponentially distributed noise
## with the variance matrix equal to 1% of the diffusion
noisy.psample3 <- noisy.sampling(psample,var.adj=Omega,rng="rexp",rate=1,mean.adj=1)
plot(noisy.psample3)

## Contaminate the observation data by its return series
## multiplied by -0.1 times the square root of the intensity vector
## of the Poisson random sampling
noisy.psample4 <- noisy.sampling(psample,end.coef=-0.1,n=2340*c(1/3,1/6))
plot(noisy.psample4)

## An application:
## Adding a compound Poisson jumps to the observation data

```

```
## Set a compound Poisson process
intensity <- 5
j.num <- rpois(1,intensity) # Set a number of jumps
j.idx <- unique(ceiling(2340*runif(j.num))) # Set time indices of jumps
jump <- matrix(0,2,2341)
jump[,j.idx+1] <- sqrt(0.25/intensity)*diffusion
grid <- seq(0,1,by=1/2340)
CPprocess <- list(zoo(cumsum(jump[1,]),grid),zoo(cumsum(jump[2,]),grid))

## Adding the jumps
yuima.jump <- noisy.sampling(yuima,znoise=CPprocess)
plot(yuima.jump)

## Poisson random sampling
psample.jump <- poisson.random.sampling(yuima.jump, rate = c(1/3,1/6), n = 2340)
plot(psample.jump)
```

---

phi.test

*Phi-divergence test statistic for stochastic differential equations*


---

### Description

Phi-divergence test statistic for stochastic differential equations.

### Usage

```
phi.test(yuima, H0, H1, phi, print=FALSE,...)
```

### Arguments

yuima	a yuima object.
H0	a named list of parameter under H0.
H1	a named list of parameter under H1.
phi	the phi function to be used in the test. See Details.
print	you can see a progress of the estimation when print is TRUE.
...	passed to <a href="#">qmls</a> function.

### Details

phi.test executes a Phi-divergence test. If H1 is not specified this hypothesis is filled with the QMLE estimates.

If phi is missing, then  $\phi(x)=1-x+x*\log(x)$  and the Phi-divergence statistic corresponds to the likelihood ratio test statistic.

### Value

ans                    an object of class phi.test.

**Author(s)**

The YUIMA Project Team

**Examples**

```

model<- setModel(drift="t1*(t2-x)",diffusion="t3")
T<-10
n<-1000
sampling <- setSampling(Terminal=T,n=n)
yuima<-setYuima(model=model, sampling=sampling)

h0 <- list(t1=0.3, t2=1, t3=0.25)
X <- simulate(yuima, xinit=1, true=h0)
h1 <- list(t1=0.3, t2=0.2, t3=0.1)

phi1 <- function(x) 1-x+x*log(x)

phi.test(X, H0=h0, H1=h1,phi=phi1)
phi.test(X, H0=h0, phi=phi1, start=h0, lower=list(t1=0.1, t2=0.1, t3=0.1),
  upper=list(t1=2,t2=2,t3=2),method="L-BFGS-B")
phi.test(X, H0=h1, phi=phi1, start=h0, lower=list(t1=0.1, t2=0.1, t3=0.1),
  upper=list(t1=2,t2=2,t3=2),method="L-BFGS-B")

```

---

poisson.random.sampling

*Poisson random sampling method*

---

**Description**

Poisson random sampling method.

**Usage**

```
poisson.random.sampling(x, rate, n)
```

**Arguments**

x	an object of <a href="#">yuima.data-class</a> or <a href="#">yuima-class</a> .
rate	a Poisson intensity or a vector of Poisson intensities.
n	a common multiplier to the Poisson intensities. The default value is 1.

**Details**

It returns an object of type [yuima.data-class](#) which is a copy of the original input data where observations are sampled according to the Poisson process. The unsampled data are set to NA.

**Value**

an object of [yuima.data-class](#).

**Author(s)**

The YUIMA Project Team

**See Also**

[cce](#)

**Examples**

```
## Set a model
diff.coef.1 <- function(t, x1=0, x2) x2*(1+t)
diff.coef.2 <- function(t, x1, x2=0) x1*sqrt(1+t^2)
cor.rho <- function(t, x1=0, x2=0) sqrt((1+cos(x1*x2))/2)
diff.coef.matrix <- matrix(c("diff.coef.1(t,x1,x2)",
"diff.coef.2(t,x1,x2)*cor.rho(t,x1,x2)", "",
"diff.coef.2(t,x1,x2)*sqrt(1-cor.rho(t,x1,x2)^2)"),2,2)
cor.mod <- setModel(drift=c("", ""), diffusion=diff.coef.matrix,
solve.variable=c("x1", "x2"), xinit=c(3,2))
set.seed(111)

## We first simulate the two dimensional diffusion model
yuima.samp <- setSampling(Terminal=1, n=1200)
yuima <- setYuima(model=cor.mod, sampling=yuima.samp)
yuima.sim <- simulate(yuima)

## Then we use function poisson.random.sampling to get observations
## by Poisson sampling.
psample <- poisson.random.sampling(yuima.sim, rate = c(0.2, 0.3), n=1000)
str(psample)
```

---

qgv

qgv

---

**Description**

Estimate the local Holder exponent with quadratic generalized variations method

**Usage**

```
qgv(yuima, filter.type = "Daubechies", order = 2, a = NULL)
```

**Arguments**

yuima	A yuima object.
filter.type	The filter.type can be set to "Daubechies" or "Classical".
order	The order of the filter a to be chosen
a	Any other filter

**Details**

Estimation of the Hurst index and the constant of the fractional Ornstein-Uhlenbeck process.

**Value**

an object of class qgv

**Author(s)**

The YUIMA Project Team

**References**

Brouste, A., Iacus, S.M. (2013) Parameter estimation for the discretely observed fractional Ornstein-Uhlenbeck process and the Yuima R package, *Computational Statistics*, pp. 1129–1147.

**See Also**

See also [mmfrac](#).

**Examples**

```
# Estimating both Hurst parameter and diffusion coefficient in fractional Ornstein-Uhlenbeck

model<-setModel(drift="-x*lambda",hurst=NA,diffusion="theta")
sampling<-setSampling(T=100,n=10000)
yui1<-simulate(model,true.param=list(theta=1,lambda=4),hurst=0.7,sampling=sampling)
qgv(yui1)

# Estimating Hurst parameter only in diffusion processes

model2<-setModel(drift="-x*lambda",hurst=NA,diffusion="theta*sqrt(x)")
sampling<-setSampling(T=1,n=10000)
yui2<-simulate(model2,true.param=list(theta=1,lambda=4),hurst=0.7,sampling=sampling,xinit=10)
qgv(yui2)
```

---

qmle

*Calculate quasi-likelihood and ML estimator of least squares estimator*

---

**Description**

Calculate the quasi-likelihood and estimate of the parameters of the stochastic differential equation by the maximum likelihood method or least squares estimator of the drift parameter.

**Usage**

```
qmle(yuima, start, method="BFGS", fixed = list(), print=FALSE, lower, upper,
     joint=FALSE, Est.Incr="Carma.IncPar",aggregation=TRUE, threshold=NULL, ...)
quasilogl(yuima, param, print=FALSE)
lse(yuima, start, lower, upper, method = "BFGS", ...)
```

**Arguments**

yuima	a yuima object.
print	you can see a progress of the estimation when print is TRUE.
method	see Details.
param	list of parameters for the quasi loglikelihood.
lower	a named list for specifying lower bounds of parameters
upper	a named list for specifying upper bounds of parameters
start	initial values to be passed to the optimizer.
fixed	for conditional (quasi)maximum likelihood estimation.
joint	perform joint estimation or two stage estimation? by default joint=FALSE.
Est.Incr	If the yuima model is an object of <a href="#">yuima.carma-class</a> the qmle returns an object of <a href="#">yuima.carma.qmle-class</a> or object of class <code>mle-class</code> . By default Est.Incr="Carma.IncPar".
aggregation	If aggregation=TRUE, before the estimation of the levy parameters we aggregate the increments.
threshold	If the model has Compund Poisson type jumps, the threshold is used to perform thresholding of the increments.
...	passed to <a href="#">optim</a> method. See Examples.

**Details**

qmle behaves more likely the standard mle function in **stats4** and argument method is one of the methods available in [optim](#).

lse calculates least squares estimators of the drift parameters. This is useful for initial guess of qmle estimation.

quasilogl returns the value of the quasi loglikelihood for a given yuima object and list of parameters coef.

**Value**

QL	a real value.
opt	a list with components the same as 'optim' function.
carmaopt	if the model is an object of <a href="#">yuima.carma-class</a> , qmle returns an object <a href="#">yuima.carma.qmle-class</a>

**Note**

The function `qmle` uses the function `optim` internally.

The function `qmle` uses the function `CarmaNoise` internally for estimation of underlying Levy if the model is an object of `yuima.carma-class`.

**Author(s)**

The YUIMA Project Team

**Examples**

```

#dXt^e = -theta2 * Xt^e * dt + theta1 * dWt
diff.matrix <- matrix(c("theta1"), 1, 1)
ymodel <- setModel(drift=c("(-1)*theta2*x"), diffusion=diff.matrix,
  time.variable="t", state.variable="x", solve.variable="x")
n <- 100

ysamp <- setSampling(Terminal=(n)^(1/3), n=n)
yuima <- setYuima(model=ymodel, sampling=ysamp)
set.seed(123)
yuima <- simulate(yuima, xinit=1, true.parameter=list(theta1=0.3,
  theta2=0.1))
QL <- quasilogl(yuima, param=list(theta2=0.8, theta1=0.7))
##QL <- ql(yuima, 0.8, 0.7, h=1/((n)^(2/3)))
QL

## another way of parameter specification
##param <- list(theta2=0.8, theta1=0.7)
##QL <- ql(yuima, h=1/((n)^(2/3)), param=param)
##QL

## old code
##system.time(
##opt <- ml.ql(yuima, 0.8, 0.7, h=1/((n)^(2/3)), c(0, 1), c(0, 1))
##)
##cat(sprintf("\nTrue param. theta2 = .3, theta1 = .1\n"))
##print(coef(opt))

system.time(
opt2 <- qmle(yuima, start=list(theta1=0.8, theta2=0.7), lower=list(theta1=0, theta2=0),
  upper=list(theta1=1, theta2=1), method="L-BFGS-B")
)
cat(sprintf("\nTrue param. theta2 = .3, theta1 = .1\n"))
print(coef(opt2))

## initial guess for theta2 by least squares estimator
tmp <- lse(yuima, start=list(theta2=0.7), lower=list(theta2=0), upper=list(theta2=1))
tmp

```



```

system.time(
opt3 <- qmle(yuima, start=list(theta1=0.8, theta2=tmp), lower=list(theta1=0,theta2=0),
  upper=list(theta1=1,theta2=1), method="L-BFGS-B")
)
cat(sprintf("\nTrue param. theta2 = .3, theta1 = .1\n"))
print(coef(opt3))

## perform joint estimation? Non-optimal, just for didactic purposes
system.time(
opt4 <- qmle(yuima, start=list(theta1=0.8, theta2=0.7), lower=list(theta1=0,theta2=0),
  upper=list(theta1=1,theta2=1), method="L-BFGS-B", joint=TRUE)
)
cat(sprintf("\nTrue param. theta2 = .3, theta1 = .1\n"))
print(coef(opt4))

## old code
##system.time(
##opt <- ml.ql(yuima, 0.8, 0.7, h=1/((n)^(2/3)), c(0, 1), c(0, 1), method="Newton")
##)
##cat(sprintf("\nTrue param. theta2 = .3, theta1 = .1\n"))
##print(coef(opt))

## Not run:

###multidimension case
##dXt^e = - drift.matrix * Xt^e * dt + diff.matrix * dWt
diff.matrix <- matrix(c("theta1.1","theta1.2", "1", "1"), 2, 2)

drift.c <- c("-theta2.1*x1", "-theta2.2*x2", "-theta2.2", "-theta2.1")
drift.matrix <- matrix(drift.c, 2, 2)

ymodel <- setModel(drift=drift.matrix, diffusion=diff.matrix, time.variable="t",
  state.variable=c("x1", "x2"), solve.variable=c("x1", "x2"))
n <- 100
ysamp <- setSampling(Terminal=(n)^(1/3), n=n)
yuima <- setYuima(model=ymodel, sampling=ysamp)
set.seed(123)

##xinit=c(x1, x2) #true.parameter=c(theta2.1, theta2.2, theta1.1, theta1.2)
yuima <- simulate(yuima, xinit=c(1, 1),
  true.parameter=list(theta2.1=0.5, theta2.2=0.3, theta1.1=0.6, theta1.2=0.2))

## theta2 <- c(0.8, 0.2) #c(theta2.1, theta2.2)
##theta1 <- c(0.7, 0.1) #c(theta1.1, theta1.2)
## QL <- ql(yuima, theta2, theta1, h=1/((n)^(2/3)))
## QL

## ## another way of parameter specification
## #param <- list(theta2=theta2, theta1=theta1)
## #QL <- ql(yuima, h=1/((n)^(2/3)), param=param)
## #QL

```

```

## theta2.1.lim <- c(0, 1)
## theta2.2.lim <- c(0, 1)
## theta1.1.lim <- c(0, 1)
## theta1.2.lim <- c(0, 1)
## theta2.lim <- t( matrix( c(theta2.1.lim, theta2.2.lim), 2, 2) )
## theta1.lim <- t( matrix( c(theta1.1.lim, theta1.2.lim), 2, 2) )

## system.time(
## opt <- ml.ql(yuima, theta2, theta1, h=1/((n)^(2/3)), theta2.lim, theta1.lim)
## )
## opt@coef

system.time(
opt2 <- qmle(yuima, start=list(theta2.1=0.8, theta2.2=0.2, theta1.1=0.7, theta1.2=0.1),
  lower=list(theta1.1=.1, theta1.2=.1, theta2.1=.1, theta2.2=.1),
  upper=list(theta1.1=4, theta1.2=4, theta2.1=4, theta2.2=4), method="L-BFGS-B")
)
opt2@coef
summary(opt2)

## unconstrained optimization
system.time(
opt3 <- qmle(yuima, start=list(theta2.1=0.8, theta2.2=0.2, theta1.1=0.7, theta1.2=0.1))
)
opt3@coef
summary(opt3)

quasilogl(yuima, param=list(theta2.1=0.8, theta2.2=0.2, theta1.1=0.7, theta1.2=0.1))

##system.time(
##opt <- ml.ql(yuima, theta2, theta1, h=1/((n)^(2/3)), theta2.lim, theta1.lim, method="Newton")
##)
##opt@coef
##

# carma(p=2,q=0) driven by a brownian motion without location parameter

mod0<-setCarma(p=2,
  q=0,
  scale.par="sigma")

true.parm0 <-list(a1=1.39631,
  a2=0.05029,
  b0=1,
  sigma=0.23)

samp0<-setSampling(Terminal=100,n=250)
set.seed(123)
sim0<-simulate(mod0,
  true.parameter=true.parm0,

```

```
        sampling=samp0)

system.time(
carmaopt0 <- qmle(sim0, start=list(a1=1.39631,a2=0.05029,
                                b0=1,
                                sigma=0.23))
)

summary(carmaopt0)

# carma(p=2,q=1) driven by a brownian motion without location parameter

mod1<-setCarma(p=2,
              q=1)

true.parm1 <-list(a1=1.39631,
                 a2=0.05029,
                 b0=1,
                 b1=2)

samp1<-setSampling(Terminal=100,n=250)
set.seed(123)
sim1<-simulate(mod1,
              true.parameter=true.parm1,
              sampling=samp1)

system.time(
  carmaopt1 <- qmle(sim1, start=list(a1=1.39631,a2=0.05029,
                                    b0=1,b1=2),joint=TRUE)
)

summary(carmaopt1)

plot(carmaopt1)

# carma(p=2,q=1) driven by a compound poisson process where the jump size is normally distributed.

mod2<-setCarma(p=2,
              q=1,
              measure=list(intensity="1",df=list("dnorm(z, 0, 1)")),
              measure.type="CP")

true.parm2 <-list(a1=1.39631,
                 a2=0.05029,
                 b0=1,
                 b1=2)

samp2<-setSampling(Terminal=100,n=250)
set.seed(123)
```

```

sim2<-simulate(mod2,
               true.parameter=true.parm2,
               sampling=samp2)

system.time(
  carmaopt2 <- qmle(sim2, start=list(a1=1.39631,a2=0.05029,
                                   b0=1,b1=2),joint=TRUE)
)

summary(carmaopt2)

plot(carmaopt2)

# carma(p=2,q=1) driven by a normal inverse gaussian process
mod3<-setCarma(p=2,q=1,
               measure=list(df=list("rNIG(z, alpha, beta, delta1, mu)")),
               measure.type="code")

#

# True param
true.param3<-list(a1=1.39631,
                  a2=0.05029,
                  b0=1,
                  b1=2,
                  alpha=1,
                  beta=0,
                  delta1=1,
                  mu=0)

samp3<-setSampling(Terminal=100,n=200)
set.seed(123)

sim3<-simulate(mod3,
               true.parameter=true.param3,
               sampling=samp3)

carmaopt3<-qmle(sim3,start=true.param3)

summary(carmaopt3)

plot(carmaopt3)

## End(Not run)

```

**Description**

Fictitious rng for the constant random variable used to generate and describe Poisson jumps.

**Usage**

```
rconst(n, k = 1)
dconst(x, k = 1)
```

**Arguments**

n	number of replications
k	the size of the jump
x	the fictitious argument

**Value**

returns a numeric vector

**Author(s)**

The YUIMA Project Team

**Examples**

```
dconst(1,1)
dconst(2,1)
dconst(2,2)

rconst(10,3)
```

---

 rng

*Random Number Generators for yuima package*


---

**Description**

simulate function uses specific random number generators to generate Levy paths.

**Usage**

```
rIG(x, delta, gamma)
rNIG(x, alpha=1, beta=0, delta=1, mu=0, Lambda)
rbgamma(x, delta.plus, gamma.plus, delta.minus, gamma.minus)
rngamma(x, lambda, alpha, beta, mu, Lambda)
rstable(x, alpha, beta, sigma, gamma)
```

**Arguments**

x	Number of R.Ns to be geneated.
delta	param
delta.plus	param
delta.minus	param
gamma	param
gamma.plus	param
gamma.minus	param
alpha	param
beta	parame
mu	param
lambda	param
Lambda	param
sigma	param

**Details**

to be written

**Value**

rIG	A vector of random numbers.
rNIG	A vector of random numbers.
rbgamma	A vector of random numbers.

**Note**

Random number generators may be rewritten with C language to speed up.

**Author(s)**

The YUIMA Project Team

---

setCarma *Continuous Autoregressive Moving Average (p, q) model*

---

### Description

'setCarma' describes the following model:

$$V_t = c_0 + \sigma (b_0 X_t(0) + \dots + b(q) X_t(q))$$

$$dX_t(0) = X_t(1) dt$$

...

$$dX_t(p-2) = X_t(p-1) dt$$

$$dX_t(p-1) = (-a(p) X_t(0) - \dots - a(1) X_t(p-1))dt + (\gamma(0) + \gamma(1) X_t(0) + \dots + \gamma(p) X_t(p-1))dt$$

The continuous ARMA process using the state-space representation as in Brockwell (2000) is obtained by choosing:

$$\gamma(0) = 1, \gamma(1) = \gamma(2) = \dots = \gamma(p) = 0.$$

Please refer to the vignettes and the examples or the **yuima** documentation for details.

### Usage

```
setCarma(p,q,loc.par=NULL,scale.par=NULL,ar.par="a",ma.par="b",
lin.par=NULL,Carma.var="v",Latent.var="x",XinExpr=FALSE, ...)
```

### Arguments

p	a non-negative integer that indicates the number of the autoregressive coefficients.
q	a non-negative integer that indicates the number of the moving average coefficients.
loc.par	location coefficient. The default value loc.par=NULL implies that $c_0=0$ .
scale.par	scale coefficient. The default value scale.par=NULL implies that $\sigma=1$ .
ar.par	a character-string that is the label of the autoregressive coefficients. The default Value is ar.par="a".
ma.par	a character-string that is the label of the moving average coefficients. The default Value is ma.par="b".
Carma.var	a character-string that is the label of the observed process. Defaults to "v".
Latent.var	a character-string that is the label of the unobserved process. Defaults to "x".
lin.par	a character-string that is the label of the linear coefficients. If lin.par=NULL, the default, the 'setCarma' builds the CARMA(p, q) model defined as in Brockwell (2000).
XinExpr	a logical variable. The default value XinExpr=FALSE implies that the starting condition for Latent.var is zero. If XinExpr=TRUE, each component of Latent.var has a parameter as a initial value.

... Arguments to be passed to 'setCarma', such as the slots of `yuima.model-class`  
 measure Levy measure of jump variables.  
 measure.type type specification for Levy measure.  
 xinit a vector of expressions identifying the starting conditions for CARMA  
 model.

### Details

Please refer to the vignettes and the examples or to the **yuimadocs** package.

An object of `yuima.carma-class` contains:

info: It is an object of `carma.info-class` which is a list of arguments that identifies the carma(p,q)  
 model

and the same slots in an object of `yuima.model-class`.

### Value

model an object of `yuima.carma-class`.

### Note

There may be missing information in the model description. Please contribute with suggestions and fixings.

### Author(s)

The YUIMA Project Team

### References

Brockwell, P. (2000) Continuous-time ARMA processes, *Stochastic Processes: Theory and Methods. Handbook of Statistics*, **19**, (C. R. Rao and D. N. Shandhag, eds.) 249-276. North-Holland, Amsterdam.

### Examples

```
# Ex 1. (Continuous ARMA process driven by a Brownian Motion)
# To describe the state-space representation of a CARMA(p=3,q=1) model:
# Vt=c0+alpha0*X0t+alpha1*X1t
# dX0t = X1t*dt
# dX1t = X2t*dt
# dX2t = (-beta3*X0t-beta2*X1t-beta1*X2t)dt+dWt
# we set
mod1<-setCarma(p=3,
               q=1,
               loc.par="c0")
# Look at the model structure by
str(mod1)
```



```

# Ex 2. (General setCarma model driven by a Brownian Motion)
# To describe the model defined as:
#  $V_t = c_0 + \alpha_0 X_{0t} + \alpha_1 X_{1t}$ 
#  $dX_{0t} = X_{1t} dt$ 
#  $dX_{1t} = X_{2t} dt$ 
#  $dX_{2t} = (-\beta_3 X_{0t} - \beta_2 X_{1t} - \beta_1 X_{2t}) dt + (c_0 + \alpha_0 X_{0t}) dW_t$ 
# we set
mod2 <- setCarma(p=3,
                 q=1,
                 loc.par="c0",
                 ma.par="alpha",
                 ar.par="beta",
                 lin.par="alpha")
# Look at the model structure by
str(mod2)

# Ex 3. (Continuous Arma model driven by a Levy process)
# To specify the CARMA(p=3,q=1) model driven by a Compound Poisson process defined as:
#  $V_t = c_0 + \alpha_0 X_{0t} + \alpha_1 X_{1t}$ 
#  $dX_{0t} = X_{1t} dt$ 
#  $dX_{1t} = X_{2t} dt$ 
#  $dX_{2t} = (-\beta_3 X_{0t} - \beta_2 X_{1t} - \beta_1 X_{2t}) dt + dz_t$ 
# we set the Levy measure as in setModel
mod3 <- setCarma(p=3,
                 q=1,
                 loc.par="c0",
                 measure=list(intensity="1",df=list("dnorm(z, 0, 1)")),
                 measure.type="CP")
# Look at the model structure by
str(mod3)

# Ex 4. (General setCarma model driven by a Levy process)
#  $V_t = c_0 + \alpha_0 X_{0t} + \alpha_1 X_{1t}$ 
#  $dX_{0t} = X_{1t} dt$ 
#  $dX_{1t} = X_{2t} dt$ 
#  $dX_{2t} = (-\beta_3 X_{1t} - \beta_2 X_{2t} - \beta_1 X_{3t}) dt + (c_0 + \alpha_0 X_{0t}) dz_t$ 
mod4 <- setCarma(p=3,
                 q=1,
                 loc.par="c0",
                 ma.par="alpha",
                 ar.par="beta",
                 lin.par="alpha",
                 measure=list(intensity="1",df=list("dnorm(z, 0, 1)")),
                 measure.type="CP")
# Look at the model structure by
str(mod4)

```

**Description**

setCharacteristic is a constructor for characteristic class.

**Usage**

```
setCharacteristic(equation.number, time.scale)
```

**Arguments**

equation.number      The number of equations modeled in yuima object.  
time.scale      time.scale assumed in the model.

**Details**

class characteristic has two slots, equation.number is the number of equations handled in the yuima object, and time.scale is a hoge of characteristic.

**Value**

An object of class characteristic.

**Author(s)**

The YUIMA Project Team

---

setData	<i>Set and access data of an object of type "yuima.data" or "yuima".</i>
---------	--

---

**Description**

setData constructs an object of [yuima.data-class](#).

get.zoo.data returns the content of the zoo.data slot of a [yuima.data-class](#) object. (Note: value is a list of [zoo](#) objects).

plot plot method for object of [yuima.data-class](#) or [yuima-class](#).

dim returns the [dim](#) of the zoo.data slot of a [yuima.data-class](#) object.

length returns the [length](#) of the time series in zoo.data slot of a [yuima.data-class](#) object.

cbind.yuima bind yuima.data object.

**Usage**

```
setData(original.data, delta=NULL)
get.zoo.data(x)
```

**Arguments**

original.data	some type of data, usually some sort of time series. The function always tries to convert to the input data into an object of <code>zoo</code> -type. See Details.
x	an object of type <code>yuima.data-class</code> or <code>yuima-class</code> .
delta	If there is the need to redefine on the fly the delta increment of the data to make it consistent to statistical theory. See Details.

**Details**

Objects in the `yuima.data-class` contain two slots:

`original.data`: The slot `original.data` contains, as the name suggests, a copy of the original data passed to the function `setData`. It is intended for backup purposes.

`zoo.data`: the function `setData` tries to convert `original.data` into an object of class `zoo`. The coerced `zoo` data are stored in the slot `zoo.data`. If the conversion fails the function exits with an error. Internally, the `yuima` package stores and operates on `zoo`-type objects.

The function `get.zoo.data` returns the content of the slot `zoo.data` of `x` if `x` is of `yuima.data-class` or the content of `x@data@zoo.data` if `x` is of `yuima-class`.

**Value**

value	a list of object(s) of <code>yuima.data-class</code> for <code>setData</code> . The content of the <code>zoo.data</code> slot for <code>get.zoo.data</code>
-------	---

**Author(s)**

The YUIMA Project Team

**Examples**

```
X <- ts(matrix(rnorm(200),100,2))
mydata <- setData(X)
str(get.zoo.data(mydata))
dim(mydata)
length(mydata)
plot(mydata)

# exactly the same output
mysde <- setYuima(data=setData(X))
str(get.zoo.data(mysde))
plot(mysde)
dim(mysde)
length(mysde)

# changing delta on the fly to 1/252
mysde2 <- setYuima(data=setData(X, delta=1/252))
str(get.zoo.data(mysde2))
plot(mysde2)
dim(mysde2)
```

```
length(mysde2)
```

---

setFunctional	<i>Description of a functional associated with a perturbed stochastic differential equation</i>
---------------	---

---

### Description

This function is used to give a description of the stochastic differential equation. The functional represent the price of the option in financial economics, for example.

### Usage

```
setFunctional(model, F, f, xinit,e)
```

### Arguments

model	yuima or yuima.model object.
F	function of $X_t$ and $\epsilon$
f	list of functions of $X_t$ and $\epsilon$
xinit	initial values of state variable.
e	epsilon parameter

### Details

You should look at the vignette and examples.

The object `foi` contains several “slots”. To see inside its structure we use the `R` command `str. f` and `Fare R` (list of) expressions which contains the functional of interest specification. `e` is a small parameter on which we conduct asymptotic expansion of the functional.

### Value

yuima	an object of class 'yuima' containing object of class 'functional'. If yuima object was given as 'model' argument, the result is just added and the other slots of the object are maintained.
-------	---

### Note

There may be missing information in the model description. Please contribute with suggestions and fixings.

### Author(s)

The YUIMA Project Team

## Examples

```

set.seed(123)
# to the Black-Scholes economy:
# dXt^e = Xt^e * dt + e * Xt^e * dWt
diff.matrix <- matrix( c("x*e"), 1,1)
model <- setModel(drift = c("x"), diffusion = diff.matrix)
# call option is evaluated by averating
# max{ (1/T)*int_0^T Xt^e dt, 0}, the first argument is the functional of interest:
Terminal <- 1
xinit <- c(1)
f <- list( c(expression(x/Terminal)), c(expression(0)))
F <- 0
division <- 1000
e <- .3
yuima <- setYuima(model = model,sampling = setSampling(Terminal = Terminal, n = division))
yuima <- setFunctional( model = yuima, xinit=xinit, f=f,F=F,e=e)
# look at the model structure
str(yuima@functional)

```

---

setModel

*Basic description of stochastic differential equations (SDE)*


---

## Description

'setModel' gives a description of stochastic differential equation with or without jumps of the following form:

$$dX_t = a(t, X_t, \alpha)dt + b(t, X_t, \beta)dW_t + c(t, X_t, \gamma)dZ_t, \quad X_0 = x_0$$

All functions relying on the **yuima** package will get as much information as possible from the different slots of the [yuima-class](#) structure without replicating the same code twice. If there are missing pieces of information, some default values can be assumed.

## Usage

```

setModel(drift = NULL, diffusion = NULL, hurst = 0.5, jump.coeff = NULL,
measure = list(), measure.type = character(), state.variable = "x",
jump.variable = "z", time.variable = "t", solve.variable, xinit)

```

## Arguments

drift	a vector of expressions (the default value is 0 when drift=NULL).
diffusion	a matrix of expressions (the default value is 0 when diffusion=NULL).
hurst	the Hurst parameter of the gaussian noise. If h=0.5, the default, the process is Wiener otherwise it is fractional Brownian motion with that precise value of the Hurst index. Can be set to NA for further specification.
jump.coeff	a matrix of expressions for the jump component.
measure	Levy measure for jump variables.

measure.type	type specification for Levy measures.
state.variable	a vector of names of the state variables in the drift and diffusion coefficients.
jump.variable	a vector of names of the jump variables in the jump coefficient.
time.variable	the name of the time variable.
solve.variable	a vector of names of the variables in the left-hand-side of the equations in the model; solve.variable equals state.variable as long as we have no exogenous variable other than statistical parameters in the coefficients (drift and diffusion).
xinit	a vector of numbers identifying the initial value of the solve.variable.

### Details

Please refer to the vignettes and the examples or to the **yuimadocs** package.

An object of `yuima.model-class` contains several slots:

**drift:** an R expression which specifies the drift coefficient (a vector).

**diffusion:** an R expression which specifies the diffusion coefficient (a matrix).

**jump.coeff:** coefficient of the jump term.

**measure:** the Levy measure of the driving Levy process.

**measure.type:** specifies the type of the measure, such as CP, code or density. See below.

**parameter:** a short name for “parameters”. It is an object of `model.parameter-class` which is a list of vectors of names of parameters belonging to the single components of the model (drift, diffusion, jump and measure), the names of common parameters and the names of all parameters. For more details see `model.parameter-class` documentation page.

**solve.variable:** a vector of variable names, each element corresponds to the name of the solution variable (left-hand-side) of each equation in the model, in the corresponding order.

**state.variable:** identifies the state variables in the R expression. By default, it is assumed to be `x`.

**jump.variable:** the variable for the jump coefficient. By default, it is assumed to be `z`.

**time:** the time variable. By default, it is assumed to be `t`.

**solve.variable:** used to identify the solution variables in the R expression, i.e. the variable with respect to which the stochastic differential equation has to be solved. By default, it is assumed to be `x`, otherwise the user can choose any other model specification.

**noise.number:** denotes the number of sources of noise. Currently only for the Gaussian part.

**equation.number:** denotes the dimension of the stochastic differential equation.

**dimension:** the dimensions of the parameters in the parameter slot.

**xinit:** denotes the initial value of the stochastic differential equation.

The `yuima.model-class` structure assumes that the user either uses the default names for `state.variable`, `jump.variable`, `solution.variable` and `time.variable` or specifies his/her own names. All the rest of the terms in the R expressions are considered as parameters and identified accordingly in the parameter slot.

**Value**

model                    an object of `yuima.model-class`.

**Note**

There may be missing information in the model description. Please contribute with suggestions and fixings.

**Author(s)**

The YUIMA Project Team

**Examples**

```
# Ex 1. (One-dimensional diffusion process)
# To describe
#  $dX_t = -3X_t dt + (1/(1+X_t^2+t))dW_t$ ,
# we set
mod1 <- setModel(drift = "-3*x", diffusion = "1/(1+x^2+t)", solve.variable = c("x"))
# We may omit the solve.variable; then the default variable x is used
mod1 <- setModel(drift = "-3*x", diffusion = "1/(1+x^2+t)")
# Look at the model structure by
str(mod1)

# Ex 2. (Two-dimensional diffusion process with three factors)
# To describe
#  $dX_{1t} = -3X_{1t}dt + dW_{1t} + x_{2t}dW_{3t}$ ,
#  $dX_{2t} = -(X_{1t} + 2X_{2t})dt + x_{1t}dW_{1t} + 3dW_{2t}$ ,
# we set the drift coefficient
a <- c("-3*x1", "-x1-2*x2")
# and also the diffusion coefficient
b <- matrix(c("1", "x1", "0", "3", "x2", "0"), 2, 3)
# Then set
mod2 <- setModel(drift = a, diffusion = b, solve.variable = c("x1", "x2"))
# Look at the model structure by
str(mod2)
# The noise.number is automatically determined by inputting the diffusion matrix expression.
# If the dimensions of the drift differs from the number of the rows of the diffusion,
# the error message is returned.

# Ex 3. (Process with jumps)
## specify the jump term as  $c(x,t)dz$ 
mod3 <- setModel(drift=c("-theta*x"), diffusion="sigma",
  jump.coeff="1", measure=list(intensity="1", df=list("dnorm(z, 0, 1)")),
  measure.type="CP", solve.variable="x")
# Look at the model structure by
str(mod3)

# Ex 4. (Process with fractional Gaussian noise)
#  $dY_t = 3Y_t dt + dW_t^h$ 
mod4 <- setModel(drift="3*y", diffusion=1, hurst=0.3, solve.variable=c("y"))
# Look at the model structure by
```

```
str(mod4)
```

---

```
setPoisson
```

*Basic constructor for Compound Poisson processes*

---

## Description

'setPoisson' construct a Compound Poisson model specification for a process of the form:

$$M_t = m_0 + \sum_{i=0}^{N_t} c * Y_{\{\tau_i\}}, \quad M_0 = m_0$$

where  $N_t$  is a homogeneous or time-inhomogeneous Poisson process,  $\tau_i$  is the sequence of random times of  $N_t$  and  $Y$  is a sequence of i.i.d. random jumps.

## Usage

```
setPoisson(intensity = 1, df = NULL, scale = 1, dimension=1, ...)
```

## Arguments

intensity	either an expression or a numerical value representing the intensity function of the Poisson process $N_t$ .
df	is the density of jump random variables $Y$ .
scale	this is the scaling factor $c$ .
dimension	this is the dimension of the jump component.
...	passed to <a href="#">setModel</a>

## Details

An object of [yuima.model-class](#) where the model slot is of class [yuima.poisson-class](#).

## Value

model            an object of [yuima.model-class](#).

## Author(s)

The YUIMA Project Team

## Examples

```
Terminal <- 10
samp <- setSampling(T=Terminal,n=1000)

# Ex 1. (Simple homogeneous Poisson process)
mod1 <- setPoisson(intensity="lambda", df=list("dconst(z,1)"))
set.seed(123)
y1 <- simulate(mod1, true.par=list(lambda=1),sampling=samp)
plot(y1)
```



```

# scaling the jumps
mod2 <- setPoisson(intensity="lambda", df=list("dconst(z,1)"),scale=5)
set.seed(123)
y2 <- simulate(mod2, true.par=list(lambda=1),sampling=samp)
plot(y2)

# scaling the jumps through the constant distribution
mod3 <- setPoisson(intensity="lambda", df=list("dconst(z,5)"))
set.seed(123)
y3 <- simulate(mod3, true.par=list(lambda=1),sampling=samp)
plot(y3)

# Ex 2. (Time inhomogeneous Poisson process)
mod4 <- setPoisson(intensity="beta*(1+sin(lambda*t))", df=list("dconst(z,1)"))
set.seed(123)
lambda <- 3
beta <- 5
y4 <- simulate(mod4, true.par=list(lambda=lambda,beta=beta),sampling=samp)
par(mfrow=c(2,1))
par(mar=c(3,3,1,1))
plot(y4)
f <- function(t) beta*(1+sin(lambda*t))
curve(f, 0, Terminal, col="red")

# Ex 2. (Time inhomogeneous Compound Poisson process with Gaussian Jumps)
mod5 <- setPoisson(intensity="beta*(1+sin(lambda*t))", df=list("dnorm(z,mu,sigma)"))
set.seed(123)
y5 <- simulate(mod5, true.par=list(lambda=lambda,beta=beta,mu=0, sigma=2),sampling=samp)
plot(y5)
f <- function(t) beta*(1+sin(lambda*t))
curve(f, 0, Terminal, col="red")

```

---

setSampling

*Set sampling information and create a 'sampling' object.*


---

## Description

setSampling is a constructor for [yuima.sampling-class](#).

## Usage

```

setSampling(Initial = 0, Terminal = 1, n = 100, delta,
  grid, random = FALSE, sdelta=as.numeric(NULL),
  sgrid=as.numeric(NULL), interpolation="pt" )

```

**Arguments**

Initial	Initial time of the grid.
Terminal	Terminal time of the grid.
n	number of time intervals.
delta	mesh size in case of regular time grid.
grid	a grid of times for the simulation, possibly empty.
random	specify if it is random sampling. See Details.
sdelta	mesh size in case of regular space grid.
sgrid	a grid in space for the simulation, possibly empty.
interpolation	a rule of interpolation in case of subsampling. By default, the previous tick interpolation. See Details.

**Details**

The function creates an object of type `yuima.sampling-class` with several slots.

**Initial:** initial time of the grid.

**Terminal:** terminal time fo the grid.

**n:** the number of observations - 1.

**delta:** in case of a regular time grid it is the mesh.

**grid:** the grid of times.

**random:** either FALSE or the distribution of the random times.

**regular:** indicator of whether the grid is regular or not. For internal use only.

**sdelta:** in case of a regular space grid it is the mesh.

**sgrid:** the grid in space.

**oindex:** in case of interpolation, a vector of indexes corresponding to the original observations used for the approximation.

**interpolation:** the name of the interpolation method used.

In case of subsampling, the observations are subsampled on some given `grid/sgrid` or according to some `random` times. When the original observations do not exist at a give point of the grid they are obtained by some approximation method. Available methods are "pt" or "previous tick" observation method, "nt" or "next tick" observation method, or by "linear" interpolation. In case of interpolation, the slot `oindex` contains the vector of indexes corresponding to the original observations used for the approximation. For the linear method the index corresponds to the left-most observation.

The slot `random` is used as information in case a `grid` is already determined (e.g. `n` or `delta`, etc. of the `grid` itself are given) or if some subsampling has occurred or if some particular method which causes a random `grid` is used in simulation (for example the space discretized Euler scheme). The slot `random` contains a list of two elements `distr` and `scale`, where `distr` is a the distribution of independent random times and `scale` is either a scaling constant or a scaling function. If the `grid` of times is deterministic, then `random` is FALSE.

If not specified and `random=FALSE`, the slot grid is filled automatically by the function. It is eventually modified or created after the call to the function `simulate`.

If `delta` is not specified, it is calculated as  $(\text{Terminal}-\text{Initial})/n$ . If `delta` is specified, the `Terminal` is adjusted to be equal to  $\text{Initial}+n*\text{delta}$ .

The vectors `delta`, `n`, `Initial` and `Terminal` may have different lengths, but then they are extended to the maximal length to keep consistency. See examples.

If `grid` is specified, it takes precedence over all other arguments.

### Value

An object of type `yuima.sampling-class`.

### Author(s)

The YUIMA Project Team

### Examples

```
samp <- setSampling(Terminal=1, n=1000)
str(samp)
```

```
samp <- setSampling(Terminal=1, n=1000, delta=0.3)
str(samp)
```

```
samp <- setSampling(Terminal=1, n=1000, delta=c(0.1,0.3))
str(samp)
```

```
samp <- setSampling(Terminal=1:3, n=1000)
str(samp)
```

---

setYuima	<i>Creates a "yuima" object by combining "model", "data", "sampling", "characteristic" and "functional" slots.</i>
----------	--

---

### Description

`setYuima` constructs an object of `yuima-class`.

### Usage

```
setYuima(data, model, sampling, characteristic, functional)
```

**Arguments**

data	an object of <code>yuima.data-class</code> .
model	an object of <code>yuima.model-class</code> .
sampling	an object of <code>yuima.sampling-class</code> .
characteristic	an object of <code>yuima.characteristic-class</code> .
functional	an object of class <code>yuima.functional-class</code> .

**Details**

The `yuima-class` object is the main object of the **yuima** package. Some of the slots can be missing.

The slot `data` contains the data, either empirical or simulated.

The slot `model` contains the description of the (statistical) model which is used to generate the data via different simulation schemes, to draw inference from the data or both.

The slot `sampling` contains information on how the data have been collected or how they should be simulated.

The slot `characteristic` contains information on PLEASE FINISH THIS. The slot `functional` contains information on PLEASE FINISH THIS.

Please refer to the vignettes and the examples in the **yuimadocs** package for more informations.

**Value**

an object of `yuima-class`.

**Author(s)**

The YUIMA Project Team

**Examples**

```
# Creation of a yuima object with all slots for a
# stochastic differential equation
#  $dX_t^e = -\theta_2 * X_t^e * dt + \theta_1 * dW_t$ 
diffusion <- matrix(c("theta1"), 1, 1)
drift <- c("-1*theta2*x")
ymodel <- setModel(drift=drift, diffusion=diffusion)
n <- 100
ysamp <- setSampling(Terminal=1, n=n)

yuima <- setYuima(model=ymodel, sampling=ysamp)

str(yuima)
```

---

simFunctional	<i>Calculate the value of functional</i>
---------------	--

---

**Description**

Calculate the value of functional associated with sde by Euler scheme.

**Usage**

```
simFunctional(yuima, expand.var="e")
Fnorm(yuima, expand.var="e")
F0(yuima, expand.var="e")
```

**Arguments**

yuima	a yuima object containing model, functional and data.
expand.var	default expand.var="e".

**Details**

Calculate the value of functional of interest. Fnorm returns normalized one, and F0 returns the value for the case small parameter  $\epsilon = 0$ . In simFunctional and Fnorm, yuima MUST contains the 'data' slot (X in legacy version)

**Value**

Fe	a real value
----	--------------

**Note**

we need to fix this routine.

**Author(s)**

YUIMA Project Team

**Examples**

```
set.seed(123)
# to the Black-Scholes economy:
#  $dX_t^e = X_t^e * dt + e * X_t^e * dW_t$ 
diff.matrix <- matrix( c("x*e"), 1,1)
model <- setModel(drift = c("x"), diffusion = diff.matrix)
# call option is evaluated by averating
#  $\max\{ (1/T) * \int_0^T X_t^e dt, 0\}$ , the first argument is the functional of interest:
Terminal <- 1
xinit <- c(1)
f <- list( c(expression(x/Terminal)), c(expression(0)))
F <- 0
```

```

division <- 1000
e <- .3
samp <- setSampling(Terminal = Terminal, n = division)
yuima <- setYuima(model = model,sampling = samp)
yuima <- setFunctional( yuima, xinit=xinit, f=f,F=F,e=e)
# evaluate the functional value

yuima <- simulate(yuima,xinit=xinit,true.par=e)
Fe <- simFunctional(yuima)
Fe
Fnorm <- Fnorm(yuima)
Fnorm

```

---

simulate

---

*Simulator function for multi-dimensional stochastic processes*


---

### Description

Simulate multi-dimensional stochastic processes.

### Usage

```

simulate(object, nsim=1, seed=NULL, xinit, true.parameter, space.discretized = FALSE,
  increment.W = NULL, increment.L = NULL, hurst, methodfGn = "WoodChan",
  sampling=sampling, subsampling=subsampling, ...)

```

### Arguments

object	an <a href="#">yuima-class</a> , <a href="#">yuima.model-class</a> or <a href="#">yuima.carma-class</a> object.
xinit	initial value vector of state variables.
true.parameter	named list of parameters.
space.discretized	flag to switch to space-discretized Euler Maruyama method.
increment.W	to specify Wiener increment for each time tics in advance.
increment.L	to specify Levy increment for each time tics in advance.
nsim	Not used yet. Included only to match the standard <code>genenirc</code> in package <code>stats</code> .
seed	Not used yet. Included only to match the standard <code>genenirc</code> in package <code>stats</code> .
hurst	value of Hurst parameter for simulation of the fGn. Overrides the specified <code>hurst</code> slot.
methodfGn	simulation methods for fractional Gaussian noise.
...	passed to <a href="#">setSampling</a> to create a sampling
sampling	a <a href="#">yuima.sampling-class</a> object.
subsampling	a <a href="#">yuima.sampling-class</a> object.

**Details**

simulate is a function to solve SDE using the Euler-Maruyama method. This function supports usual Euler-Maruyama method for multidimensional SDE, and space discretized Euler-Maruyama method for one dimensional SDE.

It simulates solutions of stochastic differential equations with Gaussian noise, fractional Gaussian noise awith/without jumps.

If a `yuima-class` object is passed as input, then the sampling information is taken from the slot `sampling` of the object. If a `yuima.carma-class` object, a `yuima.model-class` object or a `yuima-class` object with missing `sampling` slot is passed as input the `sampling` argument is used. If this argument is missing then the sampling structure is constructed from `Initial`, `Terminal`, etc. arguments (see `setSampling` for details on how to use these arguments).

**Value**

yuima            a yuima-class object.

**Note**

There may be missing information in the simulate description. Please contribute with suggestions and fixings.

**Author(s)**

The YUIMA Project Team

**Examples**

```
set.seed(123)

# Path-simulation for 1-dim diffusion process.
# dx_t = -0.3*x_t*dt + dW_t
mod <- setModel(drift="-0.3*y", diffusion=1, solve.variable=c("y"))
str(mod)

# Set the model in an `yuima' object with a sampling scheme.
T <- 1
n <- 1000
samp <- setSampling(Terminal=T, n=n)
ou <- setYuima(model=mod, sampling=samp)

# Solve SDEs using Euler-Maruyama method.
par(mfrow=c(3,1))
ou <- simulate(ou, xinit=1)
plot(ou)

set.seed(123)
ouB <- simulate(mod, xinit=1, sampling=samp)
plot(ouB)
```

```

set.seed(123)
ouC <- simulate(mod, xinit=1, Terminal=1, n=1000)
plot(ouC)

par(mfrow=c(1,1))

# Path-simulation for 1-dim diffusion process.
#  $dX_t = \theta X_t dt + dW_t$ 
mod1 <- setModel(drift="theta*y", diffusion=1, solve.variable=c("y"))
str(mod1)
ou1 <- setYuima(model=mod1, sampling=samp)

# Solve SDEs using Euler-Maruyama method.
ou1 <- simulate(ou1, xinit=1, true.p = list(theta=-0.3))
plot(ou1)

## Not run:

# A multi-dimensional (correlated) diffusion process.
# To describe the following model:
#  $X=(X_1, X_2, X_3)$ ;  $dX_t = U(t, X_t)dt + V(t)dW_t$ 
# For drift coefficient
U <- c("-x1", "-2*x2", "-t*x3")
# For diffusion coefficient of X1
v1 <- function(t) 0.5*sqrt(t)
# For diffusion coefficient of X2
v2 <- function(t) sqrt(t)
# For diffusion coefficient of X3
v3 <- function(t) 2*sqrt(t)
# correlation
rho <- function(t) sqrt(1/2)
# coefficient matrix for diffusion term
V <- matrix( c( "v1(t)",
                "v2(t) * rho(t)",
                "v3(t) * rho(t)",
                "",
                "v2(t) * sqrt(1-rho(t)^2)",
                "",
                "",
                "",
                "v3(t) * sqrt(1-rho(t)^2)"
              ), 3, 3)
# Model sde using "setModel" function
cor.mod <- setModel(drift = U, diffusion = V,
state.variable=c("x1", "x2", "x3"),
solve.variable=c("x1", "x2", "x3") )
str(cor.mod)

# Set the 'yuima' object.
cor.samp <- setSampling(Terminal=T, n=n)
cor <- setYuima(model=cor.mod, sampling=cor.samp)

```



```

# Solve SDEs using Euler-Maruyama method.
set.seed(123)
cor <- simulate(cor)
plot(cor)

# A non-negative process (CIR process)
# dXt= a*(c-y)*dt + b*sqrt(Xt)*dWt
sq <- function(x){y = 0;if(x>0){y = sqrt(x);};return(y);}
model<- setModel(drift="0.8*(0.2-x)",
  diffusion="0.5*sq(x)",solve.variable=c("x"))
T<-10
n<-1000
sampling <- setSampling(Terminal=T,n=n)
yuima<-setYuima(model=model, sampling=sampling)
cir<-simulate(yuima,xinit=0.1)
plot(cir)

# solve SDEs using Space-discretized Euler-Maruyama method
v4 <- function(t,x){
  return(0.5*(1-x)*sqrt(t))
}
mod_sd <- setModel(drift = c("0.1*x1", "0.2*x2"),
  diffusion = c("v1(t)", "v4(t,x2)"),
  solve.var=c("x1", "x2")
)
samp_sd <- setSampling(Terminal=T, n=n)
sd <- setYuima(model=mod_sd, sampling=samp_sd)
sd <- simulate(sd, xinit=c(1,1), space.discretized=TRUE)
plot(sd)

## example of simulation by specifying increments
## Path-simulation for 1-dim diffusion process
## dXt = -0.3*Xt*dt + dWt

mod <- setModel(drift="-0.3*y", diffusion=1,solve.variable=c("y"))
str(mod)

## Set the model in an `yuima' object with a sampling scheme.
Terminal <- 1
n <- 500
mod.sampling <- setSampling(Terminal=Terminal, n=n)
yuima.mod <- setYuima(model=mod, sampling=mod.sampling)

##use original increment
delta <- Terminal/n
my.dW <- rnorm(n * yuima.mod@model@noise.number, 0, sqrt(delta))
my.dW <- t(matrix(my.dW, nrow=n, ncol=yuima.mod@model@noise.number))

## Solve SDEs using Euler-Maruyama method.
yuima.mod <- simulate(yuima.mod,
  xinit=1,

```

```

                                space.discretized=FALSE,
                                increment.W=my.dW)
if( !is.null(yuima.mod) ){
  dev.new()
  # x11()
  plot(yuima.mod)
}

## A multi-dimensional (correlated) diffusion process.
## To describe the following model:
##  $X=(X1,X2,X3)$ ;  $dX_t = U(t,X_t)dt + V(t)dW_t$ 
## For drift coefficient
U <- c("-x1", "-2*x2", "-t*x3")
## For process 1
diff.coef.1 <- function(t) 0.5*sqrt(t)
## For process 2
diff.coef.2 <- function(t) sqrt(t)
## For process 3
diff.coef.3 <- function(t) 2*sqrt(t)
## correlation
cor.rho <- function(t) sqrt(1/2)
## coefficient matrix for diffusion term
V <- matrix( c( "diff.coef.1(t)",
                "diff.coef.2(t) * cor.rho(t)",
                "diff.coef.3(t) * cor.rho(t)",
                "",
                "diff.coef.2(t)",
                "diff.coef.3(t) * sqrt(1-cor.rho(t)^2)",
                "diff.coef.1(t) * cor.rho(t)",
                "",
                "diff.coef.3(t)"
              ), 3, 3)
## Model sde using "setModel" function
cor.mod <- setModel(drift = U, diffusion = V,
                   solve.variable=c("x1","x2","x3") )
str(cor.mod)
## Set the 'yuima' object.
set.seed(123)
obj.sampling <- setSampling(Terminal=Terminal, n=n)
yuima.obj <- setYuima(model=cor.mod, sampling=obj.sampling)

##use original dW
my.dW <- rnorm(n * yuima.obj@model@noise.number, 0, sqrt(delta))
my.dW <- t(matrix(my.dW, nrow=n, ncol=yuima.obj@model@noise.number))

## Solve SDEs using Euler-Maruyama method.
yuima.obj.path <- simulate(yuima.obj, space.discretized=FALSE,
                          increment.W=my.dW)
if( !is.null(yuima.obj.path) ){
  dev.new()
  # x11()
  plot(yuima.obj.path)
}

```

```

##:: sample for Levy process ("CP" type)
## specify the jump term as c(x,t)dz
obj.model <- setModel(drift=c("-theta*x"), diffusion="sigma",
jump.coeff="1", measure=list(intensity="1", df=list("dnorm(z, 0, 1)")),
measure.type="CP", solve.variable="x")

##:: Parameters
lambda <- 3
theta <- 6
sigma <- 1
xinit <- runif(1)
N <- 500
h <- N^(-0.7)
eps <- h/50
n <- 50*N
T <- N*h

set.seed(123)
obj.sampling <- setSampling(Terminal=T, n=n)
obj.yuima <- setYuima(model=obj.model, sampling=obj.sampling)
X <- simulate(obj.yuima, xinit=xinit, true.parameter=list(theta=theta, sigma=sigma))
dev.new()
plot(X)

##:: sample for Levy process ("CP" type)
## specify the jump term as c(x,t,z)
## same plot as above example
obj.model <- setModel(drift=c("-theta*x"), diffusion="sigma",
jump.coeff="z", measure=list(intensity="1", df=list("dnorm(z, 0, 1)")),
measure.type="CP", solve.variable="x")

set.seed(123)
obj.sampling <- setSampling(Terminal=T, n=n)
obj.yuima <- setYuima(model=obj.model, sampling=obj.sampling)
X <- simulate(obj.yuima, xinit=xinit, true.parameter=list(theta=theta, sigma=sigma))
dev.new()
plot(X)

##:: sample for Levy process ("code" type)
##  $dX_{\{t\}} = -x dt + dZ_t$ 
obj.model <- setModel(drift="-x", xinit=1, jump.coeff="1", measure.type="code",
measure=list(df="rIG(z, 1, 0.1)"))
obj.sampling <- setSampling(Terminal=10, n=10000)
obj.yuima <- setYuima(model=obj.model, sampling=obj.sampling)
result <- simulate(obj.yuima)
dev.new()
plot(result)

```

```

##:: sample for multidimensional Levy process ("code" type)
## dx = (theta - A X)dt + dZ,
##   theta=(theta_1, theta_2) = c(1,.5)
##   A=[a_ij], a_11 = 2, a_12 = 1, a_21 = 1, a_22=2
require(yuima)
x0 <- c(1,1)
beta <- c(.1,.1)
mu <- c(0,0)
delta0 <- 1
alpha <- 1
Lambda <- matrix(c(1,0,0,1),2,2)
cc <- matrix(c(1,0,0,1),2,2)
obj.model <- setModel(drift=c("1 - 2*x1-x2",".5-x1-2*x2"), xinit=x0,
  solve.variable=c("x1","x2"), jump.coeff=cc, measure.type="code",
  measure=list(df="rNIG(z, alpha, beta, delta0, mu, Lambda)"))
obj.sampling <- setSampling(Terminal=10, n=10000)
obj.yuima <- setYuima(model=obj.model, sampling=obj.sampling)
result <- simulate(obj.yuima,true.par=list( alpha=alpha,
  beta=beta, delta0=delta0, mu=mu, Lambda=Lambda))
plot(result)

# Path-simulation for a Carma(p=2,q=1) model driven by a Brownian motion:
carma1<-setCarma(p=2,q=1)
str(carma1)

# Set the sampling scheme
samp<-setSampling(Terminal=100,n=10000)

# Set the values of the model parameters
par.carma1<-list(b0=1,b1=2.8,a1=2.66,a2=0.3)

set.seed(123)
sim.carma1<-simulate(carma1,
  true.parameter=par.carma1,
  sampling=samp)

plot(sim.carma1)

# Path-simulation for a Carma(p=2,q=1) model driven by a Compound Poisson process.
carma1<-setCarma(p=2,
  q=1,
  measure=list(intensity="1",df=list("dnorm(z, 0, 1)")),
  measure.type="CP")

# Set Sampling scheme
samp<-setSampling(Terminal=100,n=10000)

# Fix carma parameters
par.carma1<-list(b0=1,

```

```

        b1=2.8,
        a1=2.66,
        a2=0.3)

set.seed(123)
sim.carma1<-simulate(carma1,
                    true.parameter=par.carma1,
                    sampling=samp)

plot(sim.carma1)

## End(Not run)

```

---

subsampling

*subsampling*


---

## Description

subsampling

## Usage

```
subsampling(x, sampling, ...)
```

## Arguments

`x` an [yuima-class](#) or [yuima.model-class](#) object.  
`sampling` a [yuima.sampling-class](#) object.  
`...` used to create a sampling structure

## Details

When subsampling on some grid of times, it may happen that no data is available at the given grid point. In this case it is possible to use several techniques. Different options are available specifying the argument, or the slot, interpolation:

"none" **or** "exact" no interpolation. If no data point exists at a given grid point, NA is returned in the subsampled data

"pt" **or** "previous" the first data on the left of the grid point instant is used.

"nt" **or** "next" the first data on the right of the grid point instant is used.

"lin" **or** "linear" the average of the values of the first data on the left and the first data to the right of the grid point instant is used.

## Value

yuima a [yuima.data-class](#) object.

**Author(s)**

The YUIMA Project Team

**Examples**

```
## Set a model
diff.coef.1 <- function(t, x1=0, x2) x2*(1+t)
diff.coef.2 <- function(t, x1, x2=0) x1*sqrt(1+t^2)
cor.rho <- function(t, x1=0, x2=0) sqrt((1+cos(x1*x2))/2)
diff.coef.matrix <- matrix(c("diff.coef.1(t,x1,x2)",
"diff.coef.2(t,x1,x2)*cor.rho(t,x1,x2)", "",
"diff.coef.2(t,x1,x2)*sqrt(1-cor.rho(t,x1,x2)^2)"),2,2)
cor.mod <- setModel(drift=c("", ""), diffusion=diff.coef.matrix,
solve.variable=c("x1", "x2"), xinit=c(3,2))
set.seed(111)

## We first simulate the two dimensional diffusion model
yuima.samp <- setSampling(Terminal=1, n=1200)
yuima <- setYuima(model=cor.mod, sampling=yuima.samp)
yuima.sim <- simulate(yuima)

plot(yuima.sim, plot.type="single")

## random sampling with exponential times
## one random sequence per time series
newsamp <- setSampling(
  random=list(rdist=c( function(x) rexp(x, rate=10),
  function(x) rexp(x, rate=20))) )
newdata <- subsampling(yuima.sim, sampling=newsamp)
points(get.zoo.data(newdata)[[1]],col="red")
points(get.zoo.data(newdata)[[2]],col="green")

plot(yuima.sim, plot.type="single")

## deterministic subsampling with different
## frequency for each time series
newsamp <- setSampling(delta=c(0.1,0.2))
newdata <- subsampling(yuima.sim, sampling=newsamp)
points(get.zoo.data(newdata)[[1]],col="red")
points(get.zoo.data(newdata)[[2]],col="green")
```

**Description**

These methods convert `yuima-class`, `yuima.model-class` or `yuima.carma-class` objects to character vectors with LaTeX markup.

**Usage**

```
## S3 method for class 'yuima'
toLatex(object,...)
## S3 method for class 'yuima.model'
toLatex(object,...)
## S3 method for class 'yuima.carma'
toLatex(object,...)
```

**Arguments**

```
object      object of a class yuima, yuima.model or yuima.carma.
...         currently not used.
```

**Details**

This method tries to convert a formal description of the model slot of the yuima object into a LaTeX formula. This is just a simple proof of concept and probably further LaTeX manipulations for use in papers. Copy and paste of the output of toLatex into a real LaTeX file should do the job.

**Examples**

```
# dXt = theta*Xt*dt + dWt
mod1 <- setModel(drift="theta*y", diffusion=1, solve.variable=c("y"))
str(mod1)
toLatex(mod1)

# A multi-dimensional (correlated) diffusion process.
# To describe the following model:
# X=(X1,X2,X3); dXt = U(t,Xt)dt + V(t)dWt
# For drift coefficient
U <- c("-x1", "-2*x2", "-t*x3")
# For diffusion coefficient of X1
v1 <- function(t) 0.5*sqrt(t)
# For diffusion coefficient of X2
v2 <- function(t) sqrt(t)
# For diffusion coefficient of X3
v3 <- function(t) 2*sqrt(t)
# correlation
rho <- function(t) sqrt(1/2)
# coefficient matrix for diffusion term
V <- matrix( c( "v1(t)",
               "v2(t) * rho(t)",
               "v3(t) * rho(t)",
               "",
               "v2(t) * sqrt(1-rho(t)^2)",
               "",
               "",
               "",
               "v3(t) * sqrt(1-rho(t)^2)"
             ), 3, 3)
# Model sde using "setModel" function
```

```

cor.mod <- setModel(drift = U, diffusion = V,
state.variable=c("x1","x2","x3"),
solve.variable=c("x1","x2","x3") )
str(cor.mod)
toLatex(cor.mod)

# A CARMA(p=3,q=1) process.
carma1<-setCarma(p=3,q=1,loc.par="c",scale.par="s")
str(carma1)
toLatex(carma1)

```

---

yuima-class

*Class for stochastic differential equations*


---

## Description

The yuima S4 class is a class of the **yuima** package.

## Details

The yuima-class object is the main object of the **yuima** package. Some of the slots may be missing.

The data slot contains the data, either empirical or simulated.

The model contains the description of the (statistical) model which is used to generate the data via different simulation schemes, to draw inference from the data or both.

The sampling slot contains information on how the data have been collected or how they should be generated.

The slot characteristic contains information on PLEASE FINISH THIS. The slot functional contains information on PLEASE FINISH THIS.

## Slots

**data:** an object of class [yuima.data-class](#)

**model:** an object of class [yuima.model-class](#)

**sampling:** an object of class [yuima.sampling-class](#)

**characteristic:** an object of class [yuima.characteristic-class](#)

**functional:** an object of class [yuima.functional-class](#)

## Methods

**new** signature(x = "yuima", data = "yuima.data", model = "yuima.model", sampling = "yuima.sampling", the function makes a copy of the prototype object from the class definition of [yuima-class](#), then calls the initialize method passing as arguments the newly created object and the remaining arguments.

**initialize** signature(x = "yuima", data = "yuima.data", model = "yuima.model", sampling = "yuima.sampling", makes a copy of each argument in the corresponding slots of the object x.



- get.data** signature(x = "yuima"): returns the content of the slot data.
- plot** signature(x = "yuima", ...): calls `plot` from the `zoo` package with argument `x@data@zoo.data`. Additional arguments ... are passed as is to the `plot` function.
- dim** signature(x = "yuima"): the number of SDEs in the yuima object.
- length** signature(x = "yuima"): a vector of length of each SDE described in the yuima object.
- cce** signature(x = "yuima"): calculates the asynchronous covariance estimator on the data contained in `x@data@zoo.data`. For more details see `cce`.
- llag** signature(x = "yuima"): calculates the lead lag estimate  $r$  on the data contained in `x@data@zoo.data`. For more details see `llag`.
- simulate** simulation method. For more information see `simulate`.
- cbind.yuima** signature(x = "yuima"): bind yuima.data object.

**Author(s)**

The YUIMA Project Team

---

yuima.carma-class      *Class for the mathematical description of CARMA(p,q) model*

---

**Description**

The `yuima.carma` class is a class of the `yuima` package that extends the `yuima.model-class`.

**Slots**

- info**: is an `carma.info-class` object that describes the structure of the CARMA(p,q) model.
- drift**: is an R expression which specifies the drift coefficient (a vector).
- diffusion**: is an R expression which specifies the diffusion coefficient (a matrix).
- hurst**: the Hurst parameter of the gaussian noise. If  $h=0.5$ , the process is Wiener otherwise it is fractional Brownian motion with that precise value of the Hurst index. Can be set to NA for further specification.
- jump.coeff**: a vector of expressions for the jump component.
- measure**: Levy measure for jump variables.
- measure.type**: Type specification for Levy measures.
- state.variable** a vector of names identifying the names used to denote the state variable in the drift and diffusion specifications.
- parameter**: which is a short name for "parameters", is an object of class `model.parameter-class`. For more details see `model.parameter-class` documentation page.
- state.variable**: identifies the state variables in the R expression.
- jump.variable**: identifies the variable for the jump coefficient.
- time.variable**: the time variable.

noise.number: denotes the number of sources of noise. Currently only for the Gaussian part.  
 equation.number: denotes the dimension of the stochastic differential equation.  
 dimension: the dimensions of the parameter given in the parameter slot.  
 solve.variable: identifies the variable with respect to which the stochastic differential equation has to be solved.  
 xinit: contains the initial value of the stochastic differential equation.  
 J.flag: wheather jump.coeff include jump.variable.

### Methods

**simulate** simulation method. For more information see [simulate](#).  
**toLatex** This method converts an object of yuima.carma-class to character vectors with LaTeX markup.  
**CarmaNoise** Recovering underlying Levy. For more information see [CarmaNoise](#).  
**qmle** Quasi maximum likelihood estimation procedure. For more information see [qmle](#).

### Author(s)

The YUIMA Project Team

---

yuima.carma.qmle-class

*Class for Quasi Maximum Likelihood Estimation of CARMA(p,q) model*

---

### Description

The yuima.carma.qmle class is a class of the **yuima** package that extends the mle-class of the **stats4** package.

### Slots

Incr.Lev: is an object of class [zoo](#) that contains the estimated increments of the noise obtained using [CarmaNoise](#).  
 model: is an object of of [yuima.carma-class](#).  
 logL.Incr: is an object of class `numeric` that contains the value of the log-likelihood for estimated Levy increments.  
 call: is an object of class `language`.  
 coef: is an object of class `numeric` that contains estimated parameters.  
 fullcoef: is an object of class `numeric` that contains estimated and fixed parameters.  
 vcov: is an object of class `matrix`.  
 min: is an object of class `numeric`.  
 minuslogl: is an object of class `function`.  
 method: is an object of class `character`.

**Methods**

**plot** Plot method for estimated increment of the noise.

**Methods mle** All methods for `mle-class` are available.

**Author(s)**

The YUIMA Project Team

---

`yuima.characteristic-class`

*Classe for stochastic differential equations characteristic scheme*

---

**Description**

The `yuima.characteristic` class is a class of the **yuima** package.

**Slots**

`equation.number`: The number of equations modeled in the `yuima` object.

`time.scale`: The time scale assumed in the `yuima` object.

**Author(s)**

The YUIMA Project Team

---

`yuima.CP.qmle-class`

*Class for Quasi Maximum Likelihood Estimation of Compound Poisson-based and SDE models*

---

**Description**

The `yuima.CP.qmle` class is a class of the **yuima** package that extends the `mle-class` of the **stats4** package.

**Slots**

`Jump.times`: a vector which contains the estimated time of jumps.

`Jump.values`: a vector which contains the jumps.

`X.values`: the value of the process at the jump times.

`model`: is an object of of `yuima.model-class`.

`call`: is an object of class `language`.

`coef`: is an object of class `numeric` that contains estimated parameters.

`fullcoef`: is an object of class `numeric` that contains estimated and fixed parameters.

vcov: is an object of class `matrix`.  
 min: is an object of class `numeric`.  
 minuslog1: is an object of class `function`.  
 method: is an object of class `character`.  
 model: is an object of class `yuima.model-class`.

## Methods

**plot** Plot method for plotting the jump times.  
**Methods mle** All methods for `mle-class` are available.

## Author(s)

The YUIMA Project Team

---

<code>yuima.data-class</code>	<i>Class "yuima.data" for the data slot of a "yuima" class object</i>
-------------------------------	---

---

## Description

The `yuima.data-class` is a class of the **yuima** package used to store the data which are hold in the slot `data` of an object of the `yuima-class`.

Objects from this class contain either true data or simulated data.

## Details

Objects in this class are created or initialized using the methods `new` or `initialize` or via the function `setData`. The preferred way to construct an object in this class is to use the function `setData`.

Objects in this class are used to store the data which are hold in the slot `data` of an object of the `yuima-class`.

Objects in this class contain two slots described here.

**original.data:** The slot `original.data` contains, as the name suggests, a copy of the original data passed by the user to methods `new` or `initialize` or to the function `setData`. It is intended for backup purposes.

**zoo.data:** When a new object of this class is created or initialized using the `original.data`, the package tries to convert `original.data` into an object of class `zoo`. Once coerced to `zoo`, the data are stored in the slot `zoo.data`.

If the conversion fails, the initialization or creation of the object fails.

Internally, the **yuima** package stores and operates on `zoo`-type objects.

If data are obtained by simulation, the `original.data` slot is usually empty.

**Slots**

`original.data`: The original data.  
`zoo.data`: A list of zoo format data.

**Methods**

**new** signature(`x = "yuima.data"`, `original.data`): the function makes a copy of the prototype object from the class definition of `yuima.data-class`, then calls the `initialize` method passing as arguments the newly created object and the `original.data`.

**initialize** signature(`x = "yuima.data"`, `original.data`): makes a copy of `original.data` into the slot `original.data` of `x` and tries to coerce `original.data` into an object of class `zoo`. The result is put in the slot `zoo.data` of `x`. If coercion fails, the `initialize` method fails as well.

**get.zoo.data** signature(`x = "yuima.data"`): returns the content of the slot `zoo.data` of `x`.

**plot** signature(`x = "yuima.data"`, ...): calls `plot` from the `zoo` package with argument `x@zoo.data`. Additional arguments ... are passed as is to the `plot` function.

**dim** signature(`x = "yuima.data"`): calls `dim` from the `zoo` package with argument `x@zoo.data`.

**length** signature(`x = "yuima.data"`): calls `length` from the `zoo` package with argument `x@zoo.data`.

**cce** signature(`x = "yuima.data"`): calculates asynchronous covariance estimator on the data contained in `x@zoo.data`. For more details see `cce`.

**llag** signature(`x = "yuima.data"`): calculates lead lag estimate on the data contained in `x@zoo.data`. For more details see `llag`.

**cbind.yuima** signature(`x = "yuima.data"`): bind `yuima.data` object.

**Author(s)**

The YUIMA Project Team

---

yuima.functional-class

*Classes for stochastic differential equations data object*

---

**Description**

The `yuima.functional` class is a class of the **yuima** package.

**Author(s)**

YUIMA Project

---

yuima.model-class	<i>Classes for the mathematical description of stochastic differential equations</i>
-------------------	--

---

## Description

The `yuima.model` class is a class of the **yuima** package.

## Slots

`drift`: is an R expression which specifies the drift coefficient (a vector).

`diffusion`: is an R expression which specifies the diffusion coefficient (a matrix).

`hurst`: the Hurst parameter of the gaussian noise. If  $h=0.5$ , the process is Wiener otherwise it is fractional Brownian motion with that precise value of the Hurst index. Can be set to NA for further specification.

`jump.coeff`: a matrix of expressions for the jump component.

`measure`: Levy measure for jump variables.

`measure.type`: Type specification for Levy measures.

**state.variable** a vector of names identifying the names used to denote the state variable in the drift and diffusion specifications.

`parameter`: which is a short name for “parameters”, is an object of class `model.parameter-class`. For more details see `model.parameter-class` documentation page.

`state.variable`: identifies the state variables in the R expression.

`jump.variable`: identifies the variable for the jump coefficient.

`time.variable`: the time variable.

`noise.number`: denotes the number of sources of noise. Currently only for the Gaussian part.

`equation.number`: denotes the dimension of the stochastic differential equation.

`dimension`: the dimensions of the parameter given in the parameter slot.

`solve.variable`: identifies the variable with respect to which the stochastic differential equation has to be solved.

`xinit`: contains the initial value of the stochastic differential equation.

`J.flag`: wheather `jump.coeff` include `jump.variable`.

## Author(s)

The YUIMA Project Team

---

yuima.poisson-class	<i>Class for the mathematical description of Compound Poisson processes</i>
---------------------	---

---

## Description

The `yuima.poisson` class is a class of the **yuima** package that extends the `yuima.model-class`.

## Slots

`drift`: always `expression((0))`.

`diffusion`: a list of `expression((0))`.

`hurst`: always `h=0.5`, but ignored for this model.

`jump.coeff`: set according to scale in `setPoisson`.

`measure`: a list containing the intensity measure and the jump distribution.

`measure.type`: always "CP".

**state.variable** a vector of names identifying the names used to denote the state variable in the drift and diffusion specifications.

`parameter`: which is a short name for "parameters", is an object of class `model.parameter-class`. For more details see `model.parameter-class` documentation page.

`state.variable`: identifies the state variables in the R expression.

`jump.variable`: identifies the variable for the jump coefficient.

`time.variable`: the time variable.

`noise.number`: denotes the number of sources of noise.

`equation.number`: denotes the dimension of the stochastic differential equation.

`dimension`: the dimensions of the parameter given in the parameter slot.

`solve.variable`: identifies the variable with respect to which the stochastic differential equation has to be solved.

`xinit`: contains the initial value of the stochastic differential equation.

`J.flag`: wheather `jump.coeff` include `jump.variable`.

## Methods

**simulate** simulation method. For more information see `simulate`.

**qmle** Quasi maximum likelihood estimation procedure. For more information see `qmle`.

## Author(s)

The YUIMA Project Team

---

yuima.sampling-class *Classes for stochastic differential equations sampling scheme*

---

### Description

The `yuima.sampling` class is a class of the **yuima** package.

### Details

This object is created by `setSampling` or as a result of a simulation scheme by the `simulate` function or after subsampling via the function `subsampling`.

### Slots

**Initial:** initial time of the grid.

**Terminal:** terminal time fo the grid.

**n:** the number of observations - 1.

**delta:** in case of a regular grid is the mesh.

**grid:** the grid of times.

**random:** either FALSE or the distribution of the random times.

**regular:** indicator of whether the grid is regular or not. For internal use only.

**sdelta:** in case of a regular space grid it is the mesh.

**sgrid:** the grid in space.

**oindex:** in case of interpolation, a vector of indexes corresponding to the original observations used for the approximation.

**interpolation:** the name of the interpolation method used.

### Author(s)

The YUIMA Project Team



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