

Package ‘clusterSim’

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cluster.Description	<i>Descriptive statistics calculated separately for each cluster and variable</i>
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Description

Descriptive statistics calculated separately for each cluster and variable: arithmetic mean and standard deviation, median and median absolute deviation, mode

Usage

```
cluster.Description(x, cl, sdType="sample")
```

Arguments

x	matrix or dataset
cl	a vector of integers indicating the cluster to which each object is allocated
sdType	type of standard deviation: for "sample" (n-1) or for "population" (n)

Value

Three-dimensional array:

First dimension contains cluster number

Second dimension contains original coordinate (variable) number from matrix or data set

Third dimension contains number from 1 to 5:

1 - arithmetic mean

2 - standard deviation

3 - median

4 - median absolute deviation (mad)

5 - mode (value of the variable which has the largest observed frequency. If several are tied, the N.A. value is returned. This formula is applicable for nominal and ordinal data only).

For example:

```
desc<-cluster.Description(x,cl)
```

```
desc[2,4,2] - standard deviation of fourth coordinate of second cluster
```

```
desc[3,1,5] - mode of first coordinate (variable) of third cluster
```

```
desc[1,,] - all statistics for all dimensions (variables) of first cluster
```

```
desc[,3] - medians of all dimensions (variables) for each cluster
```

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<http://keii.ue.wroc.pl/clusterSim>

See Also

[cluster.Sim](#), [mean](#), [sd](#), [median](#), [mad](#)

Examples

```
library(clusterSim)
data(data_ratio)
cl <- pam(data_ratio,5)
desc <- cluster.Description(data_ratio,cl$cluster)
print(desc)
```

cluster.Gen

Random cluster generation with known structure of clusters

Description

Random cluster generation with known structure of clusters (optionally with noisy variables and outliers)

Usage

```
cluster.Gen(numObjects=50, means=NULL, cov=NULL, fixedCov=TRUE,
            model=1, dataType="m", numCategories=NULL,
            numNoisyVar=0, numOutliers=0, rangeOutliers=
            c(1,10), inputType="csv2", inputHeader=TRUE,
            inputRowNames=TRUE, outputCsv="", outputCsv2="",
            outputColNames=TRUE, outputRowNames=TRUE)
```

Arguments

numObjects	number of objects in each cluster - positive integer value or vector with the same size as <i>nrow(means)</i> , e.g. <code>numObjects=c(50,20)</code>
means	matrix of cluster means (e.g. <code>means=matrix(c(0,8,0,8),2,2)</code>). If <code>means = NULL</code> matrix should be read from <i>means\<modelNumber>.csv file</i>
cov	covariance matrix (the same for each cluster, e.g. <code>cov=matrix(c(1, 0, 0, 1), 2, 2)</code>). If <code>cov=NULL</code> matrix should be read from <i>cov\<modelNumber>.csv file</i> . Note: you cannot use this argument for generation of clusters with different covariance matrices. Those kind of generation should be done by setting <code>fixedCov</code> to <code>FALSE</code> and using appropriate model
model	model number, <code>model=1</code> - no cluster structure. Observations are simulated from uniform distribution over the unit hypercube in number of dimensions (variables) given in <code>numNoisyVar</code> argument; <code>model=2</code> - means and covariances are taken from arguments <code>means</code> and <code>cov</code> (see Example 1); <code>model=3,4,...,20</code> - see file ../doc/clusterGen_details.pdf ;

model=21, 22, . . . - if fixedCov=TRUE means should be read from *means_<modelName>.csv* and covariance matrix for all clusters should be read from *cov_<modelName>.csv* and if fixedCov=FALSE means should be read from *means_<modelName>.csv* and covariance matrices should be read separately for each cluster from *cov_<modelName>_<clusterNumber>.csv*

fixedCov	if fixedCov=TRUE covariance matrix for all clusters is the same and if fixedCov=FALSE each cluster is generated from different covariance matrix - see model
dataType	"m" - metric (ratio, interval), "o" - ordinal, "s" - symbolic interval
numCategories	number of categories (for ordinal data only). Positive integer value or vector with the same size as <i>ncol(means)</i> plus number of noisy variables.
numNoisyVar	number of noisy variables. For model=1 it means number of variables
numOutliers	number of outliers (for metric and symbolic interval data only). If a positive integer - number of outliers, if value from <0,1> - percentage of outliers in whole data set
rangeOutliers	range for outliers (for metric and symbolic interval data only). The default range is [1, 10].The outliers are generated independently for each variable for the whole data set from uniform distribution. The generated values are randomly added to maximum of <i>j</i> -th variable or subtracted from minimum of <i>j</i> -th variable
inputType	"csv" - a dot as decimal point or "csv2" - a comma as decimal point in <i>means_<modelName>.csv</i> and <i>cov_<modelName>.csv</i> files
inputHeader	inputHeader=TRUE indicates that input files (<i>means_<modelName>.csv</i> ; <i>cov_<modelName...>.csv</i>) contain header row
inputRowNames	inputRowNames=TRUE indicates that input files (<i>means_<modelName>.csv</i> ; <i>cov_<modelName...>.csv</i>) contain first column with row names or with number of objects (positive integer values)
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)
outputColNames	outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names
outputRowNames	outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Details

See file [../doc/clusterGen_details.pdf](#) for further details

Value

clusters cluster number for each object, for model=1 each object belongs to its own cluster thus this variable contains objects numbers

data generated data: for metric and ordinal data - matrix with objects in rows and variables in columns; for symbolic interval data three-dimensional structure: first dimension represents object number, second - variable number and third dimension contains lower- and upper-bounds of intervals

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Examples

```
# Example 1
library(clusterSim)
means <- matrix(c(0,7,0,7),2,2)
cov <- matrix(c(1,0,0,1),2,2)
grnd <- cluster.Gen(numObjects=60,means=means,cov=cov,model=2,
numOutliers=8)
colnames <- c("red","blue","green")
grnd$clusters[grnd$clusters==0]<-length(colnames)
plot(grnd$data,col=colnames[grnd$clusters],ask=TRUE)

# Example 2
library(clusterSim)
grnd <- cluster.Gen(50,model=4,dataType="m",numNoisyVar=2)
data <- as.matrix(grnd$data)
colnames <- c("red","blue","green")
plot(grnd$data,col=colnames[grnd$clusters],ask=TRUE)

# Example 3
library(clusterSim)
grnd<-cluster.Gen(50,model=4,dataType="o",numCategories=7, numNoisyVar=2)
plotCategorical(grnd$data,,grnd$clusters,ask=TRUE)

# Example 4 (1 nonnoisy variable and 2 noisy variables, 3 clusters)
```

```

library(clusterSim)
grnd <- cluster.Gen(c(40,60,20), model=2, means=c(2,14,25),
cov=c(1.5,1.5,1.5),numNoisyVar=2)
colornames <- c("red","blue","green")
plot(grnd$data,col=colornames[grnd$clusters],ask=TRUE)

# Example 5
library(clusterSim)
grnd <- cluster.Gen(c(20,35,20,25),model=14,dataType="m",numNoisyVar=1,
fixedCov=FALSE, numOutliers=0.1, outputCsv2="data14.csv")
data <- as.matrix(grnd$data)
colornames <- c("red","blue","green","brown","black")
grnd$clusters[grnd$clusters==0]<-length(colornames)
plot(grnd$data,col=colornames[grnd$clusters],ask=TRUE)

# Example 6 (this example needs files means_24.csv)
# and cov_24.csv to be placed in working directory
# library(clusterSim)
# grnd<-cluster.Gen(c(50,80,20),model=24,dataType="m",numNoisyVar=1,
# numOutliers=10, rangeOutliers=c(1,5))
# print(grnd)
# data <- as.data.frame(grnd$data)
# colornames<-c("red","blue","green","brown")
# grnd$clusters[grnd$clusters==0]<-length(colornames)
# plot(data,col=colornames[grnd$clusters],ask=TRUE)

# Example 7 (this example needs files means_25.csv and cov_25_1.csv)
# cov_25_2.csv, cov_25_3.csv, cov_25_4.csv, cov_25_5.csv
# to be placed in working directory
# library(clusterSim)
# grnd<-cluster.Gen(c(40,30,20,35,45),model=25,numNoisyVar=3,fixedCov=F)
# data <- as.data.frame(grnd$data)
# colornames<-c("red","blue","green","magenta","brown")
# plot(data,col=colornames[grnd$clusters],ask=TRUE)

```

cluster.Sim

Determination of optimal clustering procedure for a data set

Description

Determination of optimal clustering procedure for a data set by varying all combinations of normalization formulas, distance measures, and clustering methods

Usage

```

cluster.Sim (x,p,minClusterNo,maxClusterNo,icq="S",outputHtml="",
outputCsv="",outputCsv2="",normalizations=NULL,
distances=NULL,methods=NULL)

```

Arguments

x	matrix or dataset
p	path of simulation: 1 - ratio data, 2 - interval or mixed (ratio & interval) data, 3 - ordinal data, 4 - nominal data, 5 - binary data, 6 - ratio data without normalization, 7 - interval or mixed (ratio & interval) data without normalization, 8 - ratio data with k-means, 9 - interval or mixed (ratio & interval) data with k-means
minClusterNo	minimal number of clusters, between 2 and no. of objects - 1 (for G3: no. of objects - 2)
maxClusterNo	maximal number of clusters, between 2 and no. of objects - 1 (for G3: no. of objects - 2; for KL: no. of objects - 3), greater or equal minClusterNo
icq	Internal cluster quality index, "S" - Silhouette,"G1" - Calinski & Harabasz index, "G2" - Baker & Hubert index , "G3" - Hubert & Levine index, "KL" - Krzanowski & Lai index
outputHtml	optional, name of html file with results
outputCsv	optional, name of csv file with results
outputCsv2	optional, name of csv (comma as decimal point sign) file with results
normalizations	optional, vector of normalization formulas that should be used in procedure
distances	optional, vector of distance measures that should be used in procedure
methods	optional, vector of classification methods that should be used in procedure

Details

Parameter normalizations for each path may be the subset of the following values

path 1: "n6" to "n11" (if measurement scale of variables is ratio and transformed measurement scale of variables is ratio) or "n1" to "n5" (if measurement scale of variables is ratio and transformed measurement scale of variables is interval)

path 2: "n1" to "n5"

path 3 to 7 : "n0"

path 8: "n1" to "n11"

path 9: "n1" to "n5"

Parameter distances for each path may be the subset of the following values

path 1: "d1" to "d7" (if measurement scale of variables is ratio and transformed measurement scale of variables is ratio) or "d1" to "d5" (if measurement scale of variables is ratio and transformed measurement scale of variables is interval)

path 2: "d1" to "d5"

path 3: "d8"

path 4: "d9"

path 5: "b1" to "b10"

path 6: "d1" to "d7"

path 7: "d1" to "d5"

path 8 and 9: N.A.

Parameter methods for each path may be the subset of the following values

path 1 to 7 : "m1" to "m8"

path 8: "m9"

path 9: "m9"

See file [../doc/clusterSim_details.pdf](#) for further details

Value

result	optimal value of icq for all classifications
normalization	normalization used to obtain optimal value of icq
distance	distance measure used to obtain optimal value of icq
method	clustering method used to obtain optimal value of icq
classes	number of clusters for optimal value of icq
time	time of all calculations for path

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See Also

[data.Normalization](#), [dist.GDM](#), [dist.BC](#), [dist.SM](#), [index.G1](#), [index.G2](#),
[index.G3](#), [index.S](#), [index.KL](#), [hclust](#), [dist](#),

Examples

```

library(clusterSim)
# Commented due to long execution time
#data(data_ratio)
#cluster.Sim(data_ratio, 1, 2, 3, "G1", outputCsv="results1")
#data(data_interval)
#cluster.Sim(data_interval, 2, 2, 4, "G1", outputHtml="results2")
#data(data_ordinal)
#cluster.Sim(data_ordinal, 3, 2, 4,"G2", outputCsv2="results3")
#data(data_nominal)
#cluster.Sim(data_nominal, p=4, 2, 4, icq="G3", outputHtml="results4", methods=c("m2","m3","m5"))
#data(data_binary)
#cluster.Sim(data_binary, p=5, 2, 4, icq="S", outputHtml="results5", distances=c("b1","b3","b6"))
data(data_ratio)
cluster.Sim(data_ratio, 1, 2, 4,"G1", outputCsv="results6",normalizations=c("n1","n3"),
distances=c("d2","d5"),methods=c("m5","m3","m1"))

```

comparing.Partitions *Calculate agreement indices between two partitions*

Description

Calculate agreement indices between two partitions

Usage

```
comparing.Partitions(c11,c12,type="nowak")
```

Arguments

c11	A vector of integers (or letters) indicating the cluster to which each object is allocated for first clustering
c12	A vector of integers (or letters) indicating the cluster to which each object is allocated for second clustering
type	"rand" - for Rand index, "crand" - for adjusted Rand index or "nowak" for Nowak index

Details

See file [../doc/comparingPartitions_details.pdf](#) for further details.

Rand and adjusted Rand indices uses classAgreement function from e1071 library.

Value

Returns value of index.

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References

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Rand, W.M. (1971), *Objective criteria for the evaluation of clustering methods*, "Journal of the American Statistical Association", no. 336, 846-850.

See Also

[replication.Mod](#)

Examples

```
# Example 1
library(clusterSim)
dataSet<-cluster.Gen(model=5)
c1<-dataSet$clusters
c2<-kmeans(dataSet$data,2)$cluster
print(comparing.Partitions(c1,c2,type="rand"))

# Example 2
library(clusterSim)
data(data_patternGDM1)
z<-data.Normalization(data_patternGDM1,type="n1")
d<-dist.GDM(z,method="GDM1")
c1<-pam(d,3,diss=TRUE)$clustering
c2<-pam(d,4,diss=TRUE)$clustering
print(comparing.Partitions(c1,c2,type="crand"))

# Example 3
library(clusterSim)
data(data_patternGDM1)
z<-data.Normalization(data_patternGDM1,type="n9")
d<-dist.GDM(z,method="GDM1")
c1<-pam(d,3,diss=TRUE)$clustering
hc<-hclust(d, method="complete")
c2<-cutree(hc,k=3)
print(comparing.Partitions(c1,c2,type="nowak"))
```

data.Normalization *Types of variable (column) and object (row) normalization formulas*

Description

Types of variable (column) and object (row) normalization formulas

Usage

```
data.Normalization (x,type="n0",normalization="column")
```

Arguments

x	vector, matrix or dataset
type	type of normalization: n0 - without normalization n1 - standardization $((x-\text{mean})/\text{sd})$ n2 - positional standardization $((x-\text{median})/\text{mad})$ n3 - unitization $((x-\text{mean})/\text{range})$ n3a - positional unitization $((x-\text{median})/\text{range})$ n4 - unitization with zero minimum $((x-\text{min})/\text{range})$ n5 - normalization in range $<-1,1>$ $((x-\text{mean})/\text{max}(\text{abs}(x-\text{mean})))$ n5a - positional normalization in range $<-1,1>$ $((x-\text{median})/\text{max}(\text{abs}(x-\text{median})))$ n6 - quotient transformation (x/sd) n6a - positional quotient transformation (x/mad) n7 - quotient transformation (x/range) n8 - quotient transformation (x/max) n9 - quotient transformation (x/mean) n9a - positional quotient transformation (x/median) n10 - quotient transformation (x/sum) n11 - quotient transformation $(x/\text{sqrt}(\text{SSQ}))$ n12 - normalization $((x-\text{mean})/\text{sqrt}(\text{sum}((x-\text{mean})^2)))$ n12a - positional normalization $((x-\text{median})/\text{sqrt}(\text{sum}((x-\text{median})^2)))$ n13 - normalization with zero being the central point $((x-\text{midrange})/(\text{range}/2))$
normalization	"column" - normalization by variable, "row" - normalization by object

Details

See file [../doc/dataNormalization_details.pdf](#) for further details

Value

Normalized data

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References

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See Also

[cluster.Sim](#)

Examples

```
library(clusterSim)
data(data_ratio)
z1 <- data.Normalization(data_ratio,type="n1",normalization="column")
z2 <- data.Normalization(data_ratio,type="n10",normalization="row")
```

data_binary

Binary data

Description

Binary variables for eight people

Format

data.frame: 8 objects, 10 variables

Source

Kaufman, L., Rousseeuw, P.J. (1990), *Finding groups in data: an introduction to cluster analysis*, Wiley, New York, p. 24.

Examples

```
library(clusterSim)
data(data_binary)
cluster.Sim(data_binary, p=5, 2, 6, icq="S",
outputHtml="results5", distances=c("b1","b3","b6"))
```

data_interval	<i>Interval data</i>
---------------	----------------------

Description

Artificially generated interval data

Format

data.frame: 75 objects, 5 variables, 5-class structure

Source

Artificially generated data

Examples

```
library(clusterSim)
data(data_interval)
cluster.Sim(data_interval, 2, 2, 3, "G1", outputHtml="results2")
```

data_mixed	<i>Mixed data</i>
------------	-------------------

Description

Artificial mixed data

Format

data.frame: 25 objects, 4 variables (1, 3 - interval variables, 2 - ordinal variable, 4, nominal variable)

Source

Artificial data

Examples

```
library(clusterSim)
data(data_mixed)
r3 <- HINoV.Mod(data_mixed, type=c("m","n","m","n"), s=2, 3, distance="d1",
  method="complete", Index="cRAND")
print(r3$stopri)
plot(r3$stopri[,2], xlab="Variable number", ylab="topri", xaxt="n")
axis(1,at=c(1:max(r3$stopri[,1])),labels=r3$stopri[,1])
```

data_nominal

Nominal data

Description

Artificial nominal data

Format

data.frame: 26 objects, 12 variables

Source

Artificial data

Examples

```
library(clusterSim)
data(data_nominal)
cluster.Sim(data_nominal, p=4, 2, 5, icq="G3",
  outputHtml="results4", methods=c("m2","m3","m5"))
```

data_ordinal

Ordinal data

Description

Artificial ordinal data

Format

data.frame: 26 objects, 12 variables

Source

Artificial data

Examples

```
library(clusterSim)
data(data_ordinal)
cluster.Sim(data_ordinal, 3, 3, 12,"S",
outputCsv2="results3")
```

data_patternGDM1	<i>Metric data with 17 objects and 10 variables (8 stimulant variables, 2 destimulant variables)</i>
------------------	--

Description

Metric data with 17 objects and 10 variables (8 stimulant variables, 2 destimulant variables)

Data on the Polish voivodships, owing to the conditions of the population living in cities in 2007. The analysis includes the following variables:

x1 - dwellings in per cent fitted with water-line system,

x2 - dwellings in per cent fitted with lavatory,

x3 - dwellings in per cent fitted with bathroom,

x4 - dwellings in per cent fitted with gas-line system,

x5 - dwellings in per cent fitted with central heating,

x6 - average number of rooms per dwelling,

x7 - average number of persons per dwelling,

x8 - average number of persons per room,

x9 - usable floor space in square meter per dwelling,

x10 - usable floor space in square meter per person.

Types of performance variables:

x1 - x6, x9, x10 - stimulants,

x7, x8 - destimulants.

Format

data.frame: 17 objects, 10 variables

Source

Voivodships Statistical Yearbook, Poland 2008.

Examples

```
# Example 1
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
performanceVariable=c("s","s","s","s","s","s","d","d","s","s"),
scaleType="r",nomOptValues=NULL,weightsType<-"equal",weights=NULL,
normalization<-"n4",patternType<-"lower",patternCoordinates<-"manual",
patternManual<-c(0,0,0,0,0,"min","max","max","min","min"),
nominalTransfMethod <-NULL)
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p),xlim=c(max(gdm_p),min(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),xaxt="n",
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object",lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)

# Example 2
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
performanceVariable=c("s","s","s","s","s","s","d","d","s","s"),
scaleType="r",nomOptValues=NULL,weightsType<-"equal",weights=NULL,
normalization<-"n2",patternType<-"upper",
patternCoordinates<-"dataBounds",patternManual<-NULL,
nominalTransfMethod <-NULL)
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p),xlim=c(min(gdm_p),max(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),xaxt="n",
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
```

data_patternGDM2

Ordinal data with 27 objects and 6 variables (3 stimulant variables, 2 destimulant variables and 1 nominant variable)

Description

Ordinal data with 27 objects and 6 variables (3 stimulant variables, 2 destimulant variables and 1 nominant variable)

Residential housing properties were described by the following variables:

x1 - Location of environmental land, which is linked to a dwelling (1 - poor, 2 - inadequate, 3 - satisfactory, 4 - good, 5 - very good),

x2 - Standard utility of a dwelling (1 - bad, 2 - low, 3 - average, 4 - high),

x3 - Living conditions occurring on the land, which is linked to a dwelling (1 - bad, 2 - average, 3 - good),

x4 - Location of land, which is related to dwelling in the area of the city (1 - central, 2 - downtown, 3 - intermediate, 4 - peripheral),

x5 - Type of condominium (1 - low, 2 - large),

x6 - Area of land, which is related to dwelling (1 - below the contour of the building, 2 - outline of the building, 3 - the outline of the building with the environment acceptable, such as parking, playground, 4 - the outline of the building with the environment too much).

Types of performance variables:

x1, x2, x3 - stimulants,

x4, x5 - destimulants,

x6 - nominant (the nominal category: 3).

Format

data.frame: 27 objects, 6 variables

Source

data from real estate market

Examples

```
# Example 1
library(clusterSim)
data(data_patternGDM2)
res<-pattern.GDM2(data_patternGDM2,
performanceVariable=c("s","s","s","d","d","n"),
nomOptValues=c(NA,NA,NA,NA,NA,3), weightsType<-"equal", weights=NULL,
patternType="lower", patternCoordinates="manual",
patternManual=c("min","min",0,5,"max","max"),
nominalTransfMethod="symmetrical")
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p),xlim=c(max(gdm_p),min(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),
xaxt="n",xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object",lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)

# Example 2
library(clusterSim)
data(data_patternGDM2)
res<-pattern.GDM2(data_patternGDM2,
performanceVariable=c("s","s","s","d","d","n"),
nomOptValues=c(NA,NA,NA,NA,NA,3), weightsType<-"equal", weights=NULL,
patternType="upper", patternCoordinates="dataBounds",
patternManual=NULL, nominalTransfMethod="database")
print(res)
```

```
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p), xlim=c(min(gdm_p),max(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),
xaxt="n",xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)
```

data_ratio

Ratio data

Description

Artificially generated ratio data

Format

data.frame: 75 objects, 5 variables, 5-class structure

Source

Artificially generated data

Examples

```
library(clusterSim)
data(data_ratio)
c <- pam(data_ratio,10)
index.G1(data_ratio, c$clustering)
```

data_symbolic

Symbolic interval data

Description

Artificially generated symbolic interval data

Format

3-dimensional array: 125 objects, 6 variables, third dimension represents beginning and end of interval, 5-class structure

Source

Artificially generated data

Examples

```
library(clusterSim)
data(data_symbolic)
r<- HINoV.Symbolic(data_symbolic, u=5)
print(r$stopri)
plot(r$stopri[,2], xlab="Variable number", ylab="topri",
      xaxt="n", type="b")
axis(1,at=c(1:max(r$stopri[,1])),labels=r$stopri[,1])
```

dist.BC

Calculates Bray-Curtis distance measure for ratio data

Description

Calculates Bray-Curtis distance measure for ratio data

Usage

```
dist.BC (x)
```

Arguments

x matrix or dataset

Details

See file [../doc/distBC_details.pdf](#) for further details

Value

object with calculated distance

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References

Cormack, R.M. (1971), *A review of classification (with discussion)*, "Journal of the Royal Statistical Society", ser. A, part 3, 321-367.

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wrocław, p. 41.

See Also

[dist.GDM](#), [dist.SM](#), [dist](#)

Examples

```
library(clusterSim)
sampleData <- cbind(c(2,3,5),c(4,5,6),c(5,3,4))
d <- dist.BC(sampleData)
```

dist.GDM	<i>Calculates Generalized Distance Measure</i>
----------	--

Description

Calculates Generalized Distance Measure for variables measured on metric scale (ratio & interval) or ordinal scale

Usage

```
dist.GDM(x, method="GDM1", weightsType="equal", weights=NULL)
GDM(x, method="GDM1", weightsType="equal", weights=NULL)
GDM1(x, weightsType="equal", weights=NULL)
GDM2(x, weightsType="equal", weights=NULL)
```

Arguments

x	matrix or data set
method	GDM1 or GDM2 "GDM1" - metric scale (ratio & interval) "GDM2" - ordinal scale
weightsType	equal or different1 or different2 "equal" - equal weights "different1" - vector of different weights should satisfy conditions: each weight takes value from interval [0; 1] and sum of weights equals one "different2" - vector of different weights should satisfy conditions: each weight takes value from interval [0; m] and sum of weights equals m (m - the number of variables)
weights	vector of weights

Details

See file [../doc/distGDM_details.pdf](#) for further details

Value

object with calculated distance

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References

Walesiak, M. (1999), *Distance Measure for Ordinal Data*, "Argumenta Oeconomica", No. 2 (8), 167-173.

Jajuga, K., Walesiak, M., Bak, A. (2003), *On the general distance measure*, In: M. Schwaiger, O. Opitz (Eds.), *Exploratory data analysis in empirical research*, Springer-Verlag, Berlin, Heidelberg, 104-109.

Walesiak, M. (2006), *Uogólniona miara odległości w statystycznej analizie wielowymiarowej [The Generalized Distance Measure in multivariate statistical analysis]*, Wydawnictwo AE, Wrocław.

See Also

[dist.BC](#), [dist.SM](#), [dist](#)

Examples

```
#Example 1
library(clusterSim)
data(data_ratio)
d1 <- GDM(data_ratio, method="GDM1")
data(data_ordinal)
d2 <- GDM(data_ordinal, method="GDM2")
d3 <- GDM1(data_ratio)
d4 <- GDM2(data_ordinal)

#Example 2
library(clusterSim)
data(data_ratio)
d1w <- GDM(data_ratio, method="GDM1", weightsType="different1",
weights=c(0.4,0.1,0.3,0.15,0.05))
data(data_ordinal)
d2w <- GDM(data_ordinal, method="GDM2", weightsType="different2",
weights=c(1,3,0.5,1.5,1.8,0.2,0.4,0.6,0.2,0.4,0.9,1.5))
```

dist.SM

Calculates Sokal-Michener distance measure for nominal variables

Description

Calculates Sokal-Michener distance measure for nominal variables

Usage

```
dist.SM(x)
```

Arguments

x matrix or data set

Details

See file [../doc/distSM_details.pdf](#) for further details

Value

object with calculated distance

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References

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wrocław, p. 43.

Kaufman, L., Rousseeuw, P.J. (1990), *Finding groups in data: an introduction to cluster analysis*, Wiley, New York, p. 28.

See Also

[dist.GDM](#), [dist.BC](#), [dist](#)

Examples

```
library(clusterSim)
data(data_nominal)
d <- dist.SM(data_nominal)
```

dist.Symbolic *Calculates distance between symbolic interval-valued data*

Description

Calculates distance between symbolic interval-valued data for four distance types

Usage

```
dist.Symbolic(data, type="U_2", gamma=0.5, power=2)
```

Arguments

data	symbolic data
type	type of distance used for symbolic interval-valued data U_2 - Ichino and Yaguchi distance M - distance between points given by means of intervals (for interval-values variables), H - Hausdorff distance, S - sum of distances between all corresponding vertices of hyperrectangles given by symbolic objects with interval-valued variables)
gamma	parameter for calculating Ichino and Yaguchi distance
power	parameter (q) for calculating Ichino and Yaguchi distance

Details

See file [../doc/distSymbolic_details.pdf](#) for further details

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References

Billard, L., Diday, E. (2006), *Symbolic data analysis. Conceptual statistics and data mining*, Wiley, Chichester.

See Also

[dist.SM](#)

Examples

```
library(clusterSim)
dataSymbolic<-cluster.Gen(numObjects=10,model=5,dataType="s")$data
print(dist.Symbolic(dataSymbolic))
```

HINoV.Mod	<i>Modification of Carmone, Kara & Maxwell Heuristic Identification of Noisy Variables (HINoV) method</i>
-----------	---

Description

Modification of Heuristic Identification of Noisy Variables (HINoV) method

Usage

```
HINoV.Mod (x, type="metric", s = 2, u, distance=NULL,
method = "kmeans", Index ="cRAND")
```

Arguments

x	data matrix
type	"metric" (default) - all variables are metric (ratio, interval), "nonmetric" - all variables are nonmetric (ordinal, nominal) or vector containing for each variable value "m"(metric) or "n"(nonmetric) for mixed variables (metric and nonmetric), e.g. type=c("m", "n", "n", "m")
s	for metric data only: 1 - ratio data, 2 - interval or mixed (ratio & interval) data
u	number of clusters (for metric data only)
distance	NULL for kmeans method (based on data matrix) and nonmetric data for ratio data: "d1" - Manhattan, "d2" - Euclidean, "d3" - Chebychev (max), "d4" - squared Euclidean, "d5" - GDM1, "d6" - Canberra, "d7" - Bray-Curtis for interval or mixed (ratio & interval) data: "d1", "d2", "d3", "d4", "d5"
method	NULL for nonmetric data clustering method: "kmeans" (default) , "single", "ward", "complete", "average", "mcquitty", "median", "centroid", "pam"
Index	"cRAND" - corrected Rand index (default); "RAND" - Rand index

Details

See file [../doc/HINoVMod_details.pdf](#) for further details

Value

parim	$m \times m$ symmetric matrix (m - number of variables). Matrix contains pairwise corrected Rand (Rand) indices for partitions formed by the j -th variable with partitions formed by the l -th variable
topri	sum of rows of parim
stopri	ranked values of topri in decreasing order

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References

Carmone, F.J., Kara, A., Maxwell, S. (1999), *HINoV: a new method to improve market segment definition by identifying noisy variables*, "Journal of Marketing Research", November, vol. 36, 501-509.

Hubert, L.J., Arabie, P. (1985), *Comparing partitions*, "Journal of Classification", no. 1, 193-218.

Rand, W.M. (1971), *Objective criteria for the evaluation of clustering methods*, "Journal of the American Statistical Association", no. 336, 846-850.

Walesiak, M. (2005), *Variable selection for cluster analysis - approaches, problems, methods*, Plenary Session of the Committee on Statistics and Econometrics of the Polish Academy of Sciences, 15 March, Wrocław.

Walesiak, M., Dudek, A. (2008), *Identification of noisy variables for nonmetric and symbolic data in cluster analysis*, In: C. Preisach, H. Burkhardt, L. Schmidt-Thieme, R. Decker (Eds.), *Data analysis, machine learning and applications*, Springer-Verlag, Berlin, Heidelberg, 85-92.

See Also

[hclust](#), [kmeans](#), [dist](#), [dist.GDM](#), [dist.BC](#), [dist.SM](#), [cluster.Sim](#)

Examples

```
# for metric data
library(clusterSim)
data(data_ratio)
r1<- HINoV.Mod(data_ratio, type="metric", s=1, 4, method="kmeans",
  Index="cRAND")
print(r1$stopri)
plot(r1$stopri[,2],xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r1$stopri[,1])),labels=r1$stopri[,1])

# for nonmetric data
library(clusterSim)
data(data_nominal)
r2<- HINoV.Mod (data_nominal, type="nonmetric", Index = "cRAND")
print(r2$stopri)
plot(r2$stopri[,2], xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r2$stopri[,1])),labels=r2$stopri[,1])

# for mixed data
library(clusterSim)
data(data_mixed)
r3<- HINoV.Mod(data_mixed, type=c("m","n","m","n"), s=2, 3, distance="d1",
```

```

        method="complete", Index="cRAND")
print(r3$stopri)
plot(r3$stopri[,2], xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r3$stopri[,1])),labels=r3$stopri[,1])

```

HINoV.Symbolic	<i>Modification of Carmone, Kara & Maxwell Heuristic Identification of Noisy Variables (HINoV) method for symbolic interval data</i>
----------------	--

Description

Modification of Heuristic Identification of Noisy Variables (HINoV) method for symbolic interval data

Usage

```

HINoV.Symbolic(x, u=NULL, distance="H", method = "pam",
Index = "cRAND")

```

Arguments

x	symbolic interval data: a 3-dimensional table, first dimension represents object number, second dimension - variable number, and third dimension contains lower- and upper-bounds of intervals
u	number of clusters
distance	"M" - minimal distance between all vertices of hyper-cubes defined by symbolic interval variables; "H" - Hausdorff distance; "S" - sum of squares of distance between all vertices of hyper-cubes defined by symbolic interval variables
method	clustering method: "single", "ward", "complete", "average", "mcquitty", "median", "centroid", "pam" (default)
Index	"cRAND" - corrected Rand index (default); "RAND" - Rand index

Details

See file [../doc/HINoVSymbolic_details.pdf](#) for further details

Value

parim	$m \times m$ symmetric matrix (m - number of variables). Matrix contains pairwise corrected Rand (Rand) indices for partitions formed by the j -th variable with partitions formed by the l -th variable
topri	sum of rows of parim
stopri	ranked values of topri in decreasing order

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<http://keii.ue.wroc.pl/clusterSim>

References

Carmone, F.J., Kara, A., Maxwell, S. (1999), *HINoV: a new method to improve market segment definition by identifying noisy variables*, "Journal of Marketing Research", November, vol. 36, 501-509.

Hubert, L.J., Arabie, P. (1985), *Comparing partitions*, "Journal of Classification", no. 1, 193-218.

Rand, W.M. (1971), *Objective criteria for the evaluation of clustering methods*, "Journal of the American Statistical Association", no. 336, 846-850.

Walesiak, M., Dudek, A. (2008), *Identification of noisy variables for nonmetric and symbolic data in cluster analysis*, In: C. Preisach, H. Burkhardt, L. Schmidt-Thieme, R. Decker (Eds.), *Data analysis, machine learning and applications*, Springer-Verlag, Berlin, Heidelberg, 85-92.

See Also

[hclust](#), [kmeans](#), [cluster.Sim](#)

Examples

```
library(clusterSim)
data(data_symbolic)
r<- HINoV.Symbolic(data_symbolic, u=5)
print(r$stopri)
plot(r$stopri[,2], xlab="Variable number", ylab="topri",
xaxt="n", type="b")
axis(1,at=c(1:max(r$stopri[,1])),labels=r$stopri[,1])

#symbolic data from .csv file
#library(clusterSim)
#dsym<-as.matrix(read.csv2(file="csv/symbolic.csv"))
#dim(dsym)<-c(dim(dsym)[1],dim(dsym)[2]%/%2,2)
#r<- HINoV.Symbolic(dsym, u=5)
#print(r$stopri)
#plot(r$stopri[,2], xlab="Variable number", ylab="topri",
#xaxt="n", type="b")
#axis(1,at=c(1:max(r$stopri[,1])),labels=r$stopri[,1])
```

index.DB	<i>Calculates Davies-Bouldin's index</i>
----------	--

Description

Calculates Davies-Bouldin's cluster separation measure

Usage

```
index.DB(x, cl, d=NULL, centrotypes="centroids", p=2, q=2)
```

Arguments

x	data
cl	vector of integers indicating the cluster to which each object is allocated
d	optional distance matrix, used for calculations if centrotypes="medoids"
centrotypes	"centroids" or "medoids"
p	the power of the Minkowski distance between centroids or medoids of clusters: p=1 - Manhattan distance; p=2 - Euclidean distance
q	the power of dispersion measure of a cluster: q=1 - the average distance of objects in the r-th cluster to the centroid or medoid of the r-th cluster; q=2 - the standard deviation of the distance of objects in the r-th cluster to the centroid or medoid of the r-th cluster

Details

See file [../doc/indexDB_details.pdf](#) for further details

Thanks to prof. Christian Hennig <c.hennig@ucl.ac.uk> for finding and fixing the "immutable p" error

Value

DB	Davies-Bouldin's index
r	vector of maximal R values for each cluster
R	R matrix $(S_r+S_s)/d_{rs}$
d	matrix of distances between centroids or medoids of clusters
S	vector of dispersion measures for each cluster
centers	coordinates of centroids or medoids for all clusters

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References

Davies, D.L., Bouldin, D.W. (1979), *A cluster separation measure*, IEEE Transactions on Pattern Analysis and Machine Intelligence, vol. 1, no. 2, 224-227.

See Also

[index.G1](#), [index.G2](#), [index.G3](#), [index.S](#), [index.H](#), [index.Gap](#), [index.KL](#)

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
cl1 <- pam(data_ratio, 4)
d<-dist(data_ratio)
print(index.DB(data_ratio, cl1$clustering,d, centrotypes="medoids"))

# Example 2
library(clusterSim)
data(data_ratio)
cl2 <- pam(data_ratio, 5)
print(index.DB(data_ratio, cl2$clustering, centrotypes="centroids"))

# Example 3
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="euclidean")
# nc - number_of_clusters
min_nc=2
max_nc=8
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
  hc <- hclust(md, method="complete")
  cl2 <- cutree(hc, k=nc)
  res[nc-min_nc+1, 2] <- DB <- index.DB(data_ratio, cl2, centrotypes="centroids")$DB
  clusters <- rbind(clusters, cl2)
}
print(paste("min DB for", (min_nc:max_nc)[which.min(res[,2])], "clusters=", min(res[,2])))
print("clustering for min DB")
print(clusters[which.min(res[,2]),])
write.table(res, file="DB_res.csv", sep=";", dec=".", row.names=TRUE, col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="DB", xaxt="n")
axis(1, c(min_nc:max_nc))

# Example 4
library(clusterSim)
data(data_ordinal)
md <- dist.GDM(data_ordinal, method="GDM2")
# nc - number_of_clusters
```

```

min_nc=2
max_nc=6
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
hc <- hclust(md, method="complete")
c12 <- cutree(hc, k=nc)
res[nc-min_nc+1,2] <- DB <- index.DB(data_ordinal,c12,d=md,centrotypes="medoids")$DB
clusters <- rbind(clusters, c12)
}
print(paste("min DB for", (min_nc:max_nc)[which.min(res[,2])], "clusters=", min(res[,2])))
print("clustering for min DB")
print(clusters[which.min(res[,2]),])
write.table(res, file="DB_res.csv", sep=";", dec=".", row.names=TRUE, col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="DB", xaxt="n")
axis(1, c(min_nc:max_nc))

```

index.G1

Calculates Calinski-Harabasz pseudo F-statistic

Description

Calculates Calinski-Harabasz pseudo F-statistic

Usage

```
index.G1 (x,c1,d=NULL,centrotypes="centroids")
```

Arguments

x	data
c1	A vector of integers indicating the cluster to which each object is allocated
d	optional distance matrix, used for calculations if centrotypes="medoids"
centrotypes	"centroids" or "medoids"

Details

See file [../doc/indexG1_details.pdf](#) for further details.

thank to Nejc Ilc from University of Ljubljana for fixing error for one-element clusters.

Value

Calinski-Harabasz pseudo F-statistic

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References

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- Everitt, B.S., Landau, E., Leese, M. (2001), *Cluster analysis*, Arnold, London, p. 103.
- Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wrocław, p. 338.
- Gordon, A.D. (1999), *Classification*, Chapman & Hall/CRC, London, p. 62.
- Milligan, G.W., Cooper, M.C. (1985), *An examination of procedures of determining the number of cluster in a data set*, "Psychometrika", vol. 50, no. 2, 159-179.

See Also

[index.G2](#), [index.G3](#), [index.S](#), [index.H](#), [index.KL](#), [index.Gap](#), [index.DB](#)

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
c<- pam(data_ratio,10)
index.G1(data_ratio,c$clustering)

# Example 2
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="euclidean")
# nc - number_of_clusters
min_nc=2
max_nc=20
res <- array(0,c(max_nc-min_nc+1,2))
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
  cl2 <- pam(md, nc, diss=TRUE)
  res[nc-min_nc+1,2] <- G1 <- index.G1(data_ratio,cl2$cluster,centrotypes="centroids")
  clusters <- rbind(clusters, cl2$cluster)
}
print(paste("max G1 for", (min_nc:max_nc)[which.max(res[,2])], "clusters=", max(res[,2])))
print("clustering for max G1")
print(clusters[which.max(res[,2]),])
write.table(res, file="G1_res.csv", sep=";", dec=".", row.names=TRUE, col.names=FALSE)
```



```
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="G1", xaxt="n")  
axis(1, c(min_nc:max_nc))
```

`index.G2`*Calculates G2 internal cluster quality index*

Description

Calculates G2 internal cluster quality index - Baker & Hubert adaptation of Goodman & Kruskal's Gamma statistic

Usage

```
index.G2(d, cl)
```

Arguments

`d` 'dist' object
`cl` A vector of integers indicating the cluster to which each object is allocated

Details

See file [../doc/indexG2_details.pdf](#) for further details

Value

calculated G2 index

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References

- Everitt, B.S., Landau, E., Leese, M. (2001), *Cluster analysis*, Arnold, London, p. 104.
- Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wrocław, p. 339.
- Gordon, A.D. (1999), *Classification*, Chapman & Hall/CRC, London, p. 62.
- Hubert, L. (1974), *Approximate evaluation technique for the single-link and complete-link hierarchical clustering procedures*, "Journal of the American Statistical Association", vol. 69, no. 347, 698-704.
- Milligan, G.W., Cooper, M.C. (1985), *An examination of procedures of determining the number of cluster in a data set*, "Psychometrika", vol. 50, no. 2, 159-179.

See Also

[index.G1](#), [index.G3](#), [index.S](#), [index.H](#), [index.KL](#), [index.Gap](#), [index.DB](#)

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
d <- dist.GDM(data_ratio)
c <- pam(d, 5, diss = TRUE)
icq <- index.G2(d,c$clustering)
print(icq)

# Example 2
library(clusterSim)
data(data_ordinal)
d <- dist.GDM(data_ordinal, method="GDM2")
# nc - number_of_clusters
min_nc=2
max_nc=6
res <- array(0,c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
  cl2 <- pam(d, nc, diss=TRUE)
  res[nc-min_nc+1,2] <- G2 <- index.G2(d,cl2$cluster)
  clusters <- rbind(clusters,cl2$cluster)
}
print(paste("max G2 for", (min_nc:max_nc)[which.max(res[,2])], "clusters=", max(res[,2])))
print("clustering for max G2")
print(clusters[which.max(res[,2]),])
write.table(res, file="G2_res.csv", sep=";", dec=".", row.names=TRUE, col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="G2", xaxt="n")
axis(1, c(min_nc:max_nc))
```

index.G3

Calculates G3 internal cluster quality index

Description

Calculates G3 Hubert & Levine internal cluster quality index

Usage

```
index.G3(d,cl)
```

Arguments

d 'dist' object
 c1 A vector of integers indicating the cluster to which each object is allocated

Details

See file [../doc/indexG3_details.pdf](#) for further details

Value

calculated G3 index

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References

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wrocław, p. 339.
 Gordon, A.D. (1999), *Classification*, Chapman & Hall/CRC, London, p. 62.
 Milligan, G.W., Cooper, M.C. (1985), *An examination of procedures of determining the number of cluster in a data set*, "Psychometrika", vol. 50, no. 2, 159-179.

See Also

[index.G1](#), [index.G2](#), [index.S](#), [index.H](#), [index.KL](#), [index.Gap](#), [index.DB](#)

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
d <- dist.GDM(data_ratio)
c <- pam(d, 5, diss = TRUE)
icq <- index.G3(d,c$clustering)
print(icq)

# Example 2
library(clusterSim)
data(data_ordinal)
d <- dist.GDM(data_ordinal, method="GDM2")
# nc - number_of_clusters
min_nc=2
max_nc=6
res <- array(0,c(max_nc-min_nc+1, 2))
```

```

res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
hc <- hclust(d, method="complete")
c12 <- cutree(hc, k=nc)
res[nc-min_nc+1,2] <- G3 <- index.G3(d,c12)
clusters <- rbind(clusters,c12)
}
print(paste("min G3 for", (min_nc:max_nc)[which.min(res[,2])], "clusters=", min(res[,2])))
print("clustering for min G3")
print(clusters[which.min(res[,2]),])
write.table(res, file="G3_res.csv", sep=";", ",dec=", ", row.names=TRUE, col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="G3", xaxt="n")
axis(1, c(min_nc:max_nc))

```

index.Gap

Calculates Tibshirani, Walther and Hastie gap index

Description

Calculates Tibshirani, Walther and Hastie gap index

Usage

```

index.Gap (x, clall, reference.distribution="unif", B=10,
method="pam", d=NULL, centrotypes="centroids")

```

Arguments

x	data
clall	Two vectors of integers indicating the cluster to which each object is allocated in partition of n objects into u, and u+1 clusters
reference.distribution	"unif" - generate each reference variable uniformly over the range of the observed values for that variable or "pc" - generate the reference variables from a uniform distribution over a box aligned with the principal components of the data. In detail, if $X = \{x_{ij}\}$ is our $n \times m$ data matrix, assume that the columns have mean 0 and compute the singular value decomposition $X = UDV^T$. We transform via $X' = XV$ and then draw uniform features Z' over the ranges of the columns of X' , as in method a) above. Finally we back-transform via $Z = Z'V^T$ to give reference data Z
B	the number of simulations used to compute the gap statistic
method	the cluster analysis method to be used. This should be one of: "ward", "single", "complete", "average", "mcquitty", "median", "centroid", "pam", "k-means", "diana"
d	optional distance matrix, used for calculations if centrotypes="medoids"
centrotypes	"centroids" or "medoids"

Details

See file [../doc/indexGap_details.pdf](#) for further details

Thanks to dr Michael P. Fay from National Institute of Allergy and Infectious Diseases for finding "one column error".

Value

Gap	Tibshirani, Walther and Hastie gap index for u clusters
diffu	necessary value for choosing correct number of clusters via gap statistic $\text{Gap}(u) - [\text{Gap}(u+1) - s(u+1)]$

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References

Tibshirani, R., Walther, G., Hastie, T. (2001), *Estimating the number of clusters in a data set via the gap statistic*, "Journal of the Royal Statistical Society", ser. B, vol. 63, part 2, 411-423.

See Also

[index.G1](#), [index.G2](#), [index.G3](#), [index.S](#), [index.H](#), [index.KL](#), [index.DB](#)

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
cl1<-pam(data_ratio,4)
cl2<-pam(data_ratio,5)
clall<-cbind(cl1$clustering,cl2$clustering)
g<-index.Gap(data_ratio, clall, reference.distribution="unif", B=10,
  method="pam")
print(g)

# Example 2
library(clusterSim)
means <- matrix(c(0,2,4,0,3,6), 3, 2)
cov <- matrix(c(1,-0.9,-0.9,1), 2, 2)
x <- cluster.Gen(numObjects=40, means=means, cov=cov, model=2)
x <- x$data
md <- dist(x, method="euclidean")^2
# nc - number_of_clusters
min_nc=1
max_nc=5
min <- 0
clopt <- NULL
```

```

res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
found <- FALSE
for (nc in min_nc:max_nc){
  cl1 <- pam(md, nc, diss=TRUE)
  cl2 <- pam(md, nc+1, diss=TRUE)
  clall <- cbind(cl1$clustering, cl2$clustering)
  gap <- index.Gap(x,clall,B=20,method="pam",centrotypes="centroids")
  res[nc-min_nc+1, 2] <- diffu <- gap$diffu
  if ((res[nc-min_nc+1, 2] >=0) && (!found)){
    nc1 <- nc
    min <- diffu
    clopt <- cl1$cluster
    found <- TRUE
  }
}
if (found){
print(paste("Minimal nc where diffu>=0 is",nc1,"for diffu=",round(min,4)),quote=FALSE)
}else{
print("I have not found clustering with diffu>=0", quote=FALSE)
}
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="diffu",xaxt="n")
abline(h=0, untf=FALSE)
axis(1, c(min_nc:max_nc))

# Example 3
library(clusterSim)
means <- matrix(c(0,2,4,0,3,6), 3, 2)
cov <- matrix(c(1,-0.9,-0.9,1), 2, 2)
x <- cluster.Gen(numObjects=40, means=means, cov=cov, model=2)
x <- x$data
md <- dist(x, method="euclidean")^2
# nc - number_of_clusters
min_nc=1
max_nc=5
min <- 0
clopt <- NULL
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
found <- FALSE
for (nc in min_nc:max_nc){
  cl1 <- pam(md, nc, diss=TRUE)
  cl2 <- pam(md, nc+1, diss=TRUE)
  clall <- cbind(cl1$clustering, cl2$clustering)
  gap <- index.Gap(x,clall,B=20,method="pam",d=md,centrotypes="medoids")
  res[nc-min_nc+1, 2] <- diffu <- gap$diffu
  if ((res[nc-min_nc+1, 2] >=0) && (!found)){
    nc1 <- nc
    min <- diffu
    clopt <- cl1$cluster
    found <- TRUE
  }
}
}

```

```

if (found){
print(paste("Minimal nc where diffu>=0 is",nc1,"for diffu=",round(min,4)),quote=FALSE)
}else{
print("I have not found clustering with diffu>=0",quote=FALSE)
}
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="diffu", xaxt="n")
abline(h=0, untf=FALSE)
axis(1, c(min_nc:max_nc))

```

index.H

Calculates Hartigan index

Description

Calculates Hartigan index

Usage

```
index.H (x, clall, d=NULL, centrotypes="centroids")
```

Arguments

x	data
clall	Two vectors of integers indicating the cluster to which each object is allocated in partition of n objects into u and u+1 clusters
d	optional distance matrix, used for calculations if centrotypes="medoids"
centrotypes	"centroids" or "medoids"

Details

See file [../doc/indexH_details.pdf](#) for further details

Value

Hartigan index

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References

Hartigan, J. (1975), *Clustering algorithms*, Wiley, New York.
Milligan, G.W., Cooper, M.C. (1985), *An examination of procedures of determining the number of cluster in a data set*, "Psychometrika", vol. 50, no. 2, 159-179.
Tibshirani, R., Walther, G., Hastie, T. (2001), *Estimating the number of clusters in a data set via the gap statistic*, "Journal of the Royal Statistical Society", ser. B, vol. 63, part 2, 411-423.

See Also

[index.G1](#), [index.G2](#), [index.G3](#), [index.S](#), [index.KL](#), [index.Gap](#), [index.DB](#)

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
cl1<-pam(data_ratio,4)
cl2<-pam(data_ratio,5)
clall<-cbind(cl1$clustering,cl2$clustering)
index.H(data_ratio,clall)

# Example 2
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="euclidean")
# nc - number_of_clusters
min_nc=1
max_nc=20
min <- 0
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
found <- FALSE
clusters <- NULL
for (nc in min_nc:max_nc)
{
  print(nc)
  hc <- hclust(md, method="complete")
  cl1 <- cutree(hc, k=nc)
  cl2 <- cutree(hc, k=nc+1)
  clall <- cbind(cl1,cl2)
  res[nc-min_nc+1,2] <- H <- index.H(data_ratio,clall,centrotypes="centroids")
  if ((res[nc-min_nc+1, 2]<10) && (!found)){
    nc1 <- nc
    min <- H
    clopt <- cl1
    found <- TRUE
  }
}
if (found)
{
  print(paste("minimal nc for H<=10 equals",nc1,"for H=",min))
  print("clustering for minimal nc where H<=10")
  print(clopt)
}else
{
  print("Clustering not found with H<=10")
}
write.table(res,file="H_res.csv",sep=";",dec="," ,row.names=TRUE,col.names=FALSE)
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="H",xaxt="n")
abline(h=10, untf=FALSE)
```



```

axis(1, c(min_nc:max_nc))

# Example 3
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="manhattan")
# nc - number_of_clusters
min_nc=1
max_nc=20
min <- 0
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
found <- FALSE
clusters <- NULL
for (nc in min_nc:max_nc)
{
print(nc)
hc <- hclust(md, method="complete")
cl1 <- cutree(hc, k=nc)
cl2 <- cutree(hc, k=nc+1)
clall <- cbind(cl1,cl2)
res[nc-min_nc+1,2] <- H <- index.H(data_ratio,clall,d=md,centrotypes="medoids")
if ((res[nc-min_nc+1, 2]<10) && (!found)){
  nc1 <- nc
  min <- H
  clopt <- cl1
  found <- TRUE
}
}
if (found)
{
print(paste("minimal nc for H<=10 equals",nc1,"for H=",min))
print("clustering for minimal nc where H<=10")
print(clopt)
}else
{
print("Clustering not found with H<=10")
}
write.table(res,file="H_res.csv",sep=";",dec=".",row.names=TRUE,col.names=FALSE)
plot(res,type="p",pch=0,xlab="Number of clusters",ylab="H",xaxt="n")
abline(h=10, untf=FALSE)
axis(1, c(min_nc:max_nc))

```

index.KL

Calculates Krzanowski-Lai index

Description

Calculates Krzanowski-Lai index

Usage

```
index.KL (x,clall,d=NULL,centrotypes="centroids")
```

Arguments

x	data
clall	Three vectors of integers indicating the cluster to which each object is allocated in partition of n objects into u-1, u, and u+1 clusters
d	optional distance matrix, used for calculations if centrotypes="medoids"
centrotypes	"centroids" or "medoids"

Details

See file [../doc/indexKL_details.pdf](#) for further details

Value

Krzanowski-Lai index

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References

Krzanowski, W.J., Lai, Y.T. (1988), *A criterion for determining the number of groups in a data set using sum of squares clustering*, "Biometrics", 44, 23-34.

Milligan, G.W., Cooper, M.C. (1985), *An examination of procedures of determining the number of cluster in a data set*, "Psychometrika", vol. 50, no. 2, 159-179.

Tibshirani, R., Walther, G., Hastie, T. (2001), *Estimating the number of clusters in a data set via the gap statistic*, "Journal of the Royal Statistical Society", ser. B, vol. 63, part 2, 411-423.

See Also

[index.G1](#), [index.G2](#), [index.G3](#), [index.S](#), [index.H](#), [index.Gap](#), [index.DB](#)

Examples

```
# Example 1
library(clusterSim)
data(data_ratio)
cl1<-pam(data_ratio,4)
cl2<-pam(data_ratio,5)
cl3<-pam(data_ratio,6)
clall<-cbind(cl1$clustering,cl2$clustering,cl3$clustering)
index.KL(data_ratio,clall)
```

```

# Example 2
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="manhattan")
# nc - number_of_clusters
min_nc=2
max_nc=15
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
  cl1 <- pam(md, nc-1, diss=TRUE)
  cl2 <- pam(md, nc, diss=TRUE)
  cl3 <- pam(md, nc+1, diss=TRUE)
  clall<- cbind(cl1$clustering, cl2$clustering, cl3$clustering)
  res[nc-min_nc+1,2] <- KL <- index.KL(data_ratio,clall,centrotypes="centroids")
  clusters <- rbind(clusters, cl2$cluster)
}
print(paste("max KL for", (min_nc:max_nc)[which.max(res[,2])], "clusters=", max(res[,2])))
print("clustering for max KL")
print(clusters[which.max(res[,2]),])
write.table(res, file="KL_res.csv", sep=";", dec=".", row.names=TRUE, col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="KL", xaxt="n")
axis(1, c(min_nc:max_nc))

# Example 3
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="manhattan")
# nc - number_of_clusters
min_nc=2
max_nc=15
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
  cl1 <- pam(md, nc-1, diss=TRUE)
  cl2 <- pam(md, nc, diss=TRUE)
  cl3 <- pam(md, nc+1, diss=TRUE)
  clall<- cbind(cl1$clustering, cl2$clustering, cl3$clustering)
  res[nc-min_nc+1,2] <- KL <- index.KL(data_ratio,clall,d=md,centrotypes="medoids")
  clusters <- rbind(clusters, cl2$cluster)
}
print(paste("max KL for", (min_nc:max_nc)[which.max(res[,2])], "clusters=", max(res[,2])))
print("clustering for max KL")
print(clusters[which.max(res[,2]),])
write.table(res, file="KL_res.csv", sep=";", dec=".", row.names=TRUE, col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="KL", xaxt="n")
axis(1, c(min_nc:max_nc))

```

`index.S`*Calculates Rousseeuw's Silhouette internal cluster quality index*

Description

Calculates Rousseeuw's Silhouette internal cluster quality index

Usage

```
index.S(d,c1,singleObject=0)
```

Arguments

<code>d</code>	'dist' object
<code>c1</code>	A vector of integers indicating the cluster to which each object is allocated
<code>singleObject</code>	0 - $s(i)=0$ or 1 - $s(i)=1$. When cluster contains a single object, it is unclear how $a(i)$ of Silhouette index should be defined (see Kaufman & Rousseeuw (1990), p. 85).

Details

See file [../doc/indexS_details.pdf](#) for further details

Value

calculated Silhouette index

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References

Gatnar, E., Walesiak, M. (Eds.) (2004), *Metody statystycznej analizy wielowymiarowej w badaniach marketingowych [Multivariate statistical analysis methods in marketing research]*, Wydawnictwo AE, Wroclaw, 342-343, erratum.

Kaufman, L., Rousseeuw, P.J. (1990), *Finding groups in data: an introduction to cluster analysis*, Wiley, New York, 83-88.

See Also

[index.G1](#), [index.G2](#), [index.G3](#), [index.KL](#), [index.H](#), [index.Gap](#), [index.DB](#)

Examples

```

# Example 1
library(clusterSim)
data(data_ratio)
d <- dist.GDM(data_ratio)
c <- pam(d, 5, diss = TRUE)
icq <- index.S(d,c$clustering)
print(icq)

# Example 2
library(clusterSim)
data(data_ratio)
md <- dist(data_ratio, method="manhattan")
# nc - number_of_clusters
min_nc=2
max_nc=20
res <- array(0, c(max_nc-min_nc+1, 2))
res[,1] <- min_nc:max_nc
clusters <- NULL
for (nc in min_nc:max_nc)
{
  cl2 <- pam(md, nc, diss=TRUE)
  res[nc-min_nc+1, 2] <- S <- index.S(md,cl2$cluster)
  clusters <- rbind(clusters, cl2$cluster)
}
print(paste("max S for", (min_nc:max_nc)[which.max(res[,2])], "clusters=", max(res[,2])))
print("clustering for max S")
print(clusters[which.max(res[,2]),])
write.table(res, file="S_res.csv", sep=";", dec=".", row.names=TRUE, col.names=FALSE)
plot(res, type="p", pch=0, xlab="Number of clusters", ylab="S", xaxt="n")
axis(1, c(min_nc:max_nc))

```

initial.Centers

*Calculation of initial clusters centers for k-means like algorithms***Description**

Function calculates initial clusters centers for k-means like algorithms with the following algorithm (similar to SPSS QuickCluster function)

- (a) if the distance between x_k and its closest cluster center is greater than the distance between the two closest centers (M_m and M_n), then x_k replaces either M_m or M_n , whichever is closer to x_k .
- (b) If x_k does not replace a cluster initial center in (a), a second test is made: If that distance d_q greater than the distance between M_q and its closest M_i , then x_k replaces M_q .

where:

M_i - initial center of i -th cluster

x_k - vector of k -th observation

$d(\dots, \dots)$ - Euclidean distance

$$d_{mn} = \min_{ij} d(M_i, M_j)$$

$$d_q = \min_i d(x_k, M_i)$$

Usage

```
initial.Centers(x, k)
```

Arguments

x	matrix or dataset
k	number of initial cluster centers

Value

Numbers of objects chosen as initial cluster centers

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References

Hartigan, J. (1975), *Clustering algorithms*, Wiley, New York.

See Also

[cluster.Sim](#)

Examples

```
#Example 1 (numbers of objects chosen as initial cluster centers)
library(clusterSim)
data(data_ratio)
ic <- initial.Centers(data_ratio, 10)
print(ic)
```

```
#Example 2 (application with kmeans algorithm)
library(clusterSim)
data(data_ratio)
kmeans(data_ratio, data_ratio[initial.Centers(data_ratio, 10),])
```

ordinalToMetric	<i>Reinforcing measurement scale for ordinal data</i>
-----------------	---

Description

Reinforcing measurement scale for ordinal data (ordinal to metric scale)

Usage

```
ordinalToMetric(data, scaleType="o", patternCoordinates)
```

Arguments

data	matrix or dataset
scaleType	"o" - variables measured on ordinal scale, "m" - variables measured on metric scale, "o/m" - vector with mixed variables - e.g. c("o","m","m","o","o","m")
patternCoordinates	vector containing pattern coordinates c(...) given by the researcher for data (for metric variables - NA, for ordinal variables - one of the categories for each ordinal variable (e.g. maximum category))

Details

See file [../doc/ordinalToMetric_details.pdf](#) for further details

Value

pdata	raw (primary) data matrix
tdata	data matrix after transformation of ordinal variables into metric variables
cpattern	vector containing pattern coordinates

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References

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See Also

[dist.GDM](#)

Examples

```
# Example 1
library(clusterSim)
data(data_patternGDM2)
res1<-ordinalToMetric(data_patternGDM2,scaleType="o",patternCoordinates=c(5,4,3,1,1,3))
print(res1)

# Example 2
library(clusterSim)
data(data_patternGDM2)
res2<-ordinalToMetric(data_patternGDM2,scaleType="o",patternCoordinates=c(5,4,3,4,2,4))
print(res2)
```

pattern.GDM1

An application of GDM1 distance for metric data to compute the distances of objects from the pattern object (upper or lower)

Description

An application of GDM1 distance for metric data to compute the distances of objects from the upper (ideal point co-ordinates) or lower (anti-ideal point co-ordinates) pattern object

Usage

```
pattern.GDM1(data, performanceVariable, scaleType="i",
nomOptValues=NULL, weightsType="equal", weights=NULL,
normalization="n0", patternType="upper",
patternCoordinates="dataBounds", patternManual=NULL,
nominalTransfMethod=NULL)
```


Arguments

data	matrix or dataset
performanceVariable	vector containing three types of performance variables: s for stimulants where higher value means better performance d for destimulants where low values indicate better performance n for nominants where the best value is implied. Object performance is positively assessed if the measure has implied value
scaleType	"i" - variables measured on interval scale, "r" - variables measured on ratio scale, "r/i" - vector with mixed variables
nomOptValues	vector containing optimal values for nominant variables and NA values for stimulants and destimulants. If performanceVariable do not contain nominant variables this nomOptValues may be set to NULL
weightsType	equal or different1 or different2 "equal" - equal weights "different1" - vector of different weights should satisfy conditions: each weight takes value from interval [0; 1] and sum of weights equals one "different2" - vector of different weights should satisfy conditions: each weight takes value from interval [0; m] and sum of weights equals m (m - the number of variables)
normalization	normalization formulas as in data.Normalization function
weights	vector of weights
patternType	"upper" - ideal point co-ordinates consists of the best variables' values "lower" - anti-ideal point co-ordinates consists of the worst variables' values
patternCoordinates	"dataBounds" - pattern should be calculated as following: "upper" pattern (maximum for stimulants, minimum for destimulants), "lower" pattern (minimum for stimulants, maximum for destimulants) "manual" - pattern should be given in patternManual variable
patternManual	Pattern co-ordinates contain: real numbers "min" - for minimal value of variable "max" - for maximal value of variable
nominalTransfMethod	method of transformation of nominant to stimulant variable: "q" - quotient transformation "d" - difference transformation

Details

See file [../doc/patternGDM1_details.pdf](#) for further details

Value

pdata	raw (primary) data matrix
tdata	data matrix after transformation of nominant variables (with pattern in last row)
data	data matrix after normalization (with pattern in last row)
distances	GDM1 distances from pattern object
sortedDistances	sorted GDM1 distances from pattern object

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References

- Jajuga, K., Walesiak, M., Bak, A. (2003), *On the general distance measure*, In: M. Schwaiger, O. Opitz (Eds.), *Exploratory data analysis in empirical research*, Springer-Verlag, Berlin, Heidelberg, 104-109.
- Walesiak, M. (1993), *Statystyczna analiza wielowymiarowa w badaniach marketingowych [Multivariate statistical analysis in marketing research]*. Wrocław University of Economics, Research Papers no. 654.
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- Walesiak, M. (2011), *Uogólniona miara odległości GDM w statystycznej analizie wielowymiarowej z wykorzystaniem programu R [The Generalized Distance Measure GDM in multivariate statistical analysis with R]*, Wydawnictwo UE, Wrocław.

See Also

[dist.GDM,data.Normalization](#)

Examples

```
# Example 1
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
performanceVariable=c("s","s","s","s","s","s","d","d","s","s"),
scaleType="r",nomOptValues=NULL,weightsType<-"equal",weights=NULL,
normalization<-"n4",patternType<-"lower",patternCoordinates<-"manual",
patternManual<-c("min","min","min","min","min","min","max","max","min","min"),
nominalTransfMethod <-NULL)
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p),xlim=c(max(gdm_p),min(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),xaxt="n",
```

```

xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p, labels=names(gdm_p), cex.axis=0.5)

# Example 2
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
performanceVariable=c("s","s","s","s","s","s","d","d","s","s"),
scaleType="r", nomOptValues=NULL, weightsType<-"equal", weights=NULL,
normalization<-"n2", patternType<-"upper",
patternCoordinates<-"dataBounds", patternManual<-NULL,
nominalTransfMethod<-NULL)
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p, gdm_p), xlim=c(min(gdm_p), max(gdm_p)),
ylim=c(min(gdm_p), max(gdm_p)), xaxt="n",
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p, labels=names(gdm_p), cex.axis=0.5)

# Example 3
library(clusterSim)
data(data_patternGDM1)
res<-pattern.GDM1(data_patternGDM1,
performanceVariable=c("s","s","s","s","s","s","d","d","s","s"),
scaleType="r", nomOptValues=NULL, weightsType<-"different2",
weights=c(1.1,1.15,1.15,1.1,1.1,0.7,0.7,1.2,0.8,1.0),
normalization<-"n6", patternType<-"upper", patternCoordinates<-"manual",
patternManual<-c(100,100,100,100,100,"max","min","min","max","max"),
nominalTransfMethod <-NULL)
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p, gdm_p), xlim=c(min(gdm_p), max(gdm_p)),
ylim=c(min(gdm_p), max(gdm_p)), xaxt="n",
xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p, labels=names(gdm_p), cex.axis=0.5)

```

pattern.GDM2

An application of GDM2 distance for ordinal data to compute the distances of objects from the pattern object (upper or lower)

Description

An application of GDM2 distance for ordinal data to compute the distances of objects from the upper (ideal point co-ordinates) or lower (anti-ideal point co-ordinates) pattern object

Usage

```
pattern.GDM2(data, performanceVariable, nomOptValues=NULL,
weightsType="equal", weights=NULL, patternType="upper",
patternCoordinates="dataBounds", patternManual=NULL,
nominalTransfMethod=NULL)
```

Arguments

data	matrix or dataset
performanceVariable	vector containing three types of performance variables: s for stimulants where higher value means better performance d for destimulants where low values indicate better performance n for nominants where the best value is implied. Object performance is positively assessed if the measure has implied value
nomOptValues	vector containing optimal values for nominant variables and NA values for stimulants and destimulants. If performanceVariable do not contain nominant variables this nomOptValues may be set to NULL
weightsType	equal or different1 or different2 "equal" - equal weights "different1" - vector of different weights should satisfy conditions: each weight takes value from interval [0; 1] and sum of weights equals one "different2" - vector of different weights should satisfy conditions: each weight takes value from interval [0; m] and sum of weights equals m (m - the number of variables)
weights	vector of weights
patternType	"upper" - ideal point co-ordinates consists of the best variables' values "lower" - anti-ideal point co-ordinates consists of the worst variables' values
patternCoordinates	"dataBounds" - pattern should be calculated as following: "upper" pattern (maximum for stimulants, minimum for destimulants, nominal value for nominants), "lower" pattern (minimum for stimulants, maximum for destimulants) "manual" - pattern should be given in patternManual variable
patternManual	Pattern co-ordinates contain: real numbers "min" - for minimal value of variable "max" - for maximal value of variable "nom" - for nominal value of variable (for upper pattern only - given in nomOptValues vector)
nominalTransfMethod	method of transformation of nominant to destimulant variable for patternType="lower": "database" - for each nominant separately GDM2 distance is calculated between each nominant observation (with repetitions - all variable values are used in calculation) and nominal value. Next the variable observations are replaced by those distances

"symmetrical" - for each nominant separately GDM2 distance is calculated between each nominant observation (without repetition - each observation is used once) and nominal value. Next the variable observations are replaced by those distances

Details

See file [../doc/patternGDM2_details.pdf](#) for further details

Value

pdata	raw (primary) data matrix
data	data matrix after transformation of nominant variables (with pattern in last row)
distances	GDM2 distances from pattern object
sortedDistances	sorted GDM2 distances from pattern object

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References

- Jajuga, K., Walesiak, M., Bak, A. (2003), *On the general distance measure*, In: M. Schwaiger, O. Opitz (Eds.), *Exploratory data analysis in empirical research*, Springer-Verlag, Berlin, Heidelberg, 104-109.
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- Walesiak, M. (2011), *Uogólniona miara odległości GDM w statystycznej analizie wielowymiarowej z wykorzystaniem programu R [The Generalized Distance Measure GDM in multivariate statistical analysis with R]*, Wydawnictwo UE, Wrocław.

See Also

[dist.GDM](#)

Examples

```

# Example 1
library(clusterSim)
data(data_patternGDM2)
res<-pattern.GDM2(data_patternGDM2,
performanceVariable=c("s","s","s","d","d","n"),
nomOptValues=c(NA,NA,NA,NA,NA,3), weightsType<-"equal", weights=NULL,
patternType="lower", patternCoordinates="manual",
patternManual=c("min","min",0,5,"max","max"),
nominalTransfMethod="symmetrical")
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p),xlim=c(max(gdm_p),min(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),
xaxt="n",xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)

# Example 2
library(clusterSim)
data(data_patternGDM2)
res<-pattern.GDM2(data_patternGDM2,
performanceVariable=c("s","s","s","d","d","n"),
nomOptValues=c(NA,NA,NA,NA,NA,3), weightsType<-"equal", weights=NULL,
patternType="upper", patternCoordinates="dataBounds",
patternManual=NULL, nominalTransfMethod="database")
print(res)
gdm_p<-res$distances
plot(cbind(gdm_p,gdm_p), xlim=c(min(gdm_p),max(gdm_p)),
ylim=c(min(gdm_p),max(gdm_p)),
xaxt="n",xlab="Order of objects from the best to the worst",
ylab="GDM distances from pattern object", lwd=1.6)
axis(1, at=gdm_p,labels=names(gdm_p), cex.axis=0.5)

```

plotCategorical

Plot categorial data on a scatterplot matrix

Description

Plot categorial data on a scatterplot matrix (optionally with clusters)

Usage

```
plotCategorical(x, pairsofVar=NULL, cl=NULL, clColors=NULL,...)
```

Arguments

x data matrix (rows correspond to observations and columns correspond to variables)

pairsofVar	pairs of variables - all variables (pairsofVar=NULL) or selected variables, e.g. pairsofVar=c(1,3,4)
cl	cluster membership vector
clColors	The colors of clusters. The colors are given arbitrary (clColors=TRUE) or by hand, e.g. clColors=c("red","blue","green"). The number of colors equals the number of clusters
...	Arguments to be passed to methods, such as graphical parameters (see par).

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See Also

[plotCategorical3d](#), [colors](#), [pairs](#)

Examples

```
# Example 1
library(clusterSim)
data(data_ordinal)
plotCategorical(data_ordinal, pairsofVar=c(1,3,4,9), cl=NULL,
clColors = NULL)

# Example 2
library(clusterSim)
grnd <- cluster.Gen(50,model=5,dataType="o",numCategories=5)
plotCategorical(grnd$data, pairsofVar=NULL, cl=grnd$clusters,
clColors=TRUE)

# Example 3
library(clusterSim)
grnd<-cluster.Gen(50,model=4,dataType="o",numCategories=7, numNoisyVar=2)
plotCategorical(grnd$data, pairsofVar=NULL, cl=grnd$clusters,
clColors = c("red","blue","green"))
```

plotCategorical3d *Plot categorical data with three-dimensional plots*

Description

Plot categorical data with three-dimensional plots (optionally with clusters)

Usage

```
plotCategorical3d(x, tripleofVar=c(1,2,3), cl=NULL, clColors=NULL,...)
```

Arguments

x	data matrix (rows correspond to observations and columns correspond to variables)
tripleofVar	triple of variables - vector of the number of variables, e.g. tripleofVar = c(1, 3, 4)
cl	cluster membership vector
clColors	The colors of clusters. The colors are given arbitrary (clColors=TRUE) or by hand, e.g. clColors=c("red", "blue", "green"). The number of colors equals the number of clusters
...	Arguments to be passed to methods, such as graphical parameters (see par).

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See Also

[plotCategorical](#), [colors](#)

Examples

```
# These examples do not run on Mac_OS-X. We're working to fix them
# They run quite well on Windows and Linux in meantime

# Example 1
#library(clusterSim)
#data(data_ordinal)
#plotCategorical3d(data_ordinal, tripleofVar=c(1,3,9), cl=NULL,
#clColors=NULL)

# Example 2
#library(clusterSim)
#grnd <- cluster.Gen(50,model=5,dataType="o",numCategories=5)
#plotCategorical3d(grnd$data, tripleofVar=c(1,2,3), cl=grnd$clusters,
#clColors=TRUE)

# Example 3
#library(clusterSim)
#grnd <- cluster.Gen(50, model=4, dataType="o", numCategories=7, numNoisyVar=2)
#plotCategorical3d(grnd$data, tripleofVar=c(1,2,4), cl=grnd$clusters,
#clColors=c("red", "blue", "green"))
```

plotInterval	<i>Plot symbolic interval-valued data on a scatterplot matrix</i>
--------------	---

Description

Plot symbolic interval-valued data on a scatterplot matrix (optionally with clusters)

Usage

```
plotInterval(x, pairsofsVar=NULL, cl=NULL, clColors=NULL,...)
```

Arguments

x	symbolic interval-valued data
pairsofsVar	pairs of symbolic interval variables - all variables (pairsofsVar=NULL) or selected variables, e.g. pairsofsVar=c(1,3,4)
cl	cluster membership vector
clColors	The colors of clusters. The colors are given arbitrary (clColors=TRUE) or by hand, e.g. clColors=c("red", "blue", "green"). The number of colors equals the number of clusters
...	Arguments to be passed to methods, such as graphical parameters (see par).

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See Also

[plotCategorical](#), [plotCategorical3d](#), [colors](#), [pairs](#)

Examples

```
# Example 1
library(clusterSim)
data(data_symbolic)
plotInterval(data_symbolic, pairsofsVar=c(1,3,4,6), cl=NULL,
clColors=NULL)

# Example 2
library(clusterSim)
grnd <- cluster.Gen(60, model=5, dataType="s", numNoisyVar=1,
numOutliers=10, rangeOutliers=c(1,5))
grnd$clusters[grnd$clusters==0] <- max(grnd$clusters)+1
# To colour outliers
plotInterval(grnd$data, pairsofsVar=NULL, cl=grnd$clusters,
```

```

c1Colors=TRUE)

# Example 3
library(clusterSim)
grnd <- cluster.Gen(50, model=4, dataType="s", numNoisyVar=2,
numOutliers=10, rangeOutliers=c(1,4))
grnd$clusters[grnd$clusters==0] <- max(grnd$clusters)+1
# To colour outliers
plotInterval(grnd$data, pairsofsVar=NULL, cl=grnd$clusters,
c1Colors=c("red", "blue", "green", "yellow"))

```

replication.Mod *Modification of replication analysis for cluster validation*

Description

Modification of replication analysis for cluster validation

Usage

```

replication.Mod(x, v="m", u=2, centrotypes="centroids",
normalization=NULL, distance=NULL, method="kmeans",
S=10, fixedAsample=NULL)

```

Arguments

x	data matrix
v	type of data: metric ("r" - ratio, "i" - interval, "m" - mixed), nonmetric ("o" - ordinal, "n" - multi-state nominal, "b" - binary)
u	number of clusters given arbitrary
centrotypes	"centroids" or "medoids"
normalization	optional, normalization formulas for metric data (normalization by variable): for ratio data: "n0" - without normalization, "n6" - (x/sd), "n6a" - (x/mad), "n7" - (x/range), "n8" - (x/max), "n9" - (x/mean), "n9a" - (x/median), "n10" - (x/sum), "n11" - x/\sqrt{SSQ} for interval or mixed data: "n0" - without normalization, "n1" - (x-mean)/sd, "n2" - (x-median)/mad, "n3" - (x-mean)/range, "n3a" - positional unitization (x-median)/range, "n4" - (x-min)/range, "n5" - (x-mean)/max[abs(x-mean)], "n5a" - (x-median)/max[abs(x-median)], "n12" - normalization (x - mean)/(sum(x - mean) ²) ^{0.5} , "n12a" - positional normalization (x - median)/(sum(x - median) ²) ^{0.5}
distance	distance measures NULL for "kmeans" method (based on data matrix), for ratio data: "d1" - Manhattan, "d2" - Euclidean, "d3" - Chebychev (max), "d4" - squared Euclidean, "d5" - GDM1, "d6" - Canberra, "d7" - Bray-Curtis for interval or mixed (ratio & interval) data: "d1", "d2", "d3", "d4", "d5"

	for ordinal data: "d8" - GDM2
	for multi-state nominal: "d9" - Sokal & Michener
	for binary data: "b1" = Jaccard; "b2" = Sokal & Michener; "b3" = Sokal & Sneath (1); "b4" = Rogers & Tanimoto; "b5" = Czekanowski; "b6" = Gower & Legendre (1); "b7" = Ochiai; "b8" = Sokal & Sneath (2); "b9" = Phi of Pearson; "b10" = Gower & Legendre (2)
method	clustering method: "kmeans" (default), "single", "complete", "average", "mcquitty", "median", "centroid", "ward", "pam", "diana"
S	the number of simulations used to compute mean corrected Rand index
fixedAsample	if NULL A sample is generated randomly, otherwise this parameter contains object numbers arbitrarily assigned to A sample

Details

See file [../doc/replication.Mod_details.pdf](#) for further details

Value

A	3-dimensional array containing data matrices for A sample of objects in each simulation (first dimension represents simulation number, second - object number, third - variable number)
B	3-dimensional array containing data matrices for B sample of objects in each simulation (first dimension represents simulation number, second - object number, third - variable number)
centroid	3-dimensional array containing centroids of u clusters for A sample of objects in each simulation (first dimension represents simulation number, second - cluster number, third - variable number)
medoid	3-dimensional array containing matrices of observations on u representative objects (medoids) for A sample of objects in each simulation (first dimension represents simulation number, second - cluster number, third - variable number)
clusteringA	2-dimensional array containing cluster numbers for A sample of objects in each simulation (first dimension represents simulation number, second - object number)
clusteringB	2-dimensional array containing cluster numbers for B sample of objects in each simulation (first dimension represents simulation number, second - object number)
clusteringBB	2-dimensional array containing cluster numbers for B sample of objects in each simulation according to 4 step of replication analysis procedure (first dimension represents simulation number, second - object number)
cRand	value of mean corrected Rand index for S simulations

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See Also

[cluster.Sim](#), [hclust](#), [kmeans](#), [dist](#), [dist.BC](#), [dist.SM](#), [dist.GDM](#),
[data.Normalization](#)

Examples

```
library(clusterSim)
data(data_ratio)
w <- replication.Mod(data_ratio, u=5, S=10)
print(w)

library(clusterSim)
data(data_binary)
replication.Mod(data_binary, "b", u=2, "medoids", NULL, "b1", "pam", fixedAsample=c(1,3,6,7))
```

shapes.blocks3d	<i>Generation of data set containing two clusters with untypical shapes (cube divided into two parts by main diagonal plane)</i>
-----------------	--

Description

Generation of data set containing two clusters with untypical shapes (cube starting at point (0,0,0) divided into two parts by main diagonal plane)

Usage

```
shapes.blocks3d(numObjects=180, shapesUnitSize=0.5, shape2coordinateX=1.2,
shape2coordinateY=1.2, shape2coordinateZ=1.2, outputCsv="", outputCsv2="",
outputColNames=TRUE, outputRowNames=TRUE)
```

Arguments

numObjects	number of objects in each cluster - positive integer value or vector with length=2
shapesUnitSize	length of one unit for shape (maximal height, width and depth of shape is 2*shapesUnitSize)
shape2coordinateX	maximal value for second shape in first (X) dimension
shape2coordinateY	maximal value for second shape in second (Y) dimension
shape2coordinateZ	maximal value for second shape in third (Z) dimension
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)
outputColNames	outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names
outputRowNames	outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Value

clusters	cluster number for each object
data	generated data - matrix with objects in rows and variables in columns

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<http://keii.ue.wroc.pl/clusterSim>

See Also

[shapes.worms](#), [shapes.circles2](#), [shapes.circles3](#), [shapes.bulls.eyes](#), [shapes.two.moon](#)

Examples

```
library(clusterSim)
library(rgl)
sb3d<-shapes.blocks3d(300,1,3,3,3)
plot3d(sb3d$data,col=rainbow(2)[sb3d$clusters])
```

shapes.circles2	<i>Generation of data set containing two clusters with untypical ring shapes (circles)</i>
-----------------	--

Description

Generation of data set containing two clusters with untypical ring shapes. For each point first random radius r from given interval is generated then random angle α and finally the coordinates of point are calculated as $(r \cdot \cos(\alpha), r \cdot \sin(\alpha))$. For bull's eye data set second shape is filled circle (r starts from 0)

Usage

```
shapes.circles2(numObjects=180, shape1rFrom=0.75, shape1rTo=0.9, shape2rFrom=0.35,
shape2rTo=0.5, outputCsv="", outputCsv2="", outputColNames=TRUE, outputRowNames=TRUE)
shapes.bulls.eye(numObjects=180, shape1rFrom=0.75, shape1rTo=0.95, shape2rTo=0.45,
outputCsv="", outputCsv2="", outputColNames=TRUE, outputRowNames=TRUE)
```

Arguments

numObjects	number of objects in each cluster - positive integer value or vector with length=2,
shape1rFrom	minimal value of radius for first ring
shape1rTo	maximal value of radius for first ring
shape2rFrom	minimal value of radius for second ring
shape2rTo	maximal value of radius for second ring
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)
outputColNames	outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names
outputRowNames	outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Value

clusters	cluster number for each object
data	generated data - matrix with objects in rows and variables in columns

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See Also

[shapes.worms](#), [shapes.circles3](#), [shapes.bulls.eye](#), [shapes.two.moon](#), [shapes.blocks3d](#)

Examples

```
#Example1
library(clusterSim)
sc2<-shapes.circles2(180)
plot(sc2$data,col=rainbow(2)[sc2$clusters])
```

```
#Example2
library(clusterSim)
sbe<-shapes.bulls.eye(numObjects=c(120,60))
plot(sbe$data,col=rainbow(2)[sbe$clusters])
```

shapes.circles3	<i>Generation of data set containing three clusters with untypical ring shapes (circles)</i>
-----------------	--

Description

Generation of data set containing three clusters with untypical ring shapes. For each point first random radius r from given interval is generated then random angle α and finally the coordinates of point are calculated as $(r \cdot \cos(\alpha), r \cdot \sin(\alpha))$

Usage

```
shapes.circles3(numObjects=180,shape1rFrom=0.15,shape1rTo=0.3,
shape2rFrom=0.55,shape2rTo=0.7,shape3rFrom=1.15,shape3rTo=1.3,
outputCsv="",outputCsv2="",outputColNames=TRUE,outputRowNames=TRUE)
```

Arguments

numObjects	number of objects in each cluster - positive integer value or vector with length=3,
shape1rFrom	minimal value of radius for first ring
shape1rTo	maximal value of radius for first ring
shape2rFrom	minimal value of radius for second ring
shape2rTo	maximal value of radius for second ring
shape3rFrom	minimal value of radius for third ring
shape3rTo	maximal value of radius for third ring
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)

outputColNames outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names

outputRowNames outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Value

clusters cluster number for each object

data generated data - matrix with objects in rows and variables in columns

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See Also

[shapes.worms](#), [shapes.circles2](#), [shapes.bulls.eyes](#), [shapes.two.moon](#), [shapes.blocks3d](#)

Examples

```
#Example1
library(clusterSim)
sc3a<-shapes.circles3(180)
plot(sc3a$data,col=rainbow(3)[sc3a$clusters])

#Example2
library(clusterSim)
sc3b<-shapes.circles3(numObjects=c(120,180,240))
plot(sc3b$data,col=rainbow(3)[sc3b$clusters])
```

shapes.two.moon	<i>Generation of data set containing two clusters with untypical shapes (similar to waxing and waning crescent moon)</i>
-----------------	--

Description

Generation of data set containing two clusters with untypical shapes (similar to waxing and waning crescent moon). For each point first random radius r from given interval is generated then random angle α and finally the coordinates of point are calculated as $(a+\text{abs}(r*\cos(\alpha)),r*\sin(\alpha))$ for first shape and $(-\text{abs}(r*\cos(\alpha)),r*\sin(\alpha)-b)$ for second shape

Usage

```
shapes.two.moon(numObjects=180,shape1a=-0.4,shape2b=1,shape1rFrom=0.8,
shape1rTo=1.2,shape2rFrom=0.8,shape2rTo=1.2,outputCsv="",outputCsv2="",
outputColNames=TRUE,outputRowNames=TRUE)
```


Arguments

numObjects	number of objects in each cluster - positive integer value or vector with length=2,
shape1a	parameter a for first shape
shape2b	parameter b for first shape
shape1rFrom	minimal value of radius for first shape
shape1rTo	maximal value of radius for first shape
shape2rFrom	minimal value of radius for second shape
shape2rTo	maximal value of radius for second shape
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)
outputColNames	outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names
outputRowNames	outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Value

clusters	cluster number for each object
data	generated data - matrix with objects in rows and variables in columns

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See Also

[shapes.worms](#), [shapes.circles2](#), [shapes.circles3](#), [shapes.bulls.eyes](#), [shapes.blocks3d](#)

Examples

```
library(clusterSim)
stm<-shapes.two.moon(180)
plot(stm$data,col=rainbow(2)[stm$clusters])
```

shapes.worms *Generation of data set containing two clusters with untypical parabolic shapes (worms)*

Description

Generation of data set containing two clusters with untypical parabolic shapes (first is given by $y=x^2$, second by $y=-(x-a)^2+b$ with distortion from $\langle -tol,+tol \rangle$)

Usage

```
shapes.worms(numObjects=180, shape1x1=-2, shape1x2=2, shape2x1=-0.5,
             shape2x2=2.5, shape2a=1.5, shape2b=5.5, tol=0.1, outputCsv="", outputCsv2="",
             outputColNames=TRUE, outputRowNames=TRUE)
```

Arguments

numObjects	number of objects in each cluster - positive integer value or vector with length=2
shape1x1	starting value on abscissa axis for shape 1
shape1x2	end value on abscissa axis for shape 1
shape2x1	starting value on abscissa axis for shape 2
shape2x2	end value on abscissa axis for shape 2
shape2a	parameter a of shape 2
shape2b	parameter b of shape 2
tol	tolerance - each generated point is randomized by adding $\text{runif}(1,0,\text{tol})$
outputCsv	optional, name of csv file with generated data (first column contains id, second - number of cluster and others - data)
outputCsv2	optional, name of csv (a comma as decimal point and a semicolon as field separator) file with generated data (first column contains id, second - number of cluster and others - data)
outputColNames	outputColNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains first row with column names
outputRowNames	outputRowNames=TRUE indicates that output file (given by outputCsv and outputCsv2 parameters) contains a vector of row names

Value

clusters	cluster number for each object
data	generated data - matrix with objects in rows and variables in columns

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See Also

[shapes.worms](#), [shapes.circles2](#), [shapes.circles3](#), [shapes.bulls.ey](#), [shapes.two.moon](#), [shapes.blocks3d](#)

Examples

```
library(clusterSim)
sw<-shapes.worms(180)
plot(sw$data,col=rainbow(2)[sw$clusters])
```

speccl

A spectral clustering algorithm

Description

A spectral clustering algorithm. Cluster analysis is performed by embedding the data into the subspace of the eigenvectors of an affinity matrix

Usage

```
speccl(data,nc,distance="GDM1",sigma="automatic",sigma.interval="default",
mod.sample=0.75,R=10,iterations=3,na.action=na.omit,...)
```

Arguments

data	matrix or dataset
nc	the number of clusters
distance	distance function used to calculate affinity matrix: "sEuclidean" - squared Euclidean distance, "euclidean" - Euclidean distance, "manhattan" - city block distance, "maximum" - Chebyshev distance, "canberra" - Lance and Williams Canberra distance, "BC" - Bray-Curtis distance measure for ratio data, "GDM1" - GDM distance for metric data, "GDM2" - GDM distance for ordinal data, "SM" - Sokal-Michener distance measure for nominal variables
sigma	scale parameter used to calculate affinity matrix: sigma="automatic" - an algorithm for searching optimal value of sigma parameter; sigma=200 - value of sigma parameter given by researcher, e.g. 200
sigma.interval	sigma.interval="default" - from zero to square root of sum of all distances in lower triangle of distance matrix for "sEuclidean" and from zero to sum of all distances in lower triangle of distance matrix for other distances; sigma.interval=1000 - from zero to value given by researcher, e.g. 1000
mod.sample	proportion of data to use when estimating sigma (default: 0.75)
R	the number of intervals examined in each step of searching optimal value of sigma parameter algorithm (See ../doc/speccl_details.pdf)
iterations	the maximum number of iterations (rounds) allowed in algorithm of searching optimal value of sigma parameter
na.action	the action to perform on NA
...	arguments passed to kmeans procedure

Details

See file [../doc/speccl_details.pdf](#) for further details

Value

scdist	returns the lower triangle of the distance matrix
clusters	a vector of integers indicating the cluster to which each object is allocated
size	the number of objects in each cluster
withinss	the within-cluster sum of squared distances for each cluster
Ematrix	data matrix $n \times u$ (n - the number of objects, u - the number of eigenvectors)
Ymatrix	normalized data matrix $n \times u$ (n - the number of objects, u - the number of eigenvectors)
sigma	the value of scale parameter given by searching algorithm

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See Also

[dist.GDM](#),[kmeans](#),[dist](#),[dist.binary](#),[dist.SM](#),[dist.BC](#)

Examples

```
# Commented due to long execution time
# Example 1
#library(clusterSim)
#library(mlbench)
#data<-mlbench.spirals(100,1,0.03)
#plot(data)
#x<-data$x
#res1<-speccl(x,nc=2,distance="GDM1",sigma="automatic",
```

```

#sigma.interval="default",mod.sample=0.75,R=10,iterations=3)
#clas1<-res1$cluster
#print(data$classes)
#print(clas1)
#cRand<-classAgreement(table(as.numeric(as.vector(data$classes)),
#res1$clusters))$cRand
#print(res1$sigma)
#print(cRand)

# Example 2
#library(clusterSim)
#grnd2<-cluster.Gen(50,model=4,dataType="m",numNoisyVar=1)
#data<-as.matrix(grnd2$data)
#colornames<-c("red","blue","green")
#grnd2$clusters[grnd2$clusters==0]<-length(colornames)
#plot(grnd2$data,col=colornames[grnd2$clusters])
#us<-nrow(data)*nrow(data)/2
#res2<-speccl(data,nc=3,distance="sEuclidean",sigma="automatic",
#sigma.interval=us,mod.sample=0.75,R=10,iterations=3)
#cRand<-comparing.Partitions(grnd2$clusters,res2$clusters,type="cRand")
#print(res2$sigma)
#print(cRand)

# Example 3
#library(clusterSim)
#grnd3<-cluster.Gen(40,model=4,dataType="o",numCategories=7)
#data<-as.matrix(grnd3$data)
#plotCategorical(grnd3$data,pairsofVar=NULL,cl=grnd3$clusters,
#clColors=c("red","blue","green"))
#res3<-speccl(data,nc=3,distance="GDM2",sigma="automatic",
#sigma.interval="default",mod.sample=0.75,R=10,iterations=3)
#cRand<-comparing.Partitions(grnd3$clusters,res3$clusters,type="cRand")
#print(res3$sigma)
#print(cRand)

# Example 4
library(clusterSim)
data(data_nominal)
res4<-speccl(data_nominal,nc=4,distance="SM",sigma="automatic",
sigma.interval="default",mod.sample=0.75,R=10,iterations=3)
print(res4)

```

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