

# Package ‘akima’

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**Description** Linear or cubic spline interpolation for irregular gridded data

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 akima

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*Waveform Distortion Data for Bivariate Interpolation*


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### Description

akima is a list with components x, y and z which represents a smooth surface of z values at selected points irregularly distributed in the x-y plane.

The data was taken from a study of waveform distortion in electronic circuits, described in: Hiroshi Akima, "A Method of Bivariate Interpolation and Smooth Surface Fitting Based on Local Procedures", CACM, Vol. 17, No. 1, January 1974, pp. 18-20.

### References

Hiroshi Akima, "A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points", ACM Transactions on Mathematical Software, Vol. 4, No. 2, June 1978, pp. 148-159. Copyright 1978, Association for Computing Machinery, Inc., reprinted by permission.

### Examples

```
## Not run:
library(rgl)
data(akima)
# data
rgl.spheres(akima$x,akima$z , akima$y,0.5,color="red")
rgl.bbox()
# bivariate linear interpolation
# interp:
akima.li <- interp(akima$x, akima$y, akima$z,
                  xo=seq(min(akima$x), max(akima$x), length = 100),
                  yo=seq(min(akima$y), max(akima$y), length = 100))
# interp surface:
rgl.surface(akima.li$x,akima.li$y,akima.li$z,color="green",alpha=c(0.5))
# interpp:
akima.p <- interpp(akima$x, akima$y, akima$z,
                  runif(200,min(akima$x),max(akima$x)),
                  runif(200,min(akima$y),max(akima$y)))
# interpp points:
rgl.points(akima.p$x,akima.p$z , akima.p$y,size=4,color="yellow")

# bivariate spline interpolation
# data
rgl.spheres(akima$x,akima$z , akima$y,0.5,color="red")
rgl.bbox()
# bivariate cubic spline interpolation
# interp:
akima.si <- interp(akima$x, akima$y, akima$z,
                  xo=seq(min(akima$x), max(akima$x), length = 100),
                  yo=seq(min(akima$y), max(akima$y), length = 100),
                  linear = FALSE, extrap = TRUE)
```

```

# interp surface:
rgl.surface(akima.si$x,akima.si$y,akima.si$z,color="green",alpha=c(0.5))
# interpp:
akima.sp <- interpp(akima$x, akima$y, akima$z,
                   runif(200,min(akima$x),max(akima$x)),
                   runif(200,min(akima$y),max(akima$y)),
                   linear = FALSE, extrap = TRUE)
# interpp points:
rgl.points(akima.sp$x,akima.sp$z , akima.sp$y,size=4,color="yellow")

## End(Not run)

```

---

akima760	<i>Sample data from Akima's Bicubic Spline Interpolation code (TOMS 760)</i>
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## Description

akima760 is a list with vector components x, y and a matrix z which represents a smooth surface of z values at the points of a regular grid spanned by the vectors x and y.

## References

Hiroshi Akima, "  
", ACM Transactions on Mathematical Software, Vol. 22, No. 3, September 1996, pp. 357-361.

## Examples

```

## Not run:
library(rgl)
data(akima)
# data
rgl.spheres(akima760$x,akima760$z , akima760$y,0.5,color="red")
rgl.bbox()
# bivariate linear interpolation
# interp:
akima.li <- interp(akima$x, akima$y, akima$z,
                  xo=seq(min(akima$x), max(akima$x), length = 100),
                  yo=seq(min(akima$y), max(akima$y), length = 100))
# interp surface:
rgl.surface(akima.li$x,akima.li$y,akima.li$z,color="green",alpha=c(0.5))
# interpp:
akima.p <- interpp(akima$x, akima$y, akima$z,
                  runif(200,min(akima$x),max(akima$x)),
                  runif(200,min(akima$y),max(akima$y)))
# interpp points:
rgl.points(akima.p$x,akima.p$z , akima.p$y,size=4,color="yellow")

```

```

# bivariate spline interpolation
# data
rgl.spheres(akima$x,akima$z , akima$y,0.5,color="red")
rgl.bbox()
# bivariate cubic spline interpolation
# interp:
akima.si <- interp(akima$x, akima$y, akima$z,
                  xo=seq(min(akima$x), max(akima$x), length = 100),
                  yo=seq(min(akima$y), max(akima$y), length = 100),
                  linear = FALSE, extrap = TRUE)
# interp surface:
rgl.surface(akima.si$x,akima.si$y,akima.si$z,color="green",alpha=c(0.5))
# interpp:
akima.sp <- interpp(akima$x, akima$y, akima$z,
                   runif(200,min(akima$x),max(akima$x)),
                   runif(200,min(akima$y),max(akima$y)),
                   linear = FALSE, extrap = TRUE)
# interpp points:
rgl.points(akima.sp$x,akima.sp$z , akima.sp$y,size=4,color="yellow")

## End(Not run)

```

---

aspline

*Univariate Akima interpolation*


---

## Description

The function returns a list of points which smoothly interpolate given data points, similar to a curve drawn by hand.

## Usage

```
aspline(x, y=NULL, xout, n = 50, ties = mean, method="original", degree=3)
```

## Arguments

x, y	vectors giving the coordinates of the points to be interpolated. Alternatively a single plotting structure can be specified: see <a href="#">xy.coords</a> .
xout	an optional set of values specifying where interpolation is to take place.
n	If xout is not specified, interpolation takes place at n equally spaced points spanning the interval $[\min(x), \max(x)]$ .
ties	Handling of tied x values. Either a function with a single vector argument returning a single number result or the string "ordered".
method	either "original" method after Akima (1970) or "improved" method after Akima (1991)
degree	if improved algorithm is selected: degree of the polynomials for the interpolating function

## Details

The original algorithm is based on a piecewise function composed of a set of polynomials, each of degree three, at most, and applicable to successive interval of the given points. In this method, the slope of the curve is determined at each given point locally, and each polynomial representing a portion of the curve between a pair of given points is determined by the coordinates of and the slopes at the points.

## Value

A list with components `x` and `y`, containing `n` coordinates which interpolate the given data points.

## References

Akima, H. (1970) A new method of interpolation and smooth curve fitting based on local procedures, *J. ACM* **17**(4), 589-602

Akima, H. (1991) A Method of Univariate Interpolation that Has the Accuracy of a Third-degree Polynomial. *ACM Transactions on Mathematical Software*, **17**(3), 341-366.

## See Also

[approx](#), [spline](#)

## Examples

```
## regular spaced data
x <- 1:10
y <- c(rnorm(5), c(1,1,1,1,3))

xnew <- seq(-1, 11, 0.1)
plot(x, y, ylim=c(-3, 3), xlim=range(xnew))
lines(spline(x, y, xmin=min(xnew), xmax=max(xnew), n=200), col="blue")

lines(aspline(x, y, xnew), col="red")
lines(aspline(x, y, xnew, method="improved"), col="black", lty="dotted")
lines(aspline(x, y, xnew, method="improved", degree=10), col="green", lty="dashed")

## irregular spaced data
x <- sort(runif(10, max=10))
y <- c(rnorm(5), c(1,1,1,1,3))

xnew <- seq(-1, 11, 0.1)
plot(x, y, ylim=c(-3, 3), xlim=range(xnew))
lines(spline(x, y, xmin=min(xnew), xmax=max(xnew), n=200), col="blue")

lines(aspline(x, y, xnew), col="red")
lines(aspline(x, y, xnew, method="improved"), col="black", lty="dotted")
lines(aspline(x, y, xnew, method="improved", degree=10), col="green", lty="dashed")

## an example of Akima, 1991
x <- c(-3, -2, -1, 0, 1, 2, 2.5, 3)
y <- c(0, 0, 0, 0, -1, -1, 0, 2)
```

```

plot(x, y, ylim=c(-3, 3))
lines(spline(x, y, n=200), col="blue")

lines(aspline(x, y, n=200), col="red")
lines(aspline(x, y, n=200, method="improved"), col="black", lty="dotted")
lines(aspline(x, y, n=200, method="improved", degree=10), col="green", lty="dashed")

```

---

bicubic

*Bivariate Interpolation for Data on a Rectangular grid*


---

### Description

The description in the Fortran code says:

This subroutine performs interpolation of a bivariate function,  $z(x,y)$ , on a rectangular grid in the  $x$ - $y$  plane. It is based on the revised Akima method.

In this subroutine, the interpolating function is a piecewise function composed of a set of bicubic (bivariate third-degree) polynomials, each applicable to a rectangle of the input grid in the  $x$ - $y$  plane. Each polynomial is determined locally.

This subroutine has the accuracy of a bicubic polynomial, i.e., it interpolates accurately when all data points lie on a surface of a bicubic polynomial.

The grid lines can be unevenly spaced.

### Usage

```
bicubic(x, y, z, x0, y0)
```

### Arguments

$x$	a vector containing the $x$ coordinates of the rectangular data grid.
$y$	a vector containing the $y$ coordinates of the rectangular data grid.
$z$	a matrix containing the $z[i, j]$ data values for the grid points $(x[i], y[j])$ .
$x0$	vector of $x$ coordinates used to interpolate at.
$y0$	vector of $y$ coordinates used to interpolate at.

### Details

This function is a R interface to Akima's Rectangular-Grid-Data Fitting algorithm (TOMS 760). The algorithm has the accuracy of a bicubic (bivariate third-degree) polynomial.

**Value**

This function produces a list of interpolated points:

x                    vector of x coordinates.  
 y                    vector of y coordinates.  
 z                    vector of interpolated data z.

If you need an output grid, see [bicubic.grid](#).

**Note**

Use [interp](#) for the general case of irregular gridded data!

**References**

Akima, H. (1996) Rectangular-Grid-Data Surface Fitting that Has the Accuracy of a Bicubic Polynomial, J. ACM **22**(3), 357-361

**See Also**

[interp](#), [bicubic.grid](#)

**Examples**

```
data(akima760)
# interpolate at the diagonal of the grid [0,8]x[0,10]
akima.bic <- bicubic(akima760$x,akima760$y,akima760$z,
                    seq(0,8,length=50), seq(0,10,length=50))
plot(sqrt(akima.bic$x^2+akima.bic$y^2), akima.bic$z, type="l")

##---- Should be DIRECTLY executable !! ----
##-- ==> Define data, use random,
##--or do help(data=index) for the standard data sets.

## The function is currently defined as
function (x, y, z, x0, y0)
{
  nx <- length(x)
  ny <- length(y)
  if (dim(z)[1] != nx)
    stop("dim(z)[1] and length of x differs!")
  if (dim(z)[2] != ny)
    stop("dim(z)[2] and length of y differs!")
  n0 <- length(x0)
  if (length(y0) != n0)
    stop("length of y0 and x0 differs!")
  ret <- .Fortran("rgbi3p", md = as.integer(1), nxd = as.integer(nx),
                nyd = as.integer(ny), xd = as.double(x), yd = as.double(y),
                zd = as.double(z), nip = as.integer(n0), xi = as.double(x0),
                yi = as.double(y0), zi = double(n0), ier = integer(1),
```

```

      wk = double(3 * nx * ny), PACKAGE = "akima")
    list(x = x0, y = y0, z = ret$zi)
  }

```

---

 bicubic.grid

*Bivariate Interpolation for Data on a Rectangular grid*


---

### Description

The description in the Fortran code says:

This subroutine performs interpolation of a bivariate function,  $z(x,y)$ , on a rectangular grid in the  $x$ - $y$  plane. It is based on the revised Akima method.

In this subroutine, the interpolating function is a piecewise function composed of a set of bicubic (bivariate third-degree) polynomials, each applicable to a rectangle of the input grid in the  $x$ - $y$  plane. Each polynomial is determined locally.

This subroutine has the accuracy of a bicubic polynomial, i.e., it interpolates accurately when all data points lie on a surface of a bicubic polynomial.

The grid lines can be unevenly spaced.

### Usage

```
bicubic.grid(x,y,z,xlim,ylim,dx,dy)
```

### Arguments

<code>x</code>	a vector containing the $x$ coordinates of the rectangular data grid.
<code>y</code>	a vector containing the $y$ coordinates of the rectangular data grid.
<code>z</code>	a matrix containing the $z[i,j]$ data values for the grid points $(x[i],y[j])$ .
<code>xlim</code>	vector of length 2 giving lower and upper limit for range $x$ coordinates used for output grid.
<code>ylim</code>	vector of length 2 giving lower and upper limit for range of $y$ coordinates used for output grid.
<code>dx</code>	output grid spacing in $x$ direction.
<code>dy</code>	output grid spacing in $y$ direction.

### Details

This function is a R interface to Akima's Rectangular-Grid-Data Fitting algorithm (TOMS 760). The algorithm has the accuracy of a bicubic (bivariate third-degree) polynomial.



**Value**

This function produces a grid of interpolated points, feasible to be used directly with [image](#) and [contour](#):

x                    vector of x coordinates of the output grid.  
y                    vector of y coordinates of the output grid.  
z                    matrix of interpolated data for the output grid.

**Note**

Use [interp](#) for the general case of irregular gridded data!

**References**

Akima, H. (1996) Rectangular-Grid-Data Surface Fitting that Has the Accuracy of a Bicubic Polynomial, *J. ACM* **22**(3), 357-361

**See Also**

[interp](#), [bicubic](#)

**Examples**

```
data(akima760)
# interpolate at a grid [0,8]x[0,10]
akima.bic <- bicubic.grid(akima760$x,akima760$y,akima760$z,
                        c(0,8),c(0,10),0.1,0.1)
image(akima.bic)
contour(akima.bic, add=TRUE)
```

---

 interp

*Gridded Bivariate Interpolation for Irregular Data*


---

**Description**

These functions implement bivariate interpolation onto a grid for irregularly spaced input data. Bilinear or bicubic spline interpolation is applied using different versions of algorithms from Akima.

**Usage**

```
interp(x, y, z, xo=seq(min(x), max(x), length = 40),
      yo=seq(min(y), max(y), length = 40),
      linear = TRUE, extrap=FALSE, duplicate = "error", dupfun = NULL, ncp = NULL)
interp.old(x, y, z, xo= seq(min(x), max(x), length = 40),
          yo=seq(min(y), max(y), length = 40), ncp = 0,
          extrap=FALSE, duplicate = "error", dupfun = NULL)
interp.new(x, y, z, xo = seq(min(x), max(x), length = 40),
          yo = seq(min(y), max(y), length = 40), linear = FALSE,
          ncp = NULL, extrap=FALSE, duplicate = "error", dupfun = NULL)
```

**Arguments**

x	vector of x-coordinates of data points. Missing values are not accepted.
y	vector of y-coordinates of data points. Missing values are not accepted.
z	vector of z-coordinates of data points. Missing values are not accepted. x, y, and z must be the same length and may contain no fewer than four points. The points of x and y cannot be collinear, i.e, they cannot fall on the same line (two vectors x and y such that $y = ax + b$ for some a, b will not be accepted). interp is meant for cases in which you have x, y values scattered over a plane and a z value for each. If, instead, you are trying to evaluate a mathematical function, or get a graphical interpretation of relationships that can be described by a polynomial, try <code>outer()</code> .
xo	vector of x-coordinates of output grid. The default is 40 points evenly spaced over the range of x. If extrapolation is not being used ( <code>extrap=FALSE</code> , the default), xo should have a range that is close to or inside of the range of x for the results to be meaningful.
yo	vector of y-coordinates of output grid; analogous to xo, see above.
linear	logical – indicating whether linear or spline interpolation should be used. supersedes old ncp parameter
ncp	deprecated, use parameter linear. Now only used by <code>interp.old()</code> . meaning was: number of additional points to be used in computing partial derivatives at each data point. ncp must be either 0 (partial derivatives are not used), or at least 2 but smaller than the number of data points (and smaller than 25).
extrap	logical flag: should extrapolation be used outside of the convex hull determined by the data points?
duplicate	character string indicating how to handle duplicate data points. Possible values are "error" produces an error message, "strip" remove duplicate z values, "mean","median","user" calculate mean, median or user defined function (dupfun) of duplicate z values.
dupfun	a function, applied to duplicate points if duplicate= "user".

**Details**

If linear is TRUE (default), linear interpolation is used in the triangles bounded by data points. Cubic interpolation is done if linear is set to FALSE. If extrap is FALSE, z-values for points outside the convex hull are returned as NA. No extrapolation can be performed for the linear case.

The interp function handles duplicate (x,y) points in different ways. As default it will stop with an error message. But it can give duplicate points an unique z value according to the parameter duplicate (mean,median or any other user defined function).

The triangulation scheme used by interp works well if x and y have similar scales but will appear stretched if they have very different scales. The spreads of x and y must be within four orders of magnitude of each other for interp to work.

**Value**

list with 3 components:

<code>x,y</code>	vectors of x- and y- coordinates of output grid, the same as the input argument <code>xo</code> , or <code>yo</code> , if present. Otherwise, their default, a vector 40 points evenly spaced over the range of the input <code>x</code> .
<code>z</code>	matrix of fitted z-values. The value <code>z[i, j]</code> is computed at the x,y point <code>xo[i]</code> , <code>yo[j]</code> . <code>z</code> has dimensions <code>length(xo)</code> times <code>length(yo)</code> .

**Note**

`interp` is a wrapper for the two versions `interp.old` (it uses (almost) the same Fortran code from Akima 1978 as the S-Plus version) and `interp.new` (it is based on new Fortran code from Akima 1996). For linear interpolation the old version is chosen, but spline interpolation is done by the new version.

Earlier versions (pre 0.5-1) of `interp` used the parameter `ncp` to choose between linear and cubic interpolation, this is now done by setting the logical parameter `linear`. Use of `ncp` is still possible, but is deprecated.

The resulting structure is suitable for input to the functions `contour` and `image`. Check the requirements of these functions when choosing values for `xo` and `yo`.

**References**

Akima, H. (1978). A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points. *ACM Transactions on Mathematical Software* **4**, 148-164.

Akima, H. (1996). Algorithm 761: scattered-data surface fitting that has the accuracy of a cubic polynomial. *ACM Transactions on Mathematical Software* **22**, 362–371.

**See Also**

[contour](#), [image](#), [approx](#), [spline](#), [aspline](#), [outer](#), [expand.grid](#).

**Examples**

```
data(akima)
plot(y ~ x, data = akima, main = "akima example data")
with(akima, text(x, y, formatC(z,dig=2), adj = -0.1))

## linear interpolation
akima.li <- interp(akima$x, akima$y, akima$z)
image (akima.li, add=TRUE)
contour(akima.li, add=TRUE)
points (akima, pch = 3)

## increase smoothness (using finer grid):
akima.smooth <-
  with(akima, interp(x, y, z, xo=seq(0,25, length=100),
                    yo=seq(0,20, length=100)))
image (akima.smooth, main = "interp(<akima data>, *) on finer grid")
```

```

contour(akima.smooth, add = TRUE, col = "thistle")
points(akima, pch = 3, cex = 2, col = "blue")
# use triangulation package to show underlying triangulation:
## Not run:
if(library(tripack, logical.return=TRUE))
  plot(tri.mesh(akima), add=TRUE, lty="dashed")

## End(Not run)
# use only 15 points (interpolation only within convex hull!)
akima.part <- with(akima, interp(x[1:15], y[1:15], z[1:15]))
image(akima.part)
title("interp() on subset of only 15 points")
contour(akima.part, add=TRUE)
points(akima$x[1:15], akima$y[1:15], col = "blue")

## spline interpolation, two variants (AMS 526 "Old", AMS 761 "New")
## -----
## "Old": use 5 points to calculate derivatives -> many NAs
akima.s0 <- interp.old(akima$x, akima$y, akima$z,
  xo=seq(0,25, length=100), yo=seq(0,20, length=100), ncp=5)
table(is.na(akima.s0$z)) ## 3990 NA's; = 40 %
akima.s0 <- with(akima,
  interp.old(x,y,z, xo=seq(0,25, length=100), yo=seq(0,20, len=100), ncp = 4))
sum(is.na(akima.s0$z)) ## still 3429
image (akima.s0, main = "interp.old(*, ncp = 4) [almost useless]")
contour(akima.s0, add = TRUE)

## "New:"
akima.spl <- with(akima, interp.new(x,y,z, xo=seq(0,25, length=100),
  yo=seq(0,20, length=100)))
## equivalent call via setting linear=FALSE in interp():
akima.spl <- with(akima, interp(x,y,z, xo=seq(0,25, length=100),
  yo=seq(0,20, length=100),
  linear=FALSE))

contour(akima.spl, main = "smooth interp(*, linear = FALSE)")
points(akima)

full.pal <- function(n) hcl(h = seq(340, 20, length = n))
cool.pal <- function(n) hcl(h = seq(120, 0, length = n) + 150)
warm.pal <- function(n) hcl(h = seq(120, 0, length = n) - 30)

filled.contour(akima.spl, color.palette = full.pal,
  plot.axes = { axis(1); axis(2);
    title("smooth interp(*, linear = FALSE)");
    points(akima, pch = 3, col= hcl(c=100, l = 20))})
# no extrapolation!

## example with duplicate points :

data(airquality)
air <- subset(airquality,
  !is.na(Temp) & !is.na(Ozone) & !is.na(Solar.R))

```

```
# gives an error {duplicate ..}:
try( air.ip <- interp(air$Temp,air$Solar.R,air$Ozone, linear=FALSE) )
# use mean of duplicate points:
air.ip <- with(air, interp(Temp, Solar.R, log(Ozone), duplicate = "mean",
                          linear = FALSE))
image(air.ip, main = "Airquality: Ozone vs. Temp and Solar.R")
with(air, points(Temp, Solar.R))
```

---

 interp2xyz

*From interp() Result, Produce 3-column Matrix*


---

### Description

From an `interp()` result, produce a 3-column matrix or `data.frame` `cbind(x, y, z)`.

### Usage

```
interp2xyz(al, data.frame = FALSE)
```

### Arguments

`al` a `list` as produced from `interp()`.  
`data.frame` logical indicating if result should be `data.frame` or matrix (default).

### Value

a matrix (or `data.frame`) with three columns, called "x", "y", "z".

### Author(s)

Martin Maechler, Jan.18, 2013

### See Also

`expand.grid()` is the "essential ingredient" of `interp2xyz()`.  
[interp](#).

### Examples

```
data(akima)
ak.spl <- with(akima, interp(x, y, z, linear = FALSE,
                           xo= seq(0,25, length=100),
                           yo= seq(0,20, length= 96)))
str(ak.spl)# list (x[i], y[j], z = <matrix>[i,j])

## Now transform to simple (x,y,z) matrix / data.frame :
str(am <- interp2xyz(ak.spl))
str(ad <- interp2xyz(ak.spl, data.frame=TRUE))
## and they are the same:
stopifnot( am == ad | (is.na(am) & is.na(ad)) )
```

interpp

*Pointwise Bivariate Interpolation for Irregular Data***Description**

If `ncp` is zero, linear interpolation is used in the triangles bounded by data points. Cubic interpolation is done if partial derivatives are used. If `extrap` is `FALSE`, `z`-values for points outside the convex hull are returned as `NA`. No extrapolation can be performed if `ncp` is zero.

The `interpp` function handles duplicate  $(x, y)$  points in different ways. As default it will stop with an error message. But it can give duplicate points an unique `z` value according to the parameter `duplicate` (`mean`, `median` or any other user defined function).

The triangulation scheme used by `interp` works well if `x` and `y` have similar scales but will appear stretched if they have very different scales. The spreads of `x` and `y` must be within four orders of magnitude of each other for `interpp` to work.

**Usage**

```
interpp(x, y, z, xo, yo, linear=TRUE, extrap=FALSE, duplicate = "error",
dupfun = NULL, ncp)
```

**Arguments**

<code>x</code>	vector of <code>x</code> -coordinates of data points. Missing values are not accepted.
<code>y</code>	vector of <code>y</code> -coordinates of data points. Missing values are not accepted.
<code>z</code>	vector of <code>z</code> -coordinates of data points. Missing values are not accepted.
	<code>x</code> , <code>y</code> , and <code>z</code> must be the same length and may contain no fewer than four points. The points of <code>x</code> and <code>y</code> cannot be collinear, i.e, they cannot fall on the same line (two vectors <code>x</code> and <code>y</code> such that $y = ax + b$ for some <code>a</code> , <code>b</code> will not be accepted).
<code>xo</code>	vector of <code>x</code> -coordinates of points at which to evaluate the interpolating function.
<code>yo</code>	vector of <code>y</code> -coordinates of points at which to evaluate the interpolating function.
<code>linear</code>	logical – indicating whether linear or spline interpolation should be used. supersedes old <code>ncp</code> parameter
<code>ncp</code>	deprecated, use parameter <code>linear</code> . Now only used by <code>interpp.old()</code> . meaning was: number of additional points to be used in computing partial derivatives at each data point. <code>ncp</code> must be either 0 (partial derivatives are not used, = linear interpolation), or at least 2 but smaller than the number of data points (and smaller than 25).
<code>extrap</code>	logical flag: should extrapolation be used outside of the convex hull determined by the data points?
<code>duplicate</code>	indicates how to handle duplicate data points. Possible values are "error" - produces an error message, "strip" - remove duplicate <code>z</code> values, "mean", "median", "user" - calculate mean, median or user defined function of duplicate <code>z</code> values.
<code>dupfun</code>	this function is applied to duplicate points if <code>duplicate="user"</code>

**Value**

list with 3 components:

x	vector of x-coordinates of output points, the same as the input argument <code>xo</code> .
y	vector of y-coordinates of output points, the same as the input argument <code>yo</code> .
z	fitted z-values. The value <code>z[i]</code> is computed at the x,y point <code>x[i]</code> , <code>y[i]</code> .

**NOTE**

Use `interp` if interpolation on a regular grid is wanted.

The two versions `interpp.old` and `interpp.new` refer to Akimas Fortran code from 1978 and 1996 resp. The call wrapper `interpp` chooses `interpp.old` for linear and `interpp.new` for cubic spline interpolation.

Earlier versions (pre 0.5-1) of `interpp` used the parameter `ncp` to choose between linear and cubic interpolation, this is now done by setting the logical parameter `linear`. Use of `ncp` is still possible, but is deprecated.

**References**

Akima, H. (1978). A Method of Bivariate Interpolation and Smooth Surface Fitting for Irregularly Distributed Data Points. *ACM Transactions on Mathematical Software*, **4**, 148-164.

Akima, H. (1996). Algorithm 761: scattered-data surface fitting that has the accuracy of a cubic polynomial. *ACM Transactions on Mathematical Software*, **22**, 362-371.

**See Also**

[contour](#), [image](#), [approxfun](#), [splinefun](#), [outer](#), [expand.grid](#), [interp](#), [aspline](#).

**Examples**

```
data(akima)
# linear interpolation at points (1,2), (5,6) and (10,12)
akima.lip<-interpp(akima$x, akima$y, akima$z,c(1,5,10),c(2,6,12))
akima.lip$z
# spline interpolation
akima.sip<-interpp(akima$x, akima$y, akima$z,c(1,5,10),c(2,6,12),
  linear=FALSE)
akima.sip$z
```

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