

# Package ‘StatRank’

July 2, 2014

**Type** Package

**Title** Statistical Rank Aggregation: Inference, Evaluation, and Visualization

**Version** 0.0.4

**Date** 2013-11-21

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**Description** This package implements Generalized Method of Moments and Maximal Likelihood methods for Random Utility Models. These methods are meant to provide inference on rank comparison data. These methods accept full, partial, and pairwise rankings, and provides methods to break down full or partial rankings into their pairwise components. Please see Generalized Method-of-Moments for Rank Aggregation from NIPS 2013 for a description of some of our methods.

**License** GPL (>= 2)

**Imports** truncdist, plyr

**Suggests** ggplot2, gridExtra, grid, testthat, lattice

**NeedsCompilation** no

**Repository** CRAN

**Date/Publication** 2014-03-05 18:09:29

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---

Breaking

*Breaks full or partial orderings into pairwise comparisons*

---

### Description

Given full or partial orderings, this function will generate pairwise comparison Options 1. full - All available pairwise comparisons. This is used for partial rank data where the ranked objects are a random subset of all objects 2. adjacent - Only adjacent pairwise breakings 3. top - also takes in k, will break within top k and will also generate pairwise comparisons comparing the top k with the rest of the data 4. top.partial - This is used for partial rank data where the ranked alternatives are preferred over the non-ranked alternatives

### Usage

```
Breaking(Data, method, k = NULL)
```

### Arguments

Data	data in either full or partial ranking format
method	- can be full, adjacent, top or top.partial
k	This applies to the top method, choose which top k to focus on

### Value

Pairwise breakings, where the three columns are winner, loser and rank distance (latter used for Zemel)

### Examples

```
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
```

---

`convert.vector.to.list`

*Helper function for the graphing interface*

---

### Description

As named, this function takes a vector where each element is a mean, then returns back a list, with each list item having the mean

### Usage

```
convert.vector.to.list(Parameters, name = "Mean")
```

**Arguments**

Parameters	a vector of parameters
name	Name of the parameter

**Value**

a list, where each element represents an alternative and has a Mean value

---

Data.Election1	<i>A1 Election Data</i>
----------------	-------------------------

---

**Description**

This is a public election dataset collected by Nicolaus Tideman where the voters provided partial orders on candidates. A partial order includes comparisons among a subset of alternative, and the non-mentioned alternatives in the partial order are considered to be ranked lower than the lowest ranked alternative among mentioned alternatives.

**Usage**

```
data(Data.Election1)
```

**Author(s)**

Nicolaus Tideman

---

Data.Election6	<i>A6 Election Data</i>
----------------	-------------------------

---

**Description**

This is a public election dataset collected by Nicolaus Tideman where the voters provided partial orders on candidates. A partial order includes comparisons among a subset of alternative, and the non-mentioned alternatives in the partial order are considered to be ranked lower than the lowest ranked alternative among mentioned alternatives.

**Usage**

```
data(Data.Election6)
```

**Author(s)**

Nicolaus Tideman

---

Data.Election9	<i>A9 Election Data</i>
----------------	-------------------------

---

**Description**

This is a public election dataset collected by Nicolaus Tideman where the voters provided partial orders on candidates. A partial order includes comparisons among a subset of alternative, and the non-mentioned alternatives in the partial order are considered to be ranked lower than the lowest ranked alternative among mentioned alternatives.

**Usage**

```
data(Data.Election9)
```

**Author(s)**

Nicolaus Tideman

---

Data.Nascar	<i>Nascar Data</i>
-------------	--------------------

---

**Description**

Nascar Data

**Usage**

```
data(Data.Nascar)
```

---

Data.NascarTrimmed	<i>Trimmed Nascar Data</i>
--------------------	----------------------------

---

**Description**

Nascar data that only keeps racers that are represented in between 20 - 30 of total races

**Usage**

```
data(Data.NascarTrimmed)
```

---

Data.Test	<i>Tiny test dataset</i>
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---

**Description**

This is a randomly generated tiny ranks file that we can use to test our methods

**Usage**

```
data(Data.Test)
```

---

Estimation.GRUM.MLE	<i>Performs parameter estimation for a Generalized Random Utility Model with user and alternative characteristics</i>
---------------------	-----------------------------------------------------------------------------------------------------------------------

---

**Description**

This function supports RUMs 1) Normal with fixed variance (fixed at 1)

**Usage**

```
Estimation.GRUM.MLE(Data, X, Z, iter, dist, din, Bin)
```

**Arguments**

Data	data in either partial or full rankings
X	user characteristics
Z	alternative characteristics
iter	number of iterations to run algorithm
dist	choice of distribution
din	initialization of delta vector
Bin	intialization of B matrix

**Value**

results from the inference

**Examples**

```
#data(Data.Test)
#Data.X= matrix( runif(15),5,3)
#Data.Z= matrix(runif(10),2,5)
#Estimation.GRUM.MLE(Data.Test, Data.X, Data.Z, iter = 3, dist = "norm",
#din=runif(5), Bin=matrix(runif(6),3,2))
```

---

Estimation.Normal.GMM *GMM Method for Estimating Random Utility Model with Normal Distributions*

---

**Description**

GMM Method for Estimating Random Utility Model with Normal Distributions

**Usage**

```
Estimation.Normal.GMM(Data.pairs, m, iter = 1000, Var = FALSE, prior = 0)
```

**Arguments**

Data.pairs	data broken up into pairs
m	number of alternatives
iter	number of iterations to run
Var	indicator for difference variance (default is FALSE)
prior	magnitude of fake observations input into the model

**Value**

Estimated mean parameters for distribution of underlying normal (variance is fixed at 1)

**Examples**

```
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
Estimation.Normal.GMM(Data.Test.pairs, 5)
```

---

Estimation.PL.GMM *GMM Method for Estimating Plackett-Luce Model Parameters*

---

**Description**

GMM Method for Estimating Plackett-Luce Model Parameters

**Usage**

```
Estimation.PL.GMM(Data.pairs, m, prior = 0, weighted = FALSE)
```

**Arguments**

<code>Data.pairs</code>	data broken up into pairs
<code>m</code>	number of alternatives
<code>prior</code>	magnitude of fake observations input into the model
<code>weighted</code>	if this is true, then the third column of <code>Data.pairs</code> is used as a weight for that data point

**Value**

Estimated mean parameters for distribution of underlying exponential

**Examples**

```
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
Estimation.PL.GMM(Data.Test.pairs, 5)
```

---

<code>Estimation.PL.MLE</code>	<i>Performs parameter estimation for the Plackett-Luce model using an Minorize Maximize algorithm</i>
--------------------------------	-------------------------------------------------------------------------------------------------------

---

**Description**

Performs parameter estimation for the Plackett-Luce model using an Minorize Maximize algorithm

**Usage**

```
Estimation.PL.MLE(Data, iter = 10)
```

**Arguments**

<code>Data</code>	data in either partial or full rankings (Partial rank case works for settings like car racing)
<code>iter</code>	number of MM iterations to run

**Value**

list of estimated means (Gamma) and the log likelihoods

**Examples**

```
data(Data.Test)
Estimation.PL.MLE(Data.Test)
```



---

Estimation.RUM.MLE	<i>Performs parameter estimation for a Random Utility Model with different noise distributions</i>
--------------------	----------------------------------------------------------------------------------------------------

---

**Description**

This function supports RUMs 1) Normal 2) Normal with fixed variance (fixed at 1) 3) Exponential (top k setting like Election)

**Usage**

```
Estimation.RUM.MLE(Data, iter = 10, dist, race = FALSE)
```

**Arguments**

Data	data in either partial or full rankings
iter	number of EM iterations to run
dist	underlying distribution. Can be "norm", "norm.fixedvariance", "exp"
race	indicator that each agent chose a random subset of alternatives to compare

**Value**

parameters of the latent RUM distributions

**Examples**

```
Data.Tiny <- matrix(c(1, 2, 3, 3, 2, 1, 1, 2, 3), ncol = 3, byrow = TRUE)
Estimation.RUM.MLE(Data.Tiny, iter = 2, dist="norm")
```

---

Estimation.RUM.MultiType.MLE	<i>Performs parameter estimation for a Multitype Random Utility Model</i>
------------------------------	---------------------------------------------------------------------------

---

**Description**

This function supports RUMs 1) Normal 2) Normal with fixed variance (fixed at 1) 3) Exponential

**Usage**

```
Estimation.RUM.MultiType.MLE(Data, K = 2, iter = 10, dist, ratio = 0.2,
  race = FALSE)
```

**Arguments**

Data	data in either partial or full rankings
K	number of components in mixture distribution
iter	number of EM iterations to run
dist	underlying distribution. Can be "norm", "norm.fixedvariance", "exp"
ratio	parameter in the algorithm that controls the difference of the starting points, the bigger the ratio the more the distance
race	TRUE if data is sub partial, FALSE (default) if not

**Value**

results from the inference

**Examples**

```
Data.Tiny <- matrix(c(1, 2, 3, 3, 2, 1, 1, 2, 3), ncol = 3, byrow = TRUE)
Estimation.RUM.MultiType.MLE(Data.Tiny, K=2, iter = 3, dist= "norm.fixedvariance")
```

---

Estimation.RUM.Nonparametric

*Nonparametric RUM Estimator*

---

**Description**

Given rank data (full, top partial, or sub partial), this function returns an inference object that fits nonparametric latent utilities on the rank data.

**Usage**

```
Estimation.RUM.Nonparametric(Data, m, iter = 10, bw = 0.025,
  utilities.per.agent = 20, race = FALSE)
```

**Arguments**

Data	full, top partial, or sub partial rank data
m	number of alternatives
iter	number of EM iterations to run
bw	bandwidth, or smoothing parameter for KDE
utilities.per.agent	Number of utility vector samples that we get per agent. More generally gives a more accurate estimate
race	TRUE if data is sub partial, FALSE (default) if not

**Examples**

```
data(Data.Test)
Estimation.RUM.Nonparametric(Data.Test, m = 5, iter = 3)
```

---

Estimation.Zemel.MLE *Estimates Zemel Parameters via Gradient Descent*

---

**Description**

This function takes in data broken into pairs, and estimates the parameters of the Zemel mode via Gradient Descent

**Usage**

```
Estimation.Zemel.MLE(Data.pairs, m, threshold = 1e-04,
  learning.rate = 1/30000)
```

**Arguments**

Data.pairs	data broken up into pairwise comparisons
m	how many alternatives
threshold	turning parameter for gradient descent
learning.rate	turning parameter for gradient descent

**Value**

a set of scores for the alternatives, normalized such that the sum of the log scores is 0 scores <- Generate.Zemel.Parameters(10)\$Score pairs <- Generate.Zemel.Ranks.Pairs(scores, 10, 10) Estimation.Zemel.MLE(pairs, 10, threshold = .1)

---

Evaluation.AveragePrecision  
*Calculates the Average Precision*

---

**Description**

Calculates the Average Precision

**Usage**

```
Evaluation.AveragePrecision(EstimatedRank, RelevanceLevel)
```

**Arguments**

EstimatedRank	estimated ranking
RelevanceLevel	score for the document

**Value**

The AP for this estimation and relevance level

**Examples**

```
EstimatedRank <- scramble(1:10)
RelevanceLevel <- runif(10)
Evaluation.AveragePrecision(EstimatedRank, RelevanceLevel)
```

---

Evaluation.KendallTau *Calculates the Kendall Tau correlation between two ranks*

---

**Description**

Calculates the Kendall Tau correlation between two ranks

**Usage**

```
Evaluation.KendallTau(rank1, rank2)
```

**Arguments**

rank1	two rankings. Order does not matter
rank2	two rankings. Order does not matter

**Value**

The Kendall Tau correlation

**Examples**

```
rank1 <- scramble(1:10)
rank2 <- scramble(1:10)
Evaluation.KendallTau(rank1, rank2)
```

---

Evaluation.KL	<i>Calculates KL divergence between empirical pairwise preferences and modeled pairwise preferences</i>
---------------	---------------------------------------------------------------------------------------------------------

---

### Description

Calculates KL divergence between empirical pairwise preferences and modeled pairwise preferences

### Usage

```
Evaluation.KL(Data.pairs, m, Estimate, pairwise.prob = NA, prior = 0,
  nonparametric = FALSE, ...)
```

### Arguments

<code>Data.pairs</code>	data broken up into pairs using <code>Breaking</code> function
<code>m</code>	number of alternatives
<code>Estimate</code>	estimation object from an <code>Estimate</code> function
<code>pairwise.prob</code>	Function that given two alternatives from the <code>Parameters</code> argument, returns back a model probability that one is larger than the other
<code>prior</code>	prior weight to put in pairwise frequency matrix
<code>nonparametric</code>	indicator that model is nonparametric (default <code>FALSE</code> )
<code>...</code>	additional arguments passed to <code>generateC.model</code>

### Value

the KL divergence between modeled and empirical pairwise preferences, thinking of the probabilities as a probability distribution over the  $(n \text{ choose } 2)$  pairs

### Examples

```
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
m <- 5
Estimate <- Estimation.PL.GMM(Data.Test.pairs, m)
Evaluation.KL(Data.Test.pairs, m, Estimate, PL.Pairwise.Prob)
```

Evaluation.LocationofWinner

*Calculates the location of the True winner in the estimated ranking*

---

### **Description**

Calculates the location of the True winner in the estimated ranking

### **Usage**

```
Evaluation.LocationofWinner(EstimatedRank, TrueRank)
```

### **Arguments**

EstimatedRank estimated ranking

TrueRank true ranking

### **Value**

The location of the true best in the estimated rank

### **Examples**

```
rank1 <- scramble(1:10)
rank2 <- scramble(1:10)
Evaluation.LocationofWinner(rank1, rank2)
```

---

Evaluation.MSE

*Calculates MSE between empirical pairwise preferences and modeled pairwise preferences*

---

### **Description**

Calculates MSE between empirical pairwise preferences and modeled pairwise preferences

### **Usage**

```
Evaluation.MSE(Data.pairs, m, Estimate, pairwise.prob = NA, prior = 0,
nonparametric = FALSE, ...)
```

**Arguments**

Data.pairs	data broken up into pairs using Breaking function
m	number of alternatives
Estimate	estimation object from an Estimate function
pairwise.prob	Function that given two alternatives from
prior	prior weight to put in pairwise frequency matrix
nonparametric	indicator that model is nonparametric (default FALSE) the the Parameters argument, returns back a model probability that one is larger than the other
...	additioanal parameters passed into generateC.model

**Value**

the KL divergence between modeled and empirical pairwise preferences, thinking of the probabilities as a probability distribution over the (n choose 2) pairs

**Examples**

```
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
m <- 5
Estimate <- Estimation.PL.GMM(Data.Test.pairs, m)
Evaluation.MSE(Data.Test.pairs, m, Estimate, PL.Pairwise.Prob)
```

---

Evaluation.NDCG

*Calculates the Normalized Discounted Cumluative Gain*


---

**Description**

Calculates the Normalized Discounted Cumluative Gain

**Usage**

```
Evaluation.NDCG(EstimatedRank, RelevanceLevel)
```

**Arguments**

EstimatedRank	estimated ranking
RelevanceLevel	score for the document

**Value**

The NDCG for this estimation and relevance level

**Examples**

```
EstimatedRank <- scramble(1:10)
RelevanceLevel <- runif(10)
Evaluation.NDCG(EstimatedRank, RelevanceLevel)
```

---

Evaluation.Precision.at.k

*Calculates the Average Precision at k*

---

### Description

Calculates the Average Precision at k

### Usage

```
Evaluation.Precision.at.k(EstimatedRank, RelevanceLevel, k)
```

### Arguments

EstimatedRank estimated ranking

RelevanceLevel score for the document

k positive that we want to run this algorithm for

### Value

The AP at k for this estimation and relevance level

### Examples

```
EstimatedRank <- scramble(1:10)
RelevanceLevel <- runif(10)
Evaluation.Precision.at.k(EstimatedRank, RelevanceLevel, 5)
```

---

Evaluation.TVD

*Calculates TVD between empirical pairwise preferences and modeled pairwise preferences*

---

### Description

Calculates TVD between empirical pairwise preferences and modeled pairwise preferences

### Usage

```
Evaluation.TVD(Data.pairs, m, Estimate, pairwise.prob = NA, prior = 0,
  nonparametric = FALSE, ...)
```



**Arguments**

Data.pairs	data broken up into pairs using Breaking function
m	number of alternatives
Estimate	estimation object from an Estimate function
pairwise.prob	Function that given two alternatives from
prior	prior weight to put in pairwise frequency matrix
nonparametric	indicator that model is nonparametric (default FALSE) the the Parameters argument, returns back a model probability that one is larger than the other
...	additional arguments passed to generateC.model

**Value**

the TVD between modeled and empirical pairwise preferences, thinking of the probabilities as a probability distribution over the  $(n \text{ choose } 2)$  pairs

**Examples**

```
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
m <- 5
Estimate <- Estimation.PL.GMM(Data.Test.pairs, m)
Evaluation.TVD(Data.Test.pairs, m, Estimate, PL.Pairwise.Prob)
```

---

Expo.MultiType.Pairwise.Prob

*Pairwise Probability for PL Multitype Model*

---

**Description**

Given alternatives a and b (both items from the inference object) what is the probability that a beats b?

**Usage**

```
Expo.MultiType.Pairwise.Prob(a, b)
```

**Arguments**

a	list containing parameters for a
b	list containing parameters for b

**Value**

probability that a beats b

---

Generate.NPRUM.Data     *Generate data from an NPRUM model*

---

### Description

This is useful for performing inference tasks for NPRUM

### Usage

```
Generate.NPRUM.Data(Estimate, n, bw = 0.1)
```

### Arguments

Estimate	fitted NPRUM object
n	number of agents that we want in our sample
bw	smoothing parameter to use when sampling data

### Examples

```
Data.Tiny <- matrix(c(1, 2, 3, 3, 2, 1, 1, 2, 3), ncol = 3, byrow = TRUE)
Estimate <- Estimation.RUM.Nonparametric(Data.Tiny, m = 3, iter = 3)
Generate.NPRUM.Data(Estimate, 3, bw = 0.1)
```

---

Generate.RUM.Data     *Generate observation of ranks given parameters*

---

### Description

Given a list of parameters (generated via the Generate RUM Parameters function), generate random utilities from these models and then return their ranks

### Usage

```
Generate.RUM.Data(Params, m, n, distribution)
```

### Arguments

Params	inference object from an Estimation function, or parameters object from a generate function
m	number of alternatives
n	number of agents
distribution	can be either 'normal' or 'exponential'

**Value**

a matrix of observed rankings

**Examples**

```
Params = Generate.RUM.Parameters(10, "normal")
Generate.RUM.Data(Params,m=10,n=5,"normal")
Params = Generate.RUM.Parameters(10, "exponential")
Generate.RUM.Data(Params,m=10,n=5,"exponential")
```

---

Generate.RUM.Parameters

*Parameter Generation for a RUM model*

---

**Description**

Exponential models mean parameters are drawn from a uniform distribution Normal models, mean and standard deviation parameters are drawn from a standard uniform

**Usage**

```
Generate.RUM.Parameters(m, distribution)
```

**Arguments**

m	number of sets of parameters to be drawn
distribution	either 'normal' or 'exponential'

**Value**

a list of RUM parameters

**Examples**

```
Generate.RUM.Parameters(10, "normal")
Generate.RUM.Parameters(10, "exponential")
```

Generate.Zemel.Parameters

*Generates possible scores for a Zemel model*

---

**Description**

Generates possible scores for a Zemel model

**Usage**

Generate.Zemel.Parameters(m)

**Arguments**

m                      Number of alternatives

**Value**

a set of scores, all whose logs sum to 1

**Examples**

Generate.Zemel.Parameters(10)

---

Generate.Zemel.Ranks.Pairs

*Generates pairwise ranks from a Zemel model given a set of scores*

---

**Description**

Generates pairwise ranks from a Zemel model given a set of scores

**Usage**

Generate.Zemel.Ranks.Pairs(scores, m, n)

**Arguments**

scores                a vector of scores

m                      Number of alternatives

n                      Number of pairwise alternatives to generate

**Value**

simulated pairwise comparison data

**Examples**

```
scores <- Generate.Zem1.Parameters(10)$Score
Generate.Zem1.Ranks.Pairs(scores, 10, 10)
```

---

 generateC
 

---



---

*Generate a matrix of pairwise wins*


---

**Description**

This function takes in data that has been broken up into pair format. The user is given a matrix C, where element C[i, j] represents (if normalized is FALSE) exactly how many times alternative i has beaten alternative j (if normalized is TRUE) the observed probability that alternative i beats j

**Usage**

```
generateC(Data.pairs, m, weighted = FALSE, prior = 0, normalized = TRUE)
```

**Arguments**

Data.pairs	the data broken up into pairs
m	the total number of alternatives
weighted	whether or not this generateC should use the third column of Data.pairs as the weights
prior	the initial "fake data" that you want to include in C. A prior of 1 would mean that you initially "observe" that all alternatives beat all other alternatives exactly once.
normalized	if TRUE, then normalizes entries to probabilities

**Value**

a Count matrix of how many times alternative i has beat alternative j

**Examples**

```
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
generateC(Data.Test.pairs, 5)
```

---

generateC.model      *Turns inference object into modeled C matrix.*

---

### Description

For parametric models, plug in a pairwise function for get.pairwise.prob. For nonparametric models, set nonparametric = TRUE

### Usage

```
generateC.model(Estimate, get.pairwise.prob = NA, nonparametric = FALSE,
  ...)
```

### Arguments

Estimate	inference object with a Parameter element, with a list of parameters for each alternative
get.pairwise.prob	(use this if its a parametric model) function that takes in two lists of parameters and computes the probability that the first is ranked higher than the second
nonparametric	set this flag to TRUE if this is a non-parametric model
...	additional arguments passed to generateC.model.Nonparametric (bandwidth)

### Examples

```
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
Estimate <- Estimation.Normal.GMM(Data.Test.pairs, 5)
generateC.model(Estimate, Normal.Pairwise.Prob)
```

---

generateC.model.Nonparametric  
*Generate pairwise matrix for an NPRUM model*

---

### Description

Generates a matrix where entry  $i, j$  is the estimated probability that alternative  $i$  beats alternative  $j$

### Usage

```
generateC.model.Nonparametric(Estimate, bw = 0.1)
```

### Arguments

Estimate	fitted NPRUM object
bw	bandwidth used for generating the pairwise probabilities

**Examples**

```
data(Data.Test)
Estimate <- Estimation.RUM.Nonparametric(Data.Test, m = 5, iter = 3)
generateC.model.Nonparametric(Estimate)
```

---

KL	<i>Calculates KL Divergence between non-diagonal entries of two matrices</i>
----	------------------------------------------------------------------------------

---

**Description**

Calculates KL Divergence between non-diagonal entries of two matrices

**Usage**

```
KL(A, B)
```

**Arguments**

A	first matrix, this is the "true" distribution
B	second matrix, this is the "estimated" distribution

**Value**

KL divergence

**Examples**

```
KL(matrix(runif(25), nrow=5), matrix(runif(25), nrow=5))
```

---

Likelihood.Nonparametric	<i>Calculate Likelihood for the nonparametric model</i>
--------------------------	---------------------------------------------------------

---

**Description**

Computes likelihood in the case that we assume no correlation structure

**Usage**

```
Likelihood.Nonparametric(Data, Estimate, race = FALSE)
```

**Arguments**

Data	full, top partial, or subpartial data
Estimate	fitted NPRUM object
race	indicator that the data is from subpartial data

**Examples**

```
data(Data.Test)
Estimate <- Estimation.RUM.Nonparametric(Data.Test, m = 5, iter = 3)
Likelihood.Nonparametric(Data.Test, Estimate)
```

---

Likelihood.PL	<i>A faster Likelihood for Plackett-Luce Model</i>
---------------	----------------------------------------------------

---

**Description**

A faster Likelihood for Plackett-Luce Model

**Usage**

```
Likelihood.PL(Data, parameter)
```

**Arguments**

Data	ranking data
parameter	Mean of Exponential Distribution

**Value**

log likelihood

**Examples**

```
data(Data.Test)
parameter = Generate.RUM.Parameters(5, "exponential")
Likelihood.PL(Data.Test, parameter)
```

---

Likelihood.RUM	<i>Likelihood for general Random Utility Models</i>
----------------	-----------------------------------------------------

---

**Description**

Likelihood for general Random Utility Models

**Usage**

```
Likelihood.RUM(Data, parameter, dist = "exp", range = NA, res = NA,
  race = FALSE)
```



**Arguments**

Data	ranking data
parameter	Mean of Exponential Distribution
dist	exp or norm
range	range
res	res
race	TRUE if data is sub partial, FALSE (default) if not

**Value**

log likelihood

**Examples**

```
data(Data.Test)
parameter = Generate.RUM.Parameters(5, "normal")
Likelihood.RUM(Data.Test,parameter, "norm")
```

---

Likelihood.RUM.Multitype

*Likelihood for Multitype Random Utility Models*

---

**Description**

Likelihood for Multitype Random Utility Models

**Usage**

```
Likelihood.RUM.Multitype(Data, Estimate, dist, race = FALSE)
```

**Arguments**

Data	n by m table of rankings
Estimate	Inference object from Estimation function
dist	Distribution of noise (exp or norm)
race	TRUE if data is sub partial, FALSE (default) if not

**Value**

log likelihood

**Examples**

```
Data.Tiny <- matrix(c(1, 2, 3, 3, 2, 1, 1, 2, 3), ncol = 3, byrow = TRUE)
Estimate <- Estimation.RUM.MultiType.MLE(Data.Tiny, K=2, iter = 1, dist= "norm")
Likelihood.RUM.Multitype(Data.Tiny, Estimate, dist = "norm")
```

---

Likelihood.Zemel	<i>Gives Zemel pairwise Log-likelihood with data and scores</i>
------------------	-----------------------------------------------------------------

---

**Description**

Calculates the log-likelihood in the pairwise Zemel model

**Usage**

```
Likelihood.Zemel(Data.pairs, Estimate)
```

**Arguments**

Data.pairs	data broken up into pairwise comparisons
Estimate	Inference object from Estimate function

**Value**

a log-likelihood of the data under the Zemel model

**Examples**

```
Estimate <- Generate.Zemel.Parameters(10)
pairs <- Generate.Zemel.Ranks.Pairs(Estimate$Score, 10, 10)
Likelihood.Zemel(pairs, Estimate)
```

---

MSE	<i>Calculates MSE between non-diagonal entries of two matrices if the diagonal elements are 0s</i>
-----	----------------------------------------------------------------------------------------------------

---

**Description**

Calculates MSE between non-diagonal entries of two matrices if the diagonal elements are 0s

**Usage**

```
MSE(A, B)
```

**Arguments**

A	first matrix
B	second matrix

**Value**

MSE divergence

**Examples**

```
MSE(matrix(runif(25), nrow=5), matrix(runif(25), nrow=5))
```

---

```
Normal.MultiType.Pairwise.Prob
```

*Pairwise Probability for Normal Multitype Model*

---

**Description**

Given alternatives a and b (both items from the inference object) what is the probability that a beats b?

**Usage**

```
Normal.MultiType.Pairwise.Prob(a, b)
```

**Arguments**

a	list containing parameters for a
b	list containing parameters for b

**Value**

probability that a beats b

---

```
Normal.Pairwise.Prob
```

*Pairwise Probability for Normal Model*

---

**Description**

Given alternatives a and b (both items from the inference object) what is the probability that a beats b?

**Usage**

```
Normal.Pairwise.Prob(a, b)
```

**Arguments**

a	list containing parameters for a
b	list containing parameters for b

**Value**

probability that a beats b

---

PL.Pairwise.Prob      *Pairwise Probability for PL Model*

---

**Description**

Given alternatives a and b (both items from the inference object) what is the probability that a beats b?

**Usage**

PL.Pairwise.Prob(a, b)

**Arguments**

a                      list containing parameters for a  
 b                      list containing parameters for b

**Value**

probability that a beats b

---

scores.to.order      *Converts scores to a ranking*

---

**Description**

takes in vector of scores (with the largest score being the one most preferred) and returns back a vector of WINNER, SECOND PLACE, ... LAST PLACE

**Usage**

scores.to.order(scores)

**Arguments**

scores                the scores (e.g. means) of a set of alternatives

**Value**

an ordering of the index of the winner, second place, etc.

**Examples**

```
scores <- Generate.RUM.Parameters(10, "exponential")$Mean
scores.to.order(scores)
```

---

scramble	<i>Scramble a vector</i>
----------	--------------------------

---

**Description**

This function takes a vector and returns it in a random order

**Usage**

```
scramble(x)
```

**Arguments**

x                    a vector

**Value**

a vector, now in random order

**Examples**

```
scramble(1:10)
```

---

turn_matrix_into_table	<i>Converts a matrix into a table</i>
------------------------	---------------------------------------

---

**Description**

takes a matrix and returns a data frame with the columns being row, column, entry

**Usage**

```
turn_matrix_into_table(A, uppertriangle = FALSE)
```

**Arguments**

A                    matrix to be converted  
uppertriangle    if true, then will only convert the upper right triangle of matrix

**Value**

a table with the entries being the row, column, and matrix entry

---

TVD	<i>Calculates TVD between two matrices</i>
-----	--------------------------------------------

---

**Description**

Calculates TVD between two matrices

**Usage**

```
TVD(A, B)
```

**Arguments**

A	first matrix
B	second matrix

**Value**

Total variation distance

**Examples**

```
TVD(matrix(runif(25), nrow=5), matrix(runif(25), nrow=5))
```

---

Visualization.Empirical	<i>RPD Visualization</i>
-------------------------	--------------------------

---

**Description**

Creates histograms of the empirical rank position distribution for each alternative in rank data

**Usage**

```
Visualization.Empirical(Data, ymax, ncol = 5, names = NA)
```

**Arguments**

Data	full, top partial, or sub partial data
ymax	maximum value of density to show on graph
ncol	number of columns visualization is displayed in
names	names of alternatives

**Examples**

```
library(ggplot2)
library(gridExtra)
data(Data.Test)
Visualization.Empirical(Data.Test, 0.5)
```

---

Visualization.MultiType

*Multitype Random Utility visualizer*

---

**Description**

Multitype Random Utility visualizer

**Usage**

```
Visualization.MultiType(multitype.output, min, max, names, ncol)
```

**Arguments**

multitype.output	output from a multitype fitter
min	left boundary of graphed x-axis
max	right boundary of graphed x-axis
names	names of alternatives
ncol	number of columns in final output

**Value**

none

**Examples**

```
library(ggplot2)
library(gridExtra)
Data.Tiny <- matrix(c(1, 2, 3, 3, 2, 1, 1, 2, 3), ncol = 3, byrow = TRUE)
multitype.output <- Estimation.RUM.MultiType.MLE(Data.Tiny, iter = 1, dist = "norm", ratio = .5)
names <- 1:3
#run the following code to make plots
#plots <- Visualization.MultiType(multitype.output, -2, 2, names, 3)
```

---

Visualization.Pairwise.Probabilities

*Creates pairwise matrices to compare inference results with the empirical pairwise probabilities*

---

### Description

Creates pairwise matrices to compare inference results with the empirical pairwise probabilities

### Usage

```
Visualization.Pairwise.Probabilities(Data.pairs, Parameters, get.pairwise.prob,
  name.of.method)
```

### Arguments

Data.pairs      datas broken into pairs  
 Parameters      The Parameter element of a result from an Estimation function  
 get.pairwise.prob      function that we use to generate the pairwise probability of beating  
 name.of.method      names of the alternatives

### Value

none

### Examples

```
library(ggplot2)
library(gridExtra)
data(Data.Test)
Data.Test.pairs <- Breaking(Data.Test, "full")
Parameters <- Estimation.PL.GMM(Data.Test.pairs, 5)$Parameters
PL.Pairwise.Prob <- function(a, b) a$Mean / (a$Mean + b$Mean)
Visualization.Pairwise.Probabilities(Data.Test.pairs, Parameters, PL.Pairwise.Prob, "PL")
```

---

Visualization.RUMplots

*RUMplot visualization*

---

### Description

Creates marginal random utility density plots for each alternatives given an Estimation object for a PL or Nonparameteric model



**Usage**

```
Visualization.RUMplots(RUM = "Exponential", Estimate = NA, min = -5,
  max = 5, ncol = 5, names = NA)
```

**Arguments**

RUM	choice of Exponential, Gumbel, or Nonparametric
Estimate	fitted RUM object
min	minimum x value to display
max	maximum x value to display
ncol	number of columns in the visualization
names	names of alternatives

**Examples**

```
library(ggplot2)
library(gridExtra)
Data.Tiny <- matrix(c(1, 2, 3, 3, 2, 1, 1, 2, 3), ncol = 3, byrow = TRUE)
Estimate <- Estimation.PL.GMM(Breaking(Data.Tiny, method = "full"), m = 3)
Visualization.RUMplots("Exponential", Estimate, names = 1:3)
```

---

Zemel.Pairwise.Prob    *Pairwise Probability for Zemel*

---

**Description**

Given alternatives a and b (both items from the inference object) what is the probability that a beats b?

**Usage**

```
Zemel.Pairwise.Prob(a, b)
```

**Arguments**

a	list containing parameters for a
b	list containing parameters for b

**Value**

probability that a beats b

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